# **Transducers for Medical Imaging**

Erik V. Thomsen





# Agenda

- The probe
- The PZT transducer
- The CMUT transducer
  - Introduction
  - Design
  - Fabrication
  - Use
- Conclusions
- Problem solving: Design your transducer!

# How does the probe work?





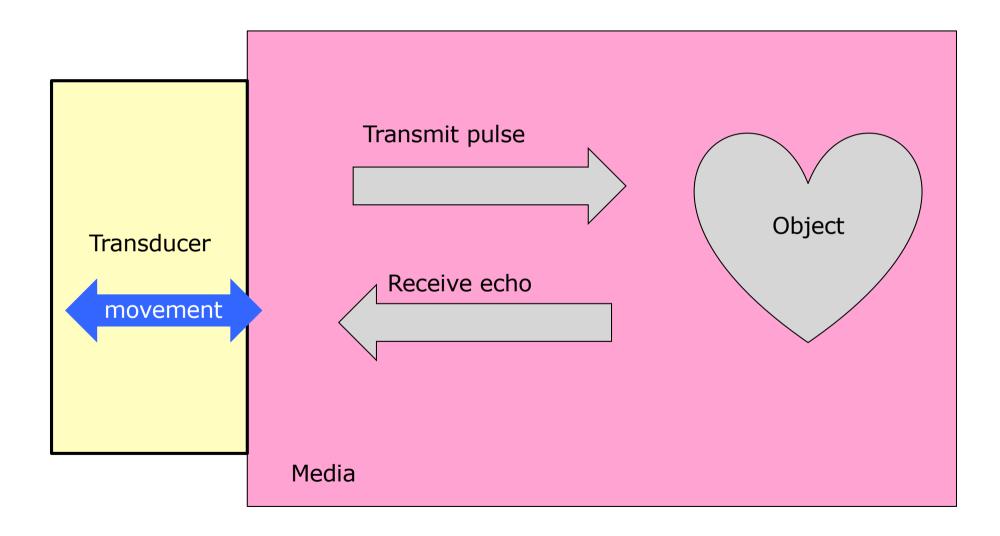
# 1D PZT probe



2D CMUT probe

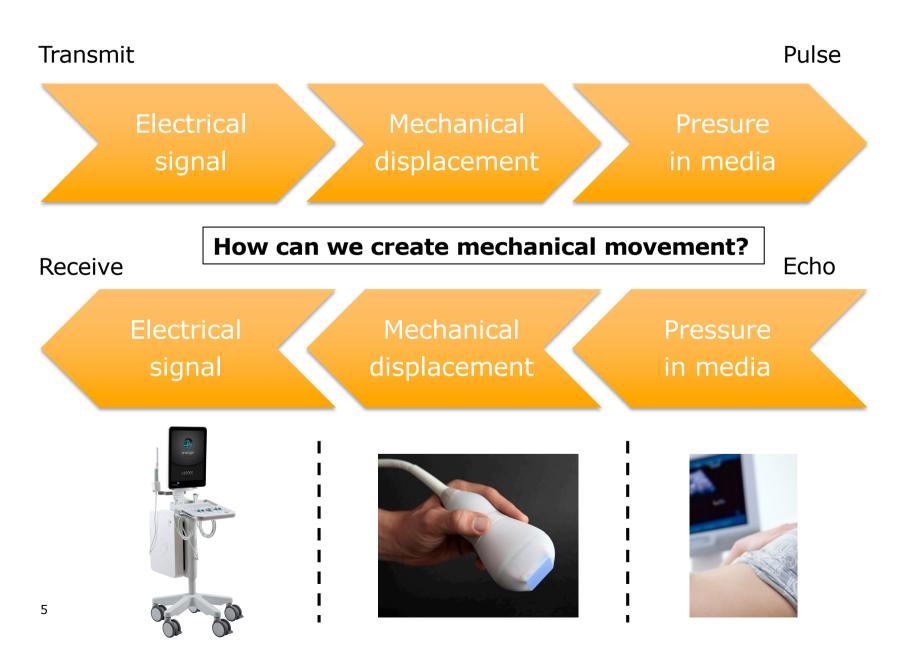


## Transduction



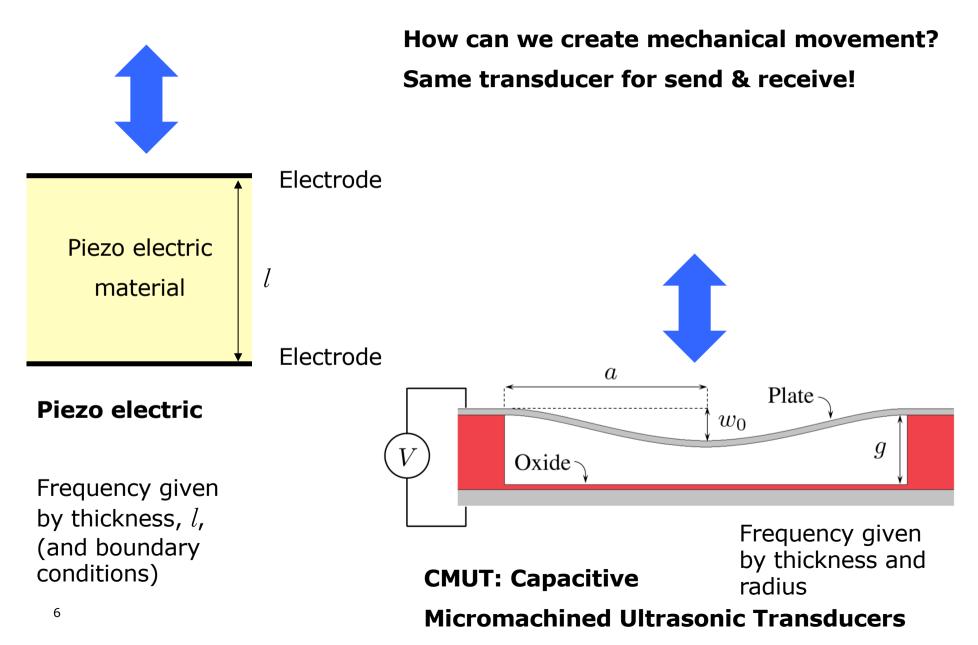
# Transduction





# **Transducer principles: PZT & CMUT**







# **CMUT's: Pros and cons**

Piezoelectric transducers	CMUTs
<ul> <li>Conventional technology - well known</li> <li>Elements defined mechanically <ul> <li>Limited design flexibility</li> <li>Size limitation 20 µm</li> </ul> </li> <li>High mechanical impedance <ul> <li>Z<sub>media</sub>.</li> <li>Z<sub>media</sub>.</li> <li>Need impedance matching layers</li> </ul> </li> <li>Narrow bandwidth, &lt;100%</li> <li>High pressure</li> <li>Difficult direct integration with CMOS</li> <li>Contains lead</li> </ul>	<ul> <li>New technology - not as mature</li> <li>Elements defined by photolithography <ul> <li>Large design flexibility (different elements in TX &amp; RX, lateral flexibility)</li> <li>Size limitation 1 µm</li> </ul> </li> <li>Very low plate mechanical impedance <ul> <li>Z<sub>media.</sub> » Z<sub>mech.</sub></li> <li>No need for impedance matching</li> </ul> </li> <li>Wide bandwidth, &gt;100% → Improved axial resolution</li> <li>Pressure-bandwidth trade off</li> <li>Integration capability with silicon CMOS</li> <li>Lead free</li> <li>Potential for low cost (&amp; high yield)</li> <li>Do not heat up -&gt; coded excitation</li> </ul>
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CMUT's have been promising for 30 years

Still - few products on the marked The PZT transducer rules the game (today) might change (tomorrow?)

# What's inside a probe?

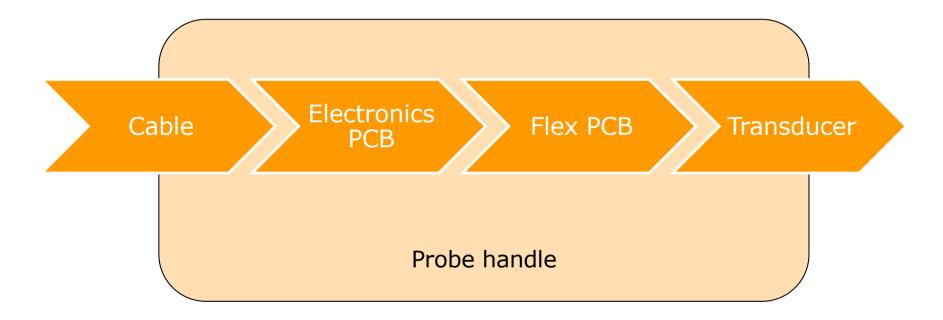




#### Example: 2D CMUT probe



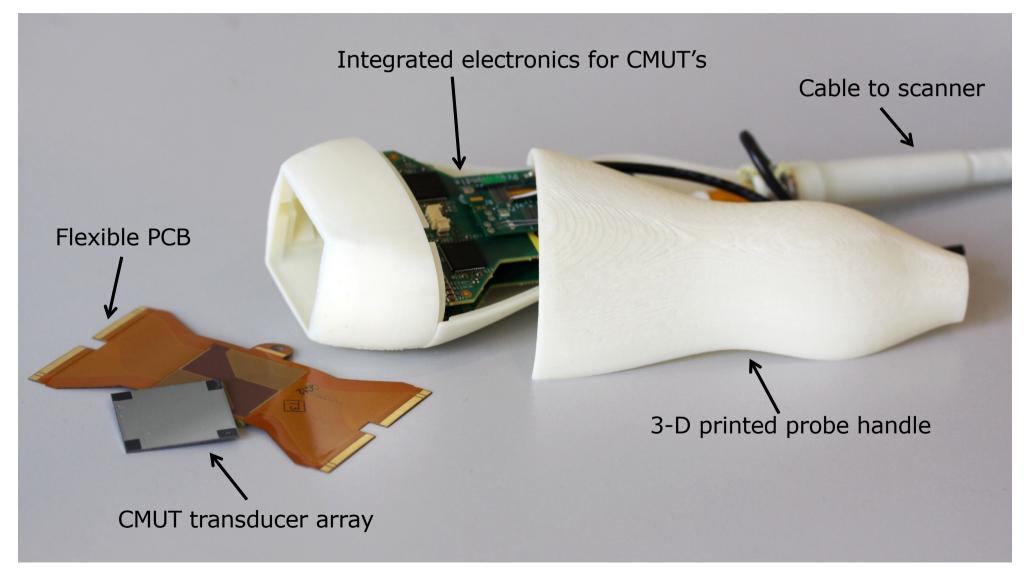




PCB = Printed Circuit Board Flex: Flexible

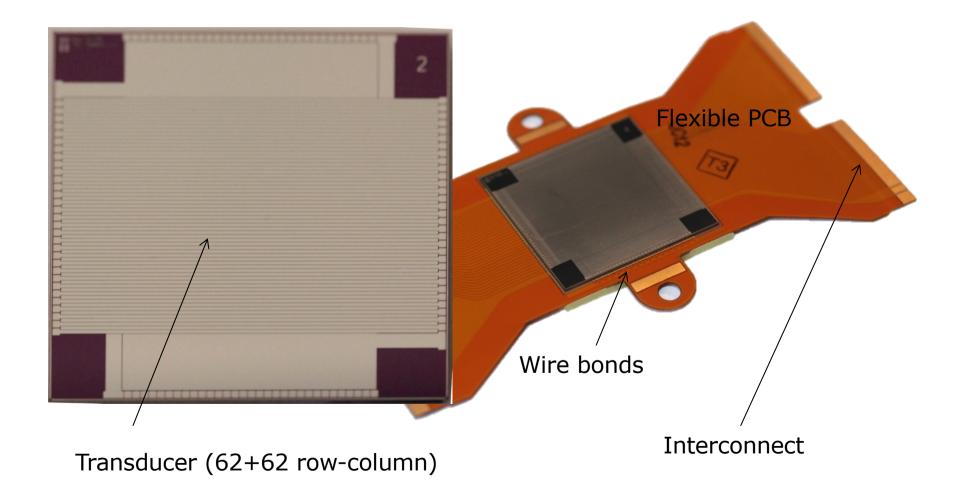


# **Example: 2D CMUT Probe assembly**



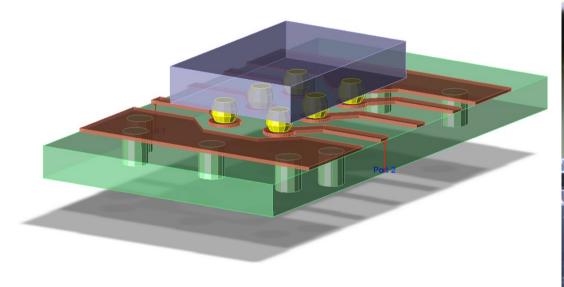


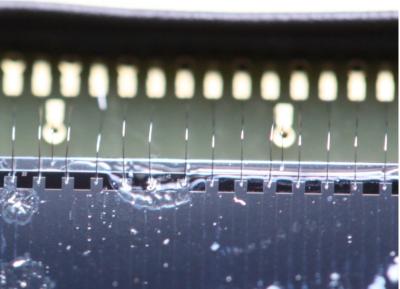
# **Probe Assembly – Flexible PCB**





# **Interconnect technology**





#### Flip-chip:

Transducer mounted to PCB using solder bumps

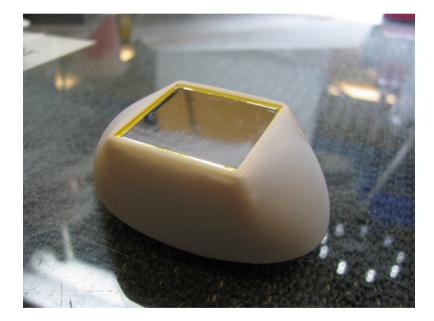
#### Wire bonding:

Transducer mounted to PCB using thin ( $\emptyset$ 20  $\mu$ m) wires

# **Probe Assembly – Nose piece**



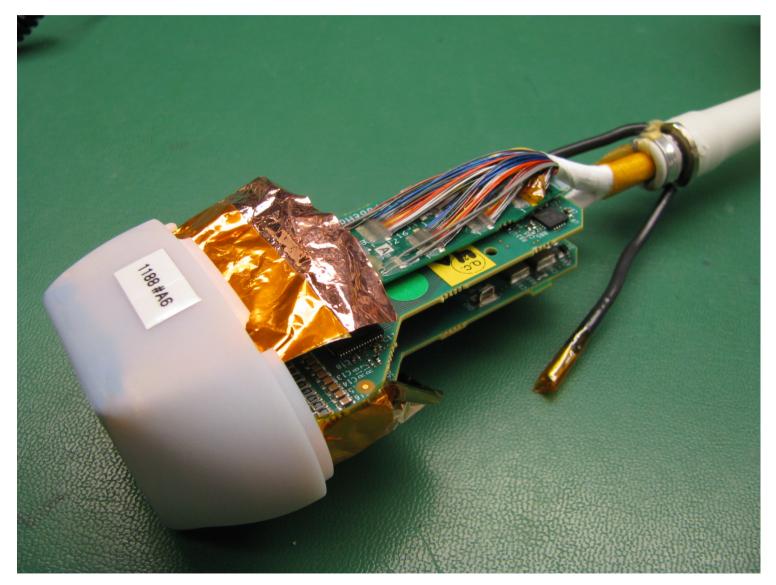
- Transducer array mounted in nose piece with grounded shielding layer
- Polymer coating for physical and electrical insulation







# **Probe Assembly – Attach to electronics and cable**





# **Probe Assembly – PCB shielding**



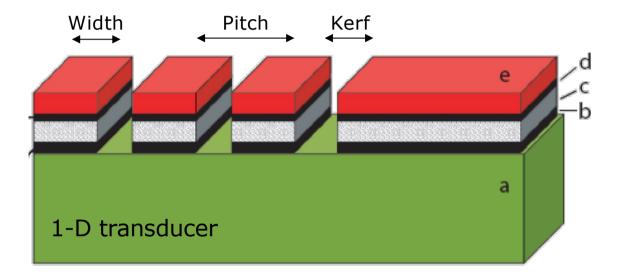
# **Probe Assembly – Finished Probe**



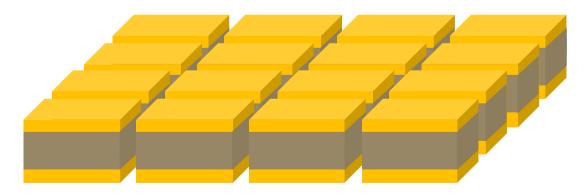




# **Array based transducers**



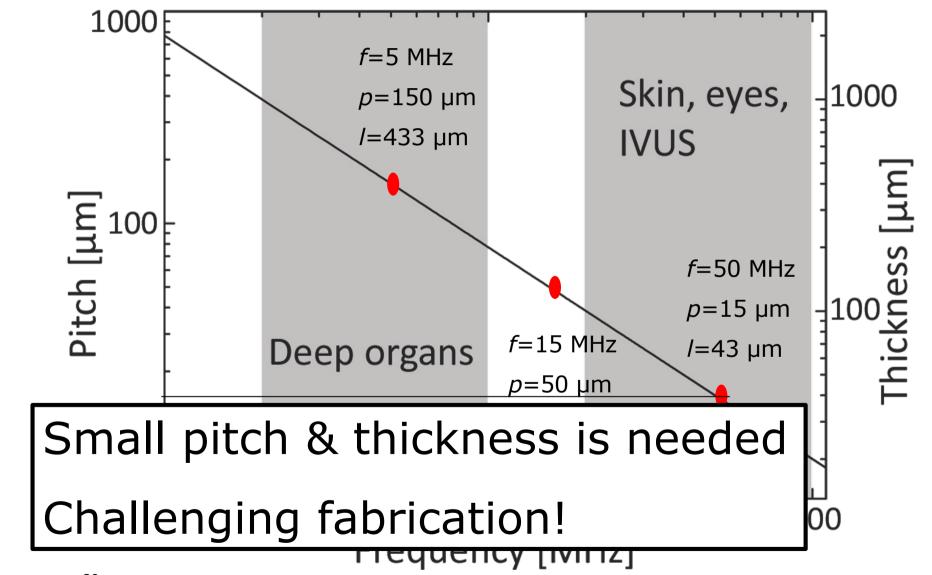
Width = pitch - kerf Fill factor = width/pitch



2-D transducer

# **PZT transducer dimensions**

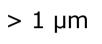
For arrays: Pitch must be  $\lambda/2$  to avoid grating lobes!



# **Fabrication technologies**

How to pattern *lateral* structures in the micrometer range?

- Fine mechanics
- Micro mechanics > 1 μr
- Nano technology



< 1 µm

> 25 µm

Saw blade

#### Mechanical shaping:

Grinding, dicing & polishing

Silicon based micro fabrication: Lithography Deposition Etching

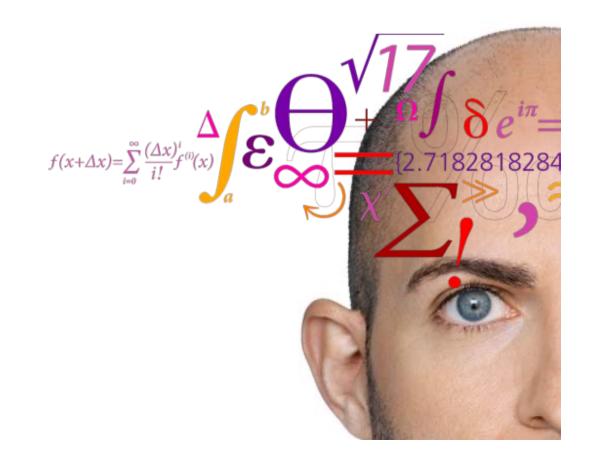








### **The PZT transducer**

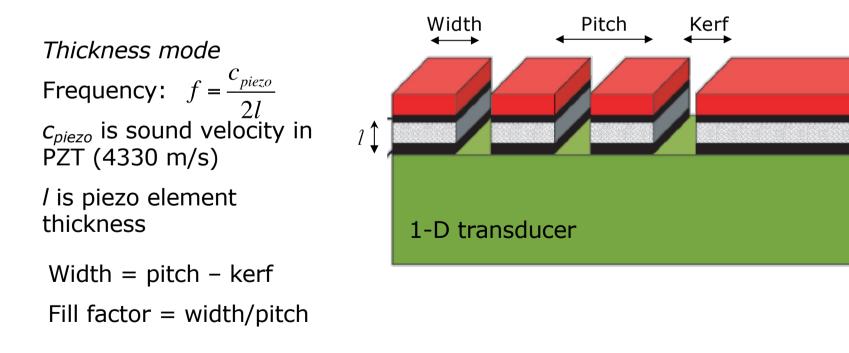


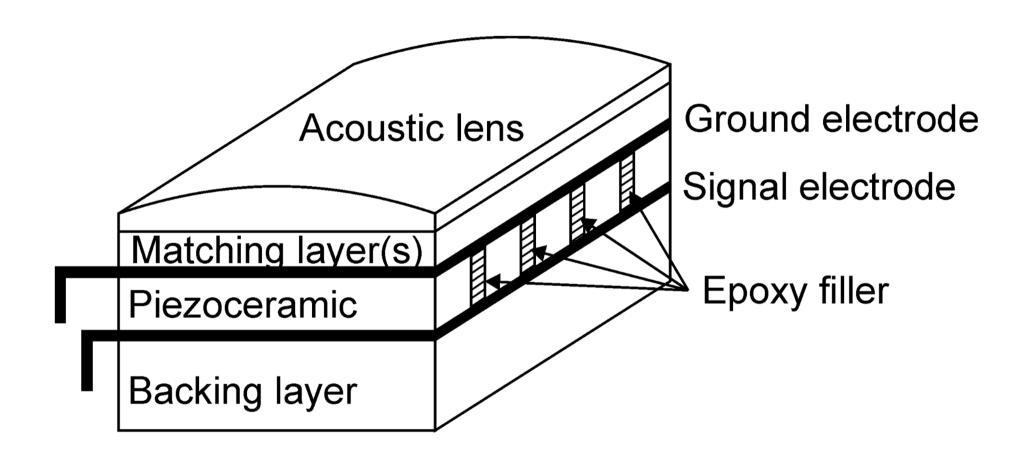


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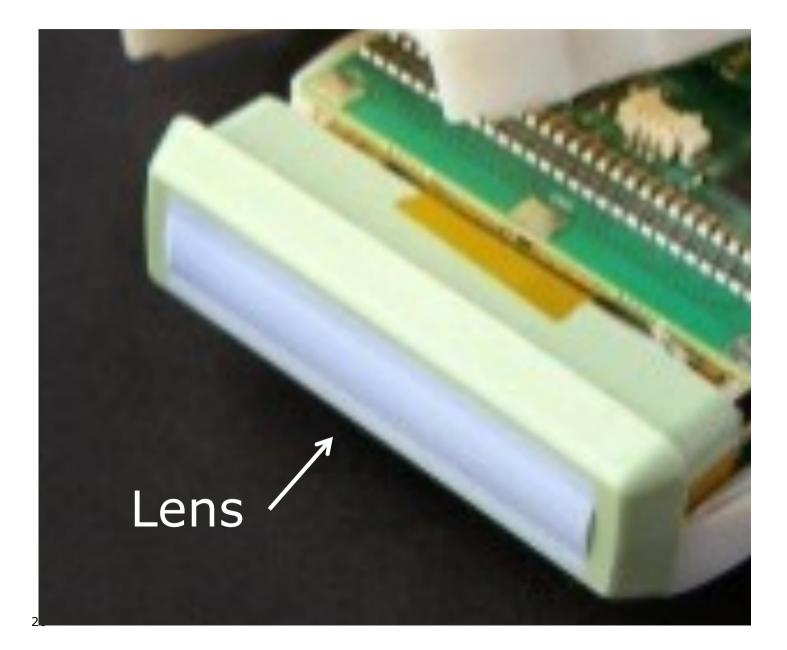
# **Conventional 1D PZT transducer array**

- a) Backing layer (reduce ringing)
- b) Bottom electrode
- c) Each element is a piezoelectric block
- d) Top electrode
- e) Matching layers (high to low acoustic impedance)



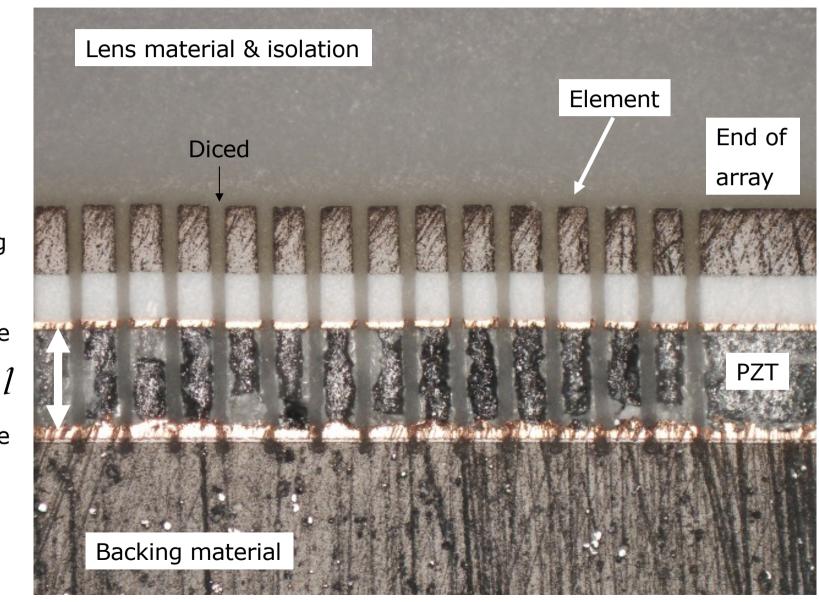






# DTU

# **A PZT transducer: Cross-section**

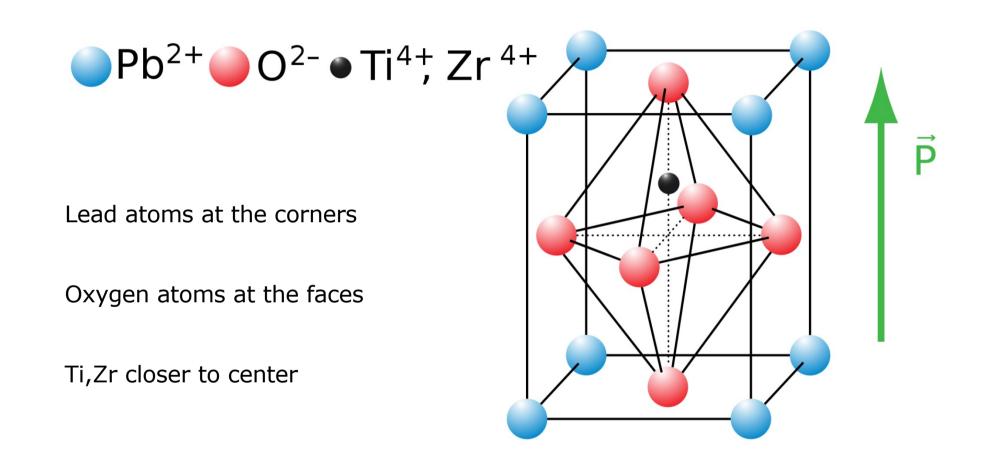


Matching layers Electrode

Electrode

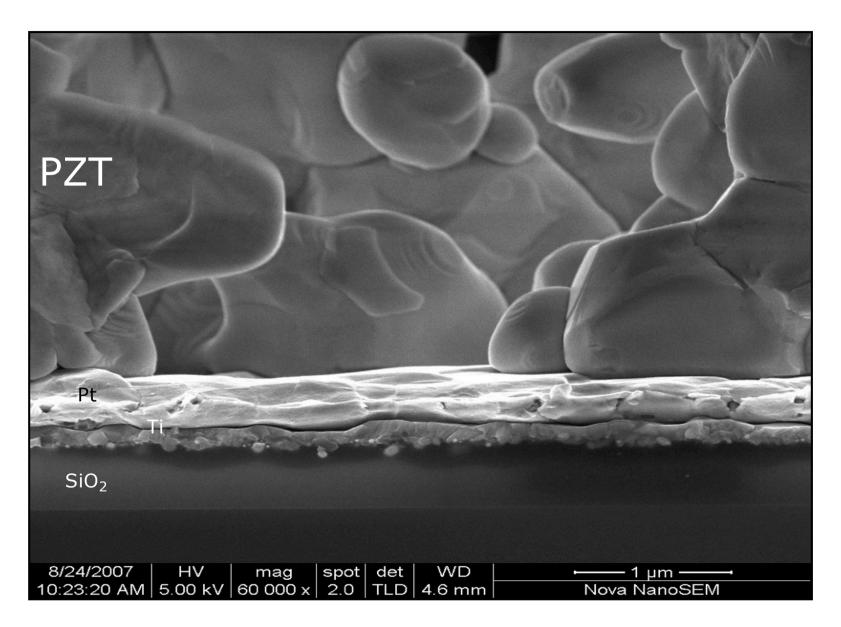


## **Structure of PZT**





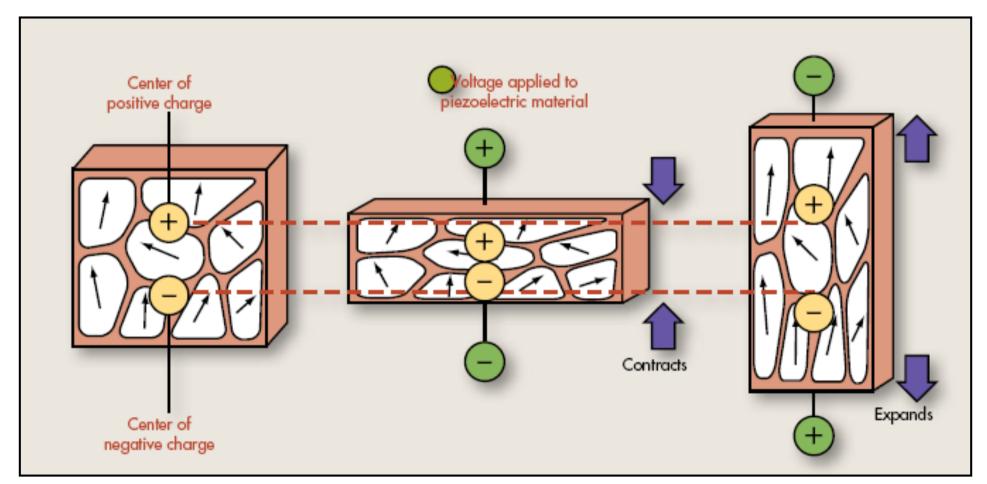
# Inside PZT ...



# **Working principle**

The PZT transducer is based on the piezoelectric transducer principle:

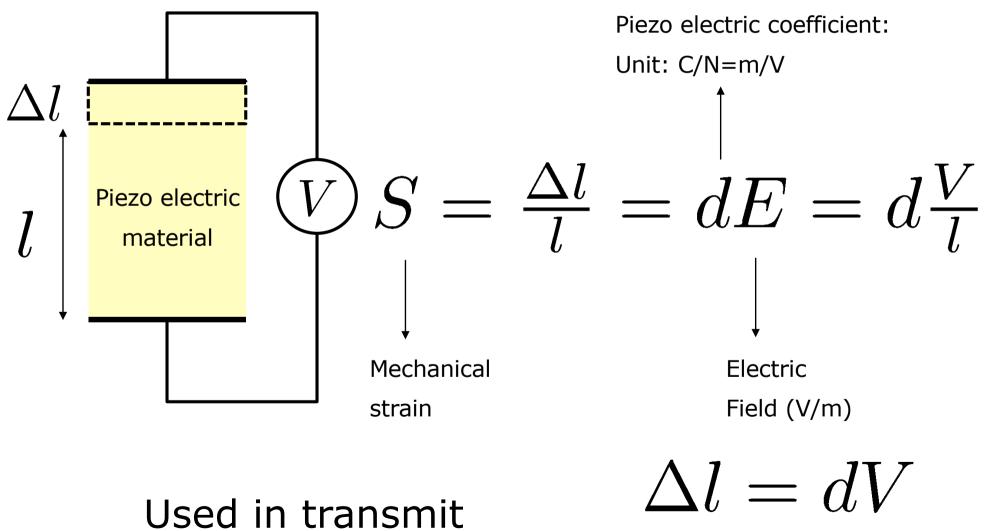
- Direct effect: Stress => Charge build up
- Converse effect: Applied charge (voltage) => Strain



DTU



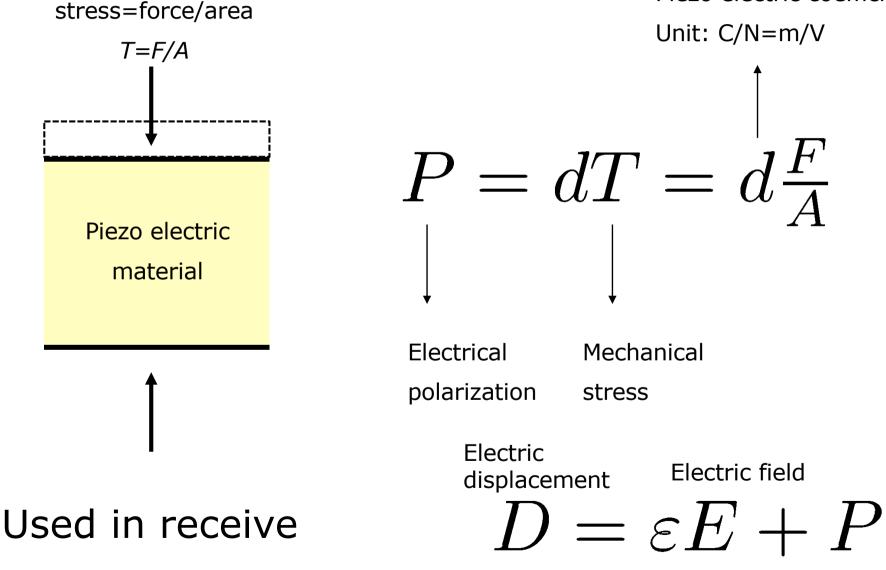
# Working principle in 1D: Converse effect



# **Working principle in 1D: Direct effect**



Piezo electric coefficient:



Permittivity

# **Receive – in 1D**



Electrical polarization

T=force/area=F/A=pressure=p

$$P = dT = d\frac{F}{A} = dp$$

*T*: Mechanical stress *d*: Piezo electric coefficient

Electric displacement

$$D = \varepsilon E + P = \varepsilon \frac{V}{l} + dp = 0$$

Permittivity Electric field

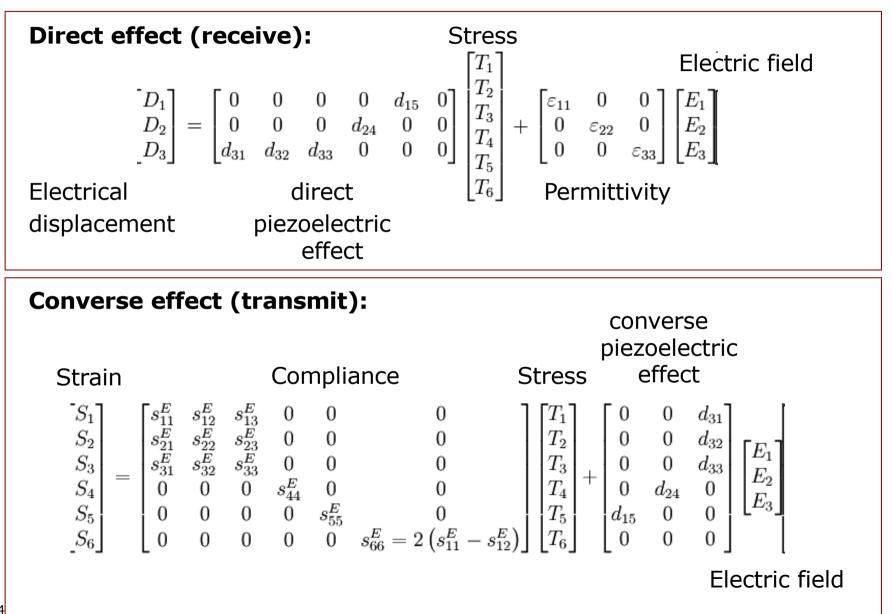
Receive voltage

 $V = \frac{dl}{\varepsilon}p$ 

*E*= Electric field=Voltage/distance=*V*/*I* 

# DTU

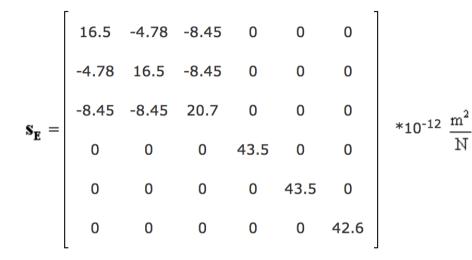
# Working principle in 3D: Coupled equations



# **Properties of PZT (5-H)**



#### Compliance



#### **Piezoelectric Coupling**

$$\mathbf{d} = \begin{bmatrix} 0 & 0 & 0 & 0 & 741 & 0 \\ 0 & 0 & 0 & 741 & 0 & 0 \\ -274 & -274 & 593 & 0 & 0 & 0 \end{bmatrix} *10^{-12} \frac{\mathrm{C}}{\mathrm{N}}$$

**Relative Permittivity** 

Ν

$$\frac{\mathbf{\varepsilon}_{\mathbf{T}}}{\varepsilon_{0}} = \begin{bmatrix} 3130 & 0 & 0 \\ 0 & 3130 & 0 \\ 0 & 0 & 3400 \end{bmatrix}, \quad \varepsilon_{0} = 8.854 * 10^{-12} \frac{\mathrm{F}}{\mathrm{m}}$$



# **Characteristics of piezoelectric transducer**

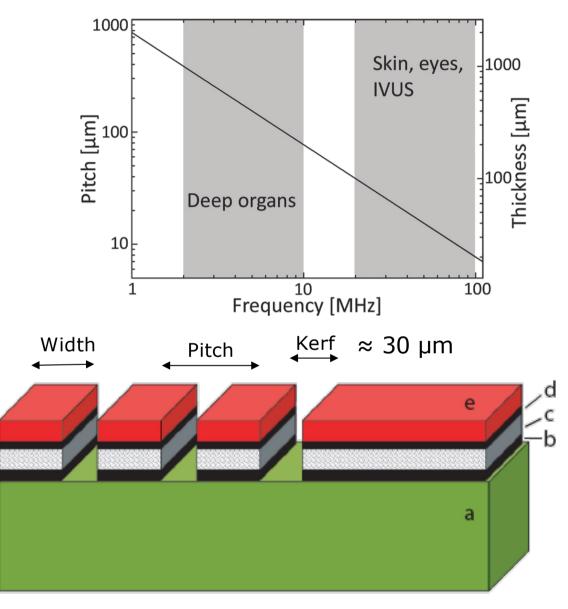
- Thickness mode

   Frequency f = C<sub>piezo</sub>/2l
   c<sub>piezo</sub> is sound velocity in PZT (4330 m/s)
   l is element thickness
- Element pitch =  $0.5 \lambda_{media}$
- Width = pitch-kerf

#### 3 MHz:

 $\lambda_{media} \approx 500 \ \mu m$ Pitch  $\approx 250 \ \mu m$ Thickness  $\approx 722 \ \mu m$ Width  $\approx 220 \ \mu m$ 







# **Advanced PZT transducer design**

BioSono KLM 2.0

Some tools:

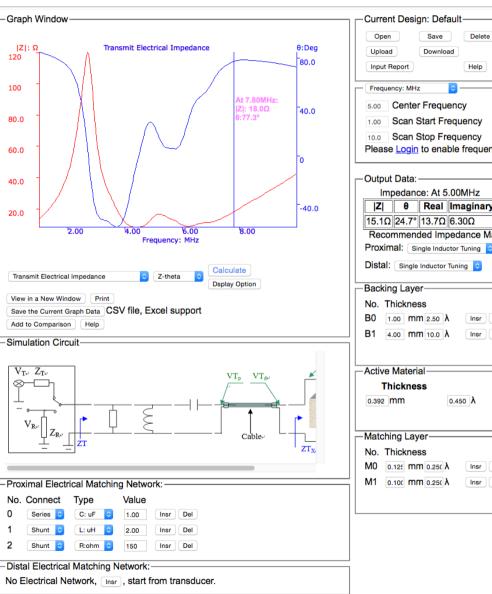
- PZCAD •
- COMSOL •
- KLM modeling ٠
- OnScale •

On-line KIM tool: https://www.biosono.com/

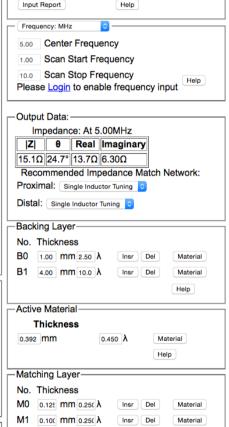
(https://biosono.com/?page id=91)

Onscale has a 10 core hour/month free account

https://onscale.com



**Technical Description** 



Help

Home Ultrasound Calculator Beam Profile Ultrasound Electronics



# BREAK

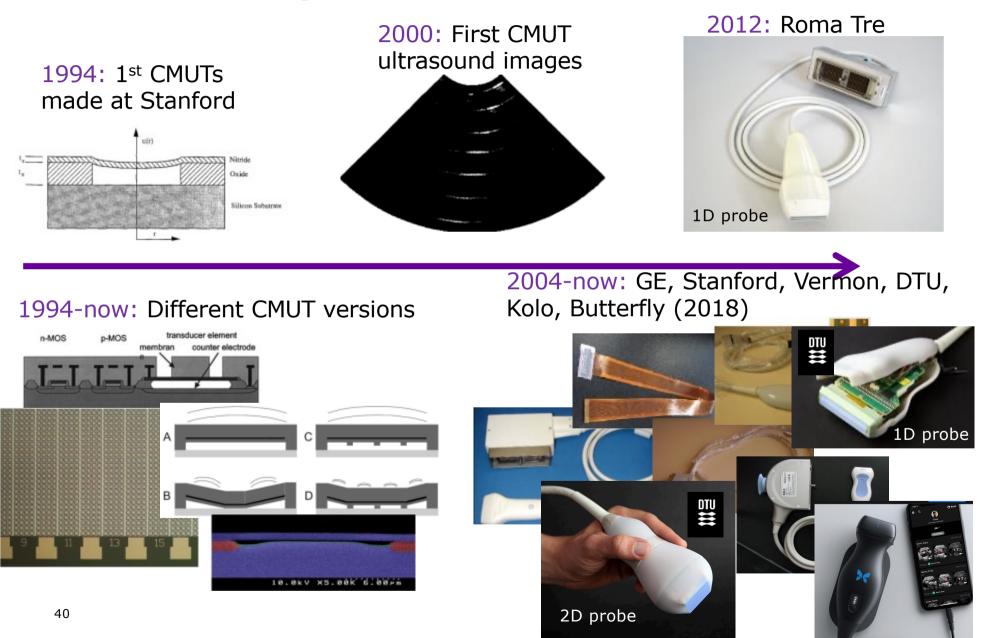


# THE CMUT TRANSDUCER

Capacitive Micro-machined Ultrasonic Transducers

### **CMUT: History**







### **Butterfly – 2018 – portable ultrasound**

Butterfly							About	Su
iQ	Home	Product	Tech	Clinical	Specs	Pricing	FAQ	
CMUT based probe				ng under \$	62k.			
Ultrasound-on-Chip <sup>™</sup> No more piez		~r\/	ets	10::		MI Hz i Gard	.ıl २ ■ 0	
Semiconductor-based u high performance imagin at a dramatically lower co	ltras ng ar	ound	mea	ns			2 - 3 - 4 - 5 - 6 - 7 - 8 - 9 - 10 - 11 - 12 - 13 - 14 -	







### The CMUT building block: Capacitor

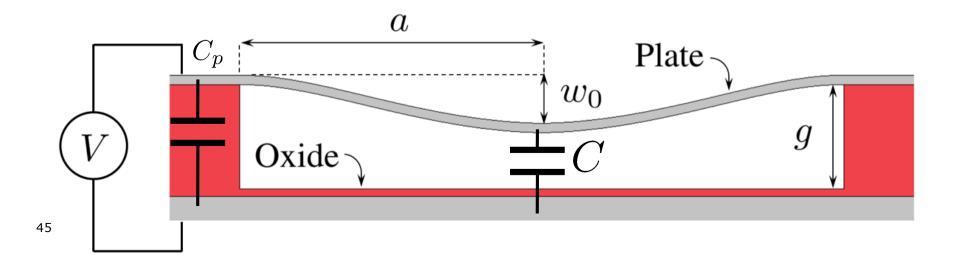
The CMUT is a capacitive device:

$$C_{\rm tot} = C + C_p$$

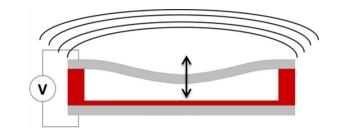
#### **Transmit:**

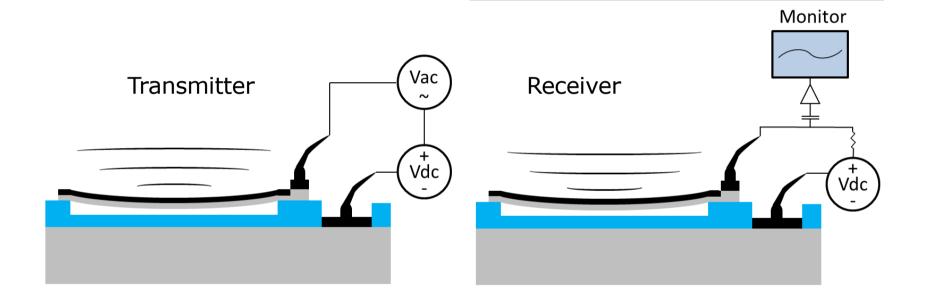
Use DC voltage to increase coupling coefficient Actuation is performed by varying the voltage

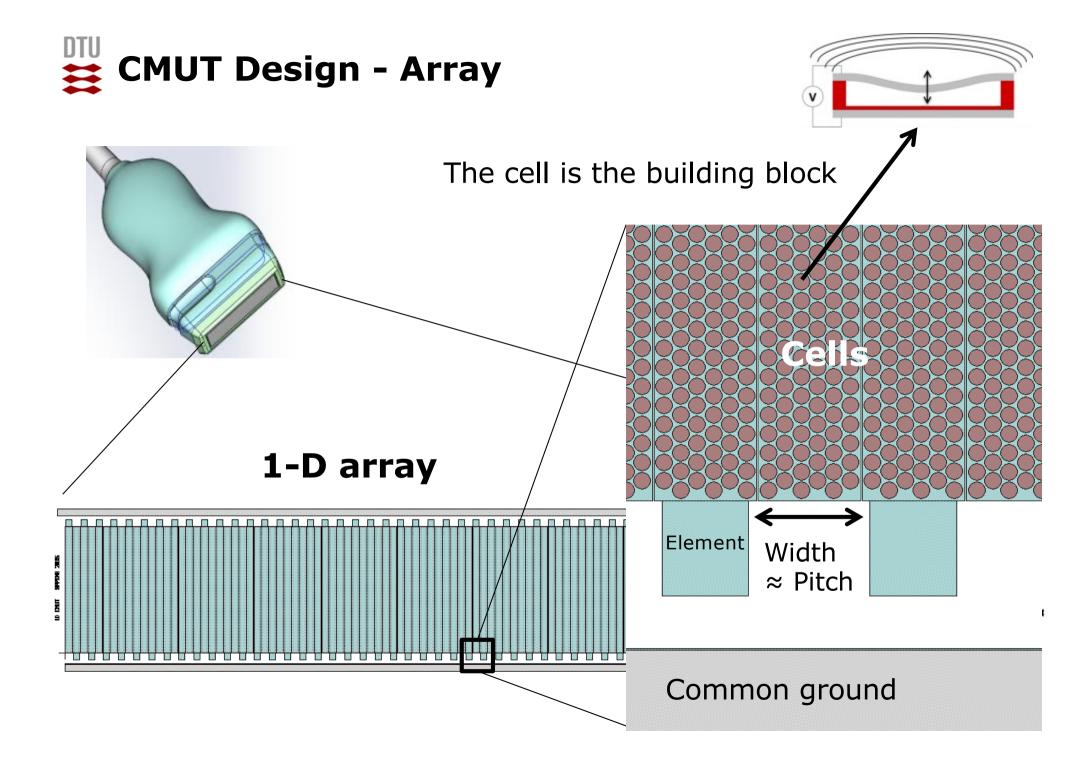
**Receive:** Change in capacitance is detected







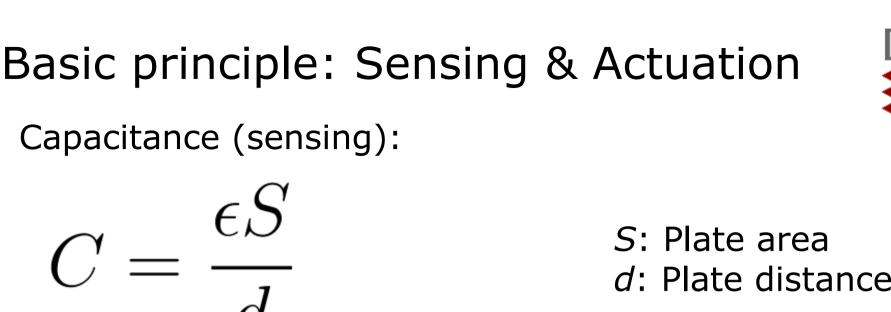






## UNDERSTANDING CAPACITIVE TRANSDUCERS

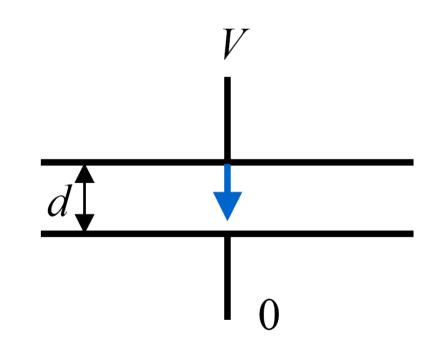
What is pull-in and spring softening?

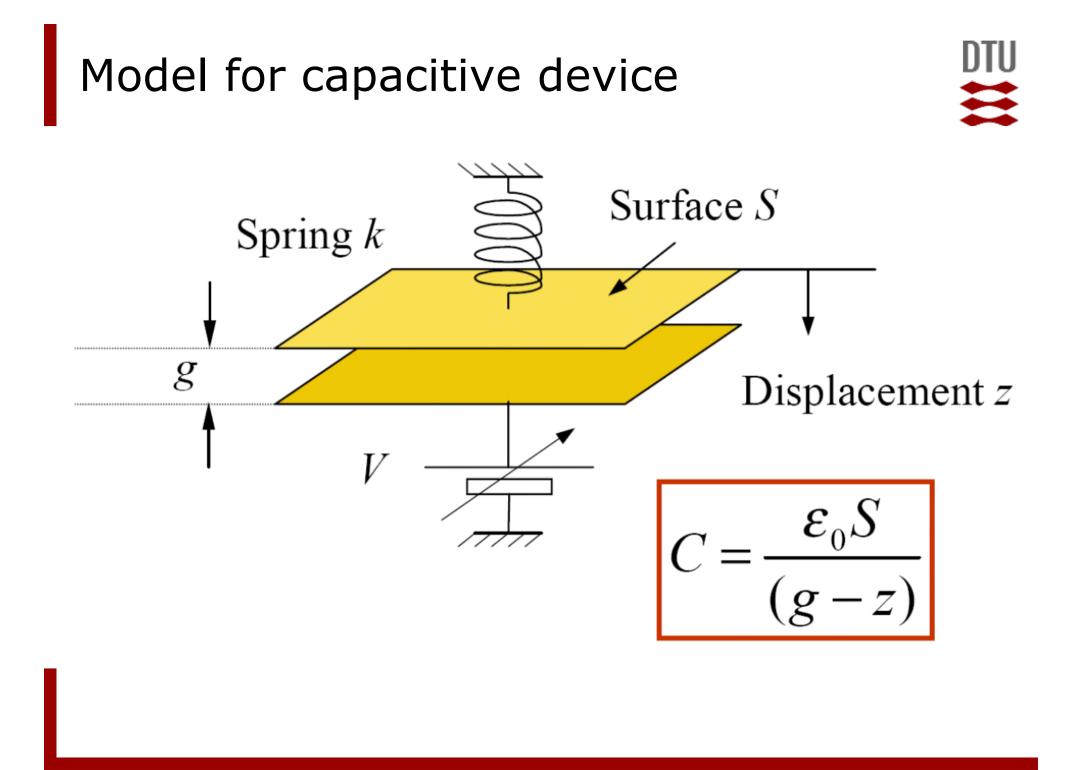


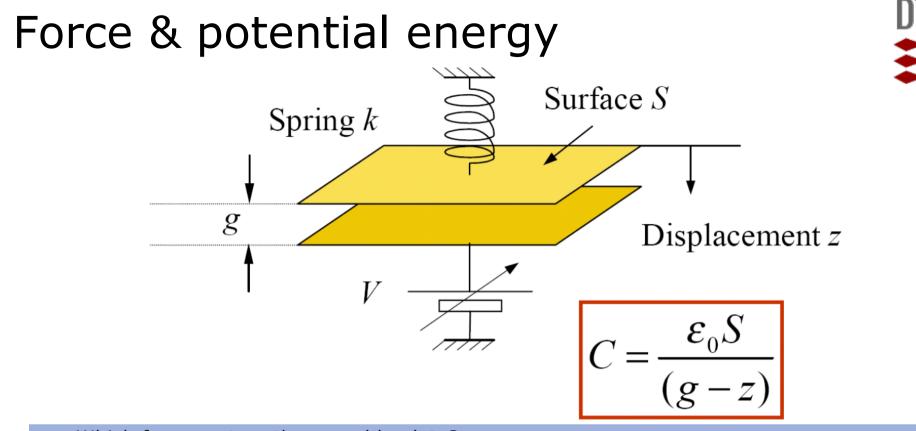
Attractive force between the plates (actuation):

$$F = \frac{1}{2} \frac{\epsilon S}{d^2} V^2$$

d: Plate distance

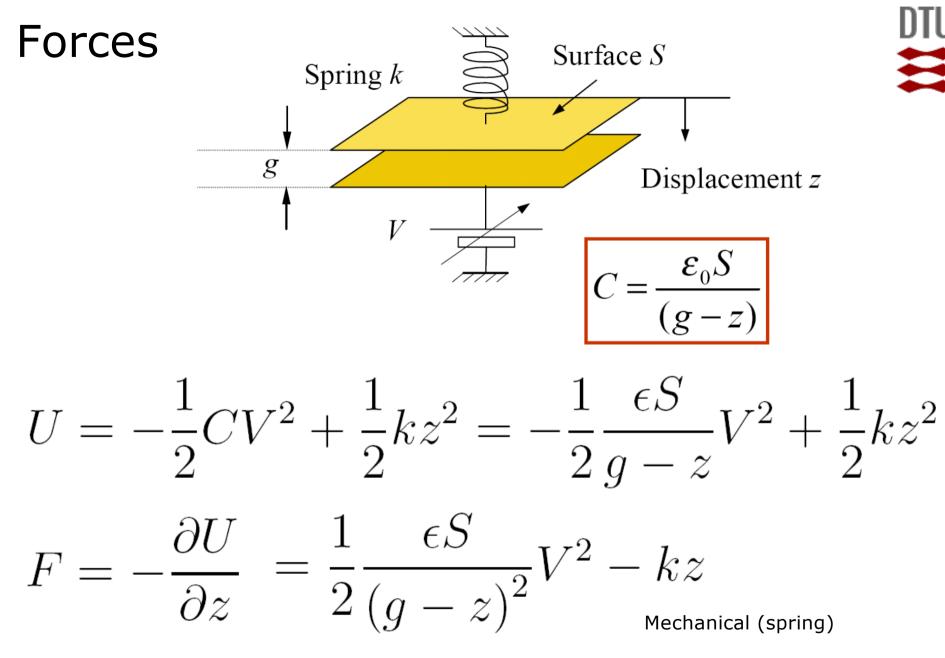




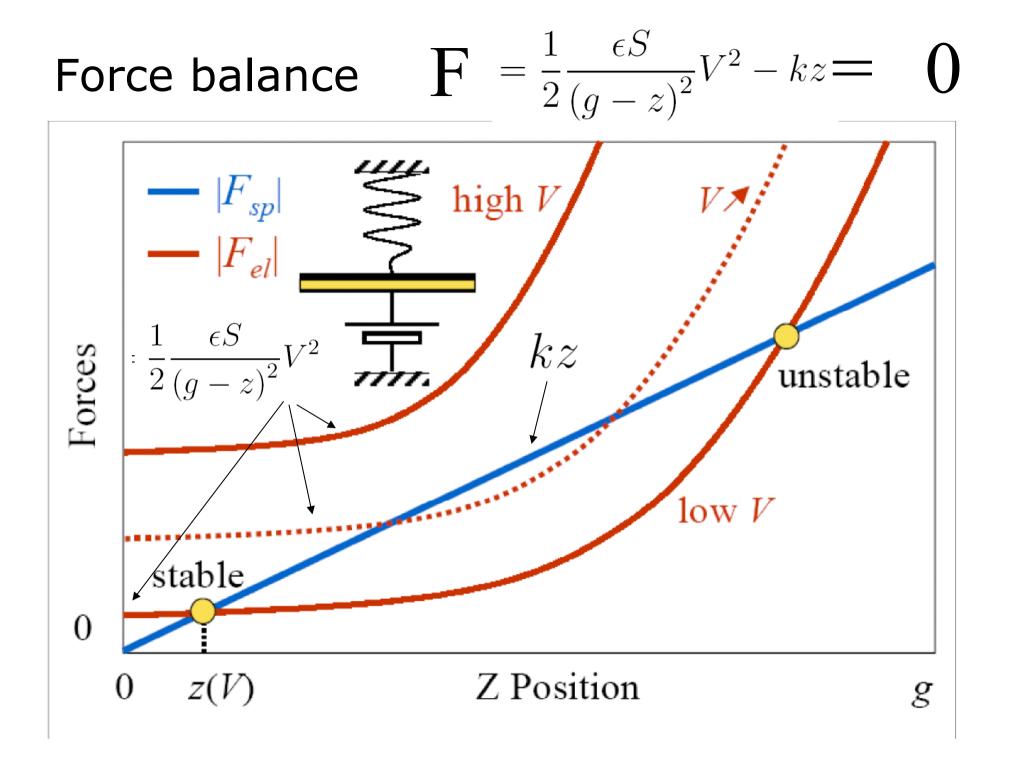


- Which forces act on the movable plate?
- How does force/energy depend on z and V?
- Calculate the force as function of *z* and *V*

Potential energy: Force:  $U = -\frac{1}{2}CV^2 + \frac{1}{2}kz^2 \qquad F = -\frac{\partial U}{\partial z}$ 



Electrostatic



## Stable equilibrium



- Condition 1: Total force = 0
- Condition 2: Small movement lowers force

(i.e. minimum in potential energy)

$$U = -\frac{1}{2}CV^{2} + \frac{1}{2}kz^{2} = -\frac{1}{2}\frac{\epsilon S}{g-z}V^{2} + \frac{1}{2}kz^{2}$$

$$F = -\frac{\partial U}{\partial z} = \frac{1}{2} \frac{\epsilon S}{\left(g-z\right)^2} V^2 - kz$$

$$\delta F = \left. \frac{\partial F}{\partial z} \right|_V \delta z \qquad \text{Must be negative!}$$

# Stable equilibrium

$$\left. \frac{\partial F}{\partial z} \right|_{V} = \frac{\epsilon S}{\left(g-z\right)^{3}} V^{2} - k$$

1 - Stable position:

$$\frac{\epsilon S}{\left(g-z\right)^3}V^2 - k < 0$$

2 – Pull-in voltage:

$$\frac{\epsilon S}{\left(g-z\right)^3}V_{pi}^2 = k$$

DTU

Pull-in voltage

At pull in the electrostatic & the spring force are equal:

$$\frac{1}{2} \frac{\epsilon S}{\left(g-z\right)^2} V_{pi}^2 = kz$$

 $\sim$ 

Pull in voltage:

1

2

$$\frac{\epsilon S}{\left(g-z\right)^3}V_{pi}^2 = k$$

Combining:

$$\frac{\epsilon S}{(g-z)^3} V_{pi}^2 = \frac{1}{2} \frac{1}{z} \frac{\epsilon S}{(g-z)^2} V_{pi}^2$$

What is *z* at pull in?

$$z = \frac{1}{3}g$$





Pull-in distance:

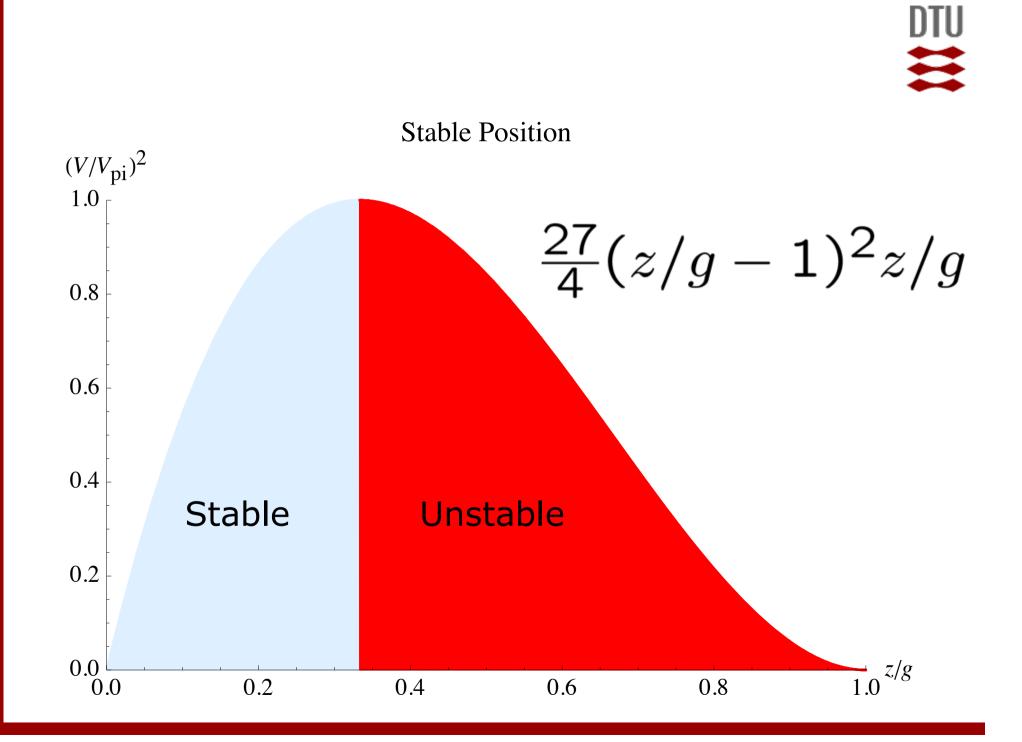
$$z = \frac{1}{3}g$$

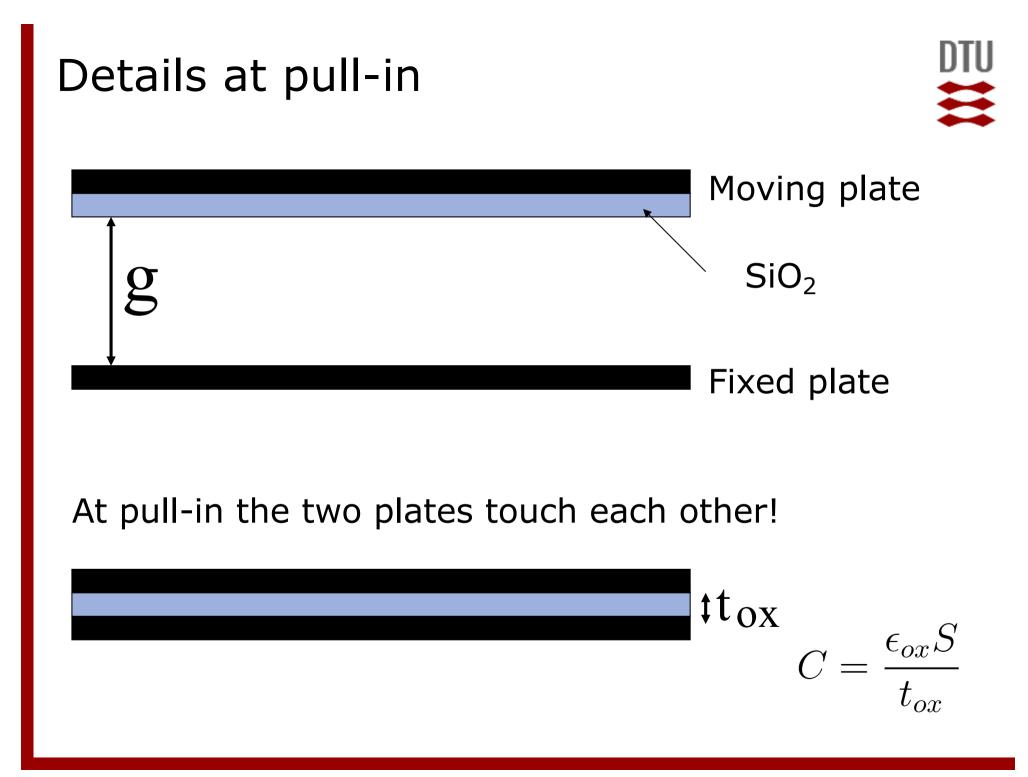
Thus,

Pull-in voltage:

$$V_{pi} = \sqrt{\frac{2\left(g-z\right)^2}{\epsilon S}kz} = \sqrt{\frac{2\left(g-\frac{1}{3}g\right)^2}{\epsilon S}k\frac{1}{3}g} = \sqrt{\frac{8}{27}\frac{kg^3}{\epsilon S}}$$

Depends on  $g^{3/2}$  !





At pull-in the moving plate touches fixed plate

Plate distance is the thickness of the insulating layer

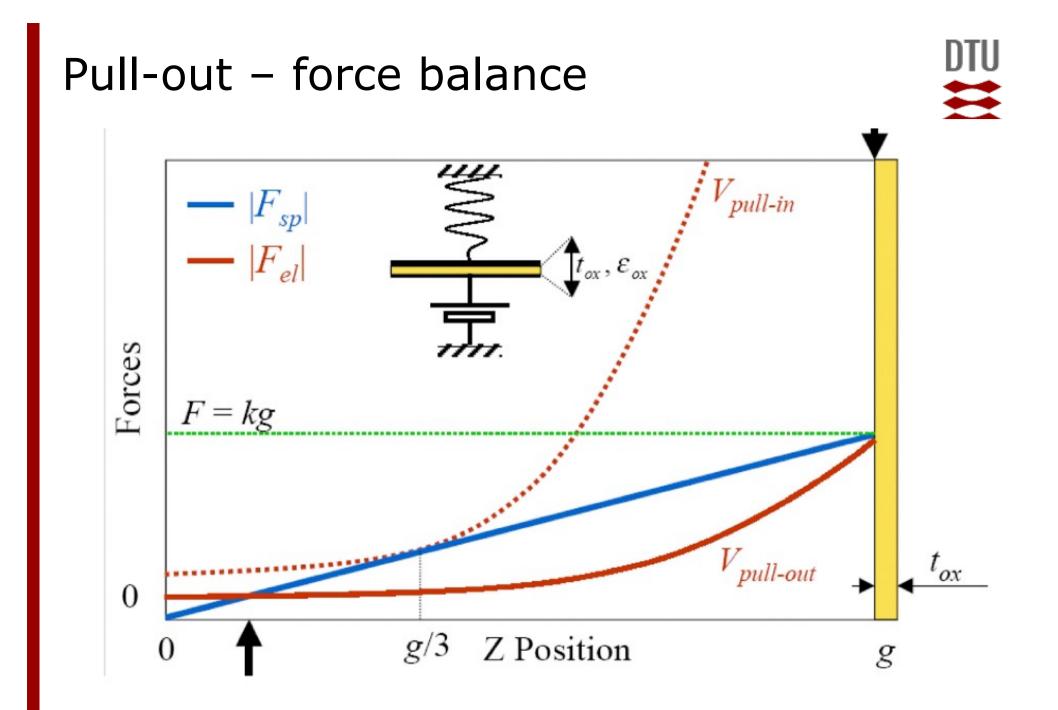
Force balance leads to pull-out condition:

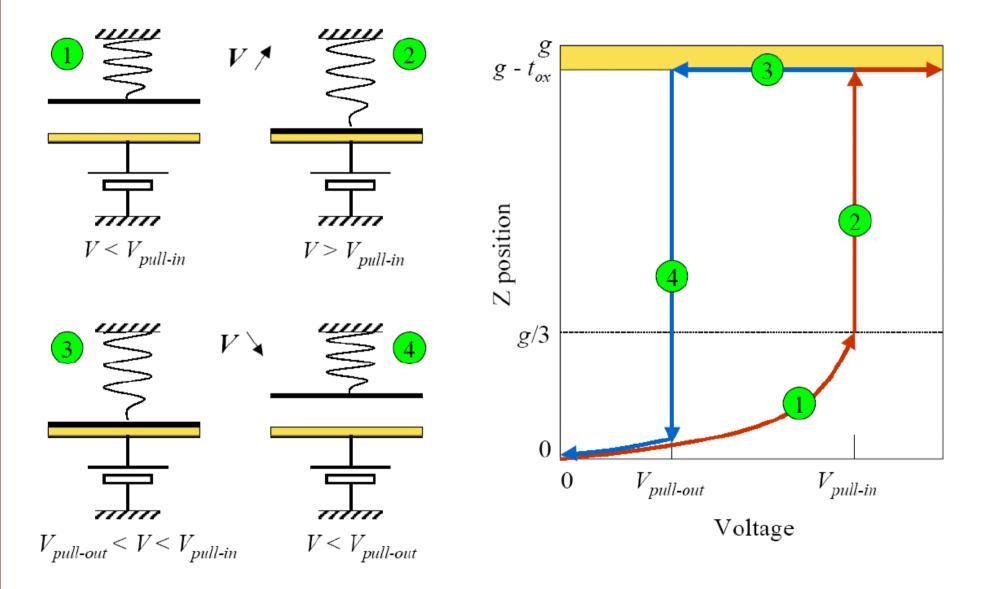
$$\frac{1}{2} \frac{\epsilon_{ox} S}{t_{ox}^2} V_{pu}^2 = kg \qquad V_{pu} = \sqrt{\frac{2kg}{\epsilon_{ox} S}} t_{ox}$$



 $C = \frac{\epsilon_{ox}S}{t_{or}}$ 

Force between plates:  $F = \frac{1}{2} \frac{\epsilon_{ox} S}{t_{ex}^2} V^2$ 



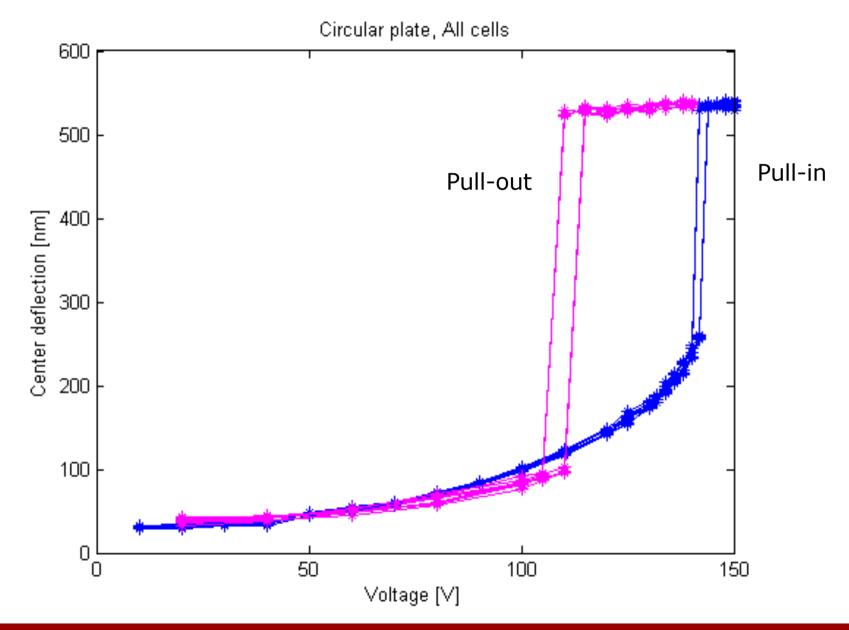


### Hysteresis



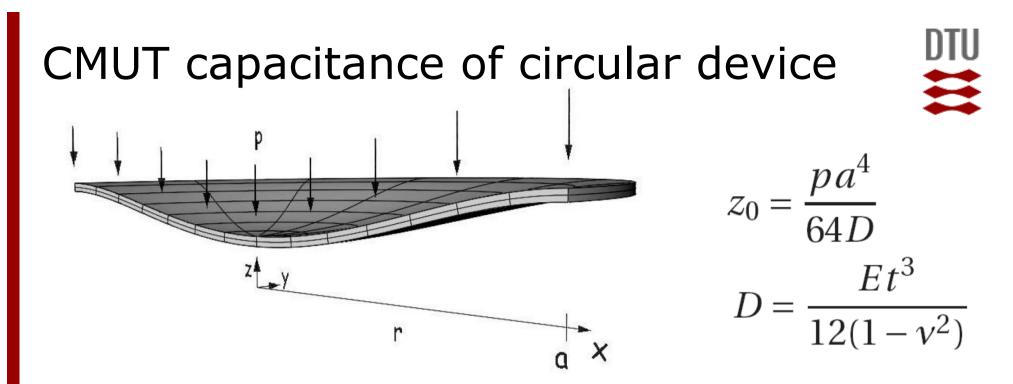
## Measured hysteresis







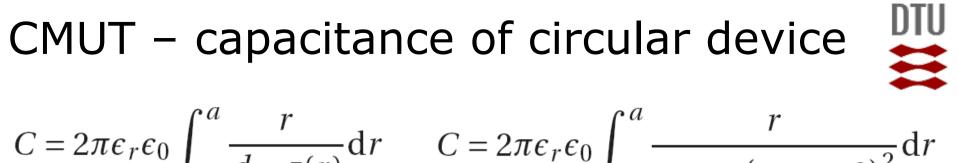
# The CMUT is not a parallel plate capacitor – what do we do?



Deflection comes from structural mechanics

$$z(r) = z_0 \left( 1 - \left(\frac{r}{a}\right)^2 \right)^2 = \frac{p}{64D} (a^2 - r^2)^2$$

$$C = \epsilon_r \epsilon_0 \int_0^{2\pi} \int_0^a \frac{r}{d - z(r,\theta)} \mathrm{d}r \mathrm{d}\theta$$

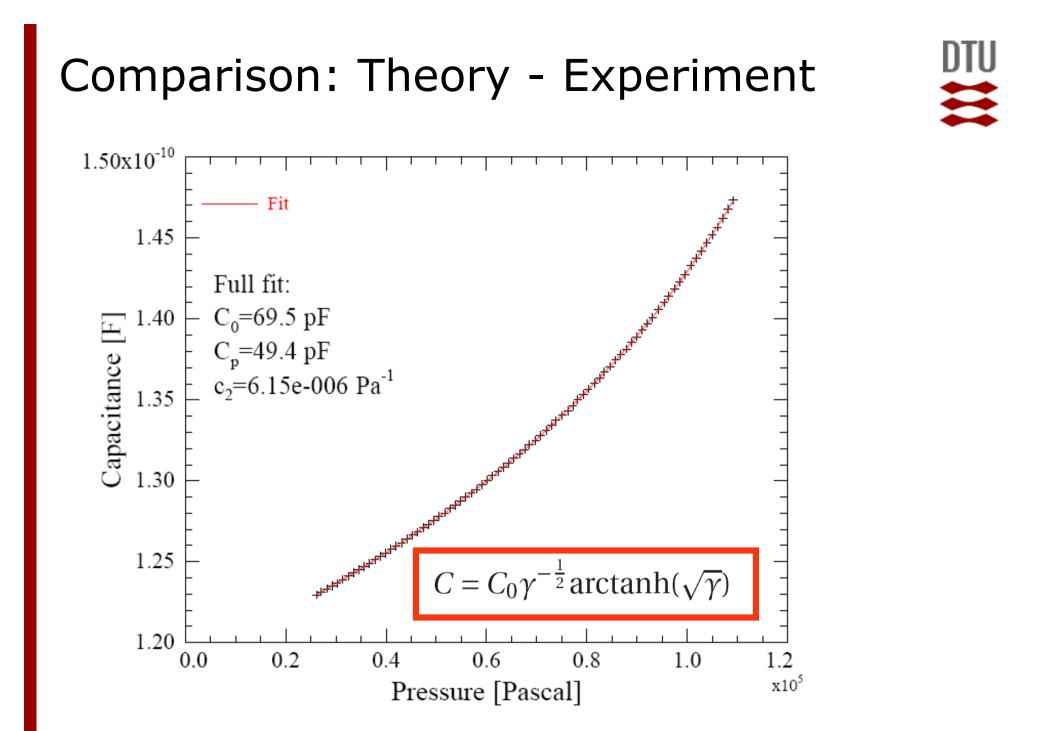


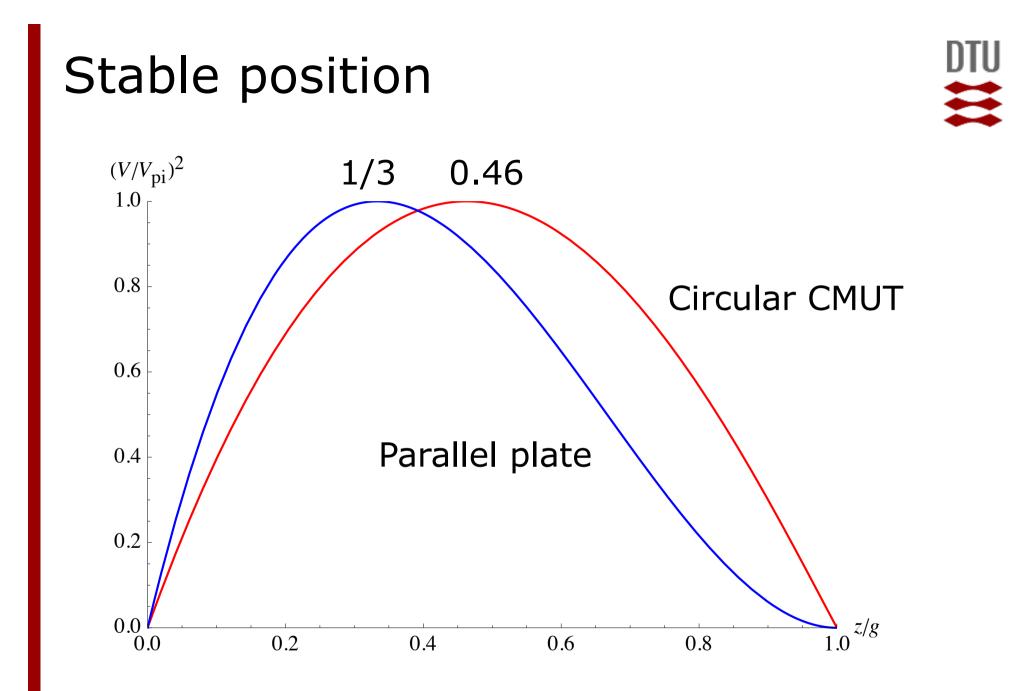
$$C = 2\pi\epsilon_r\epsilon_0 \int_0^{\infty} \frac{r}{d-z(r)} dr \qquad C = 2\pi\epsilon_r\epsilon_0 \int_0^{\infty} \frac{r}{d-z_0 \left(1-\left(\frac{r}{a}\right)^2\right)^2} dr$$

$$\gamma = \frac{z_0}{d}$$
  $x = \sqrt{\gamma} \left(1 - \left(\frac{r}{a}\right)^2\right)^2$ 

$$C = \epsilon_r \epsilon_0 \frac{\pi a^2}{d} \gamma^{-\frac{1}{2}} \int_0^{\sqrt{\gamma}} \frac{1}{1 - x^2} \mathrm{d}x$$

$$C = C_0 \gamma^{-\frac{1}{2}} \operatorname{arctanh}(\sqrt{\gamma})$$





Pull-in parameters



For the circular plate:

### Pull-in distance:

$$x = \frac{w_0}{g} = 0.463\,26$$

Pull-in voltage:

$$V_{\rm pi} = \sqrt{\frac{2.373g^3h^3Y}{a^4(1-\nu^2)\epsilon}}$$

- g = gap
- h = plate thickness
- a = radius
- Y = Young's modulus, ~148 GPa
- $\nu$  = Poisson's ratio, ~ 0.17
- $\varepsilon$  = Vacuum permittivity

## Spring softning

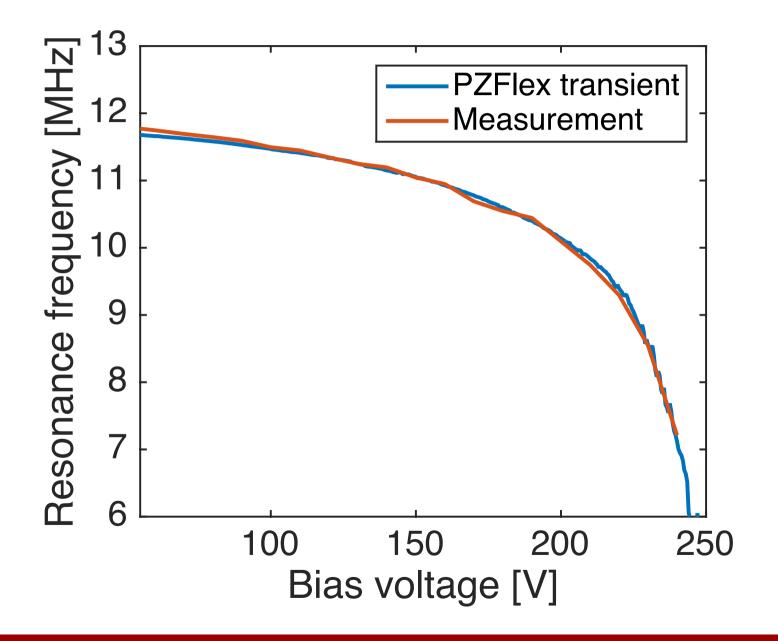


Spring constant decreases with voltage!

$$k_{\text{eff}} = -\frac{\partial F}{\partial z} = -\frac{\partial}{\partial z} \left( -\frac{\partial U}{\partial z} \right) = \frac{\partial^2 U}{\partial z^2}$$
$$= -\frac{\partial}{\partial z} \left( \frac{1}{2} \frac{\epsilon S}{(g-z)^2} V^2 - kz \right)$$
$$= -\frac{\partial}{\partial z} \left( \frac{1}{2} \frac{\epsilon S}{(g-z)^2} V^2 \right) - \frac{\partial}{\partial z} (-kz)$$
$$= k - \frac{\epsilon S}{(g-z)^3} V^2$$

## Spring softning: Measured





## Mini conclusion



- Capacitive sensors have high sensitivity!
- Can be used for actuation & sensing
- Pull-in <> pull-out
- Hysteresis



## **CMUT DESIGN**

From specifications to design parameters



### **Probe requirements – one example**

### **Medical imaging:**

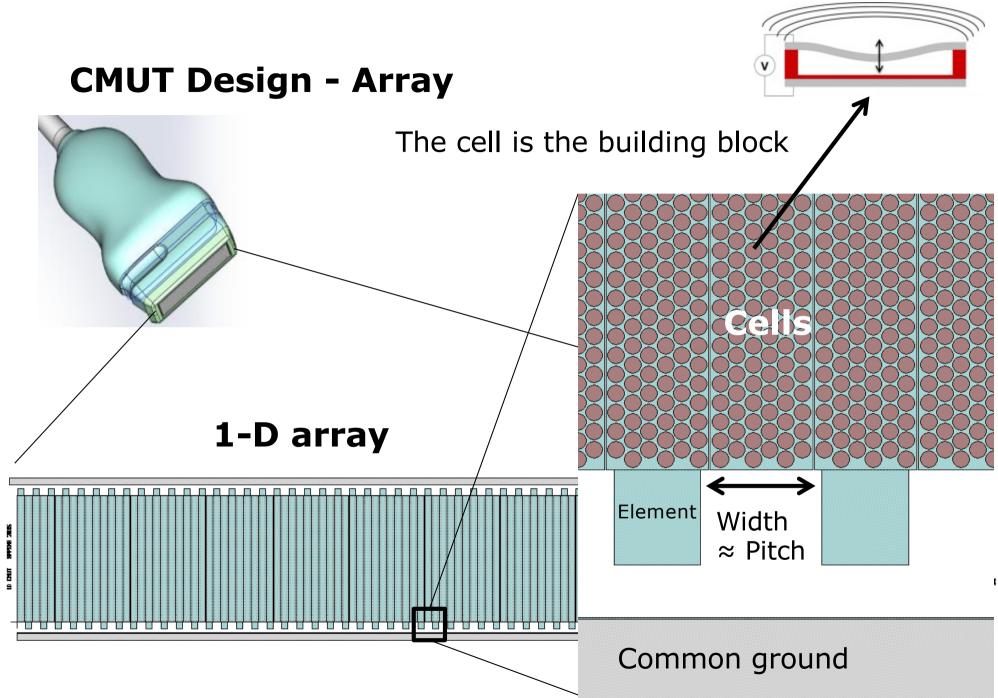
- 128-element linear array
- 5 MHz center frequency
- λ-pitch

#### Assembly and electronics:

- Compatible with commercial BK ultrasound scanner
- Up to 190 V DC bias is available
- Up to +/- 75 V AC transmit voltage

All CMUT designs begin with a set of specifications





# **CMUT design questions**



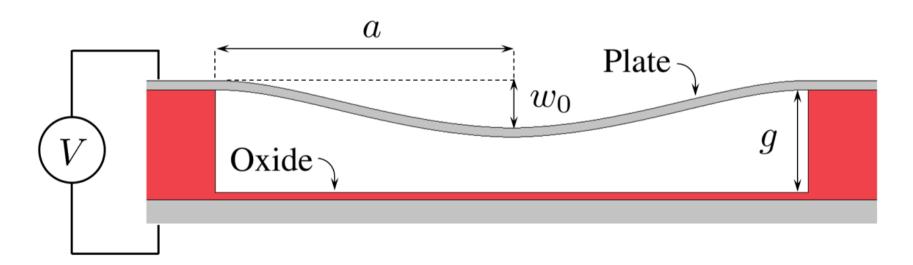
The CMUT designer must choose dimensions and fabrication technology.

#### Given:

- Array type (linear, row-column, ...)
- Center frequency in water,  $f_{water}$
- Pitch ( $\lambda$  or  $\lambda/2$  or ...), p
- DC and AC voltages

One must find:

- How to layout the cells
- Plate radius, a
- Plate thickness, *h*
- Vacuum gap, g



# DTU

# **Basic CMUT cell design equations**

Circular plate vacuum resonant frequency:

$$f_r = \frac{10.2158}{2\pi} \sqrt{\frac{h^2 Y}{12(a^4(1-\nu^2)\rho)}}$$

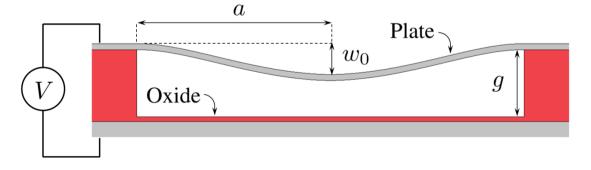
Circular plate resonant frequency in water: (Lamb 1920)

$$\frac{f_{\text{water}}}{f_r} = \frac{1}{\sqrt{\frac{a}{h} \frac{\rho_{\text{water}}}{\rho_{\text{plate}}} \Gamma + 1}}$$

Ratio is around ½, i.e., the resonant frequency is water is half that in vacuum

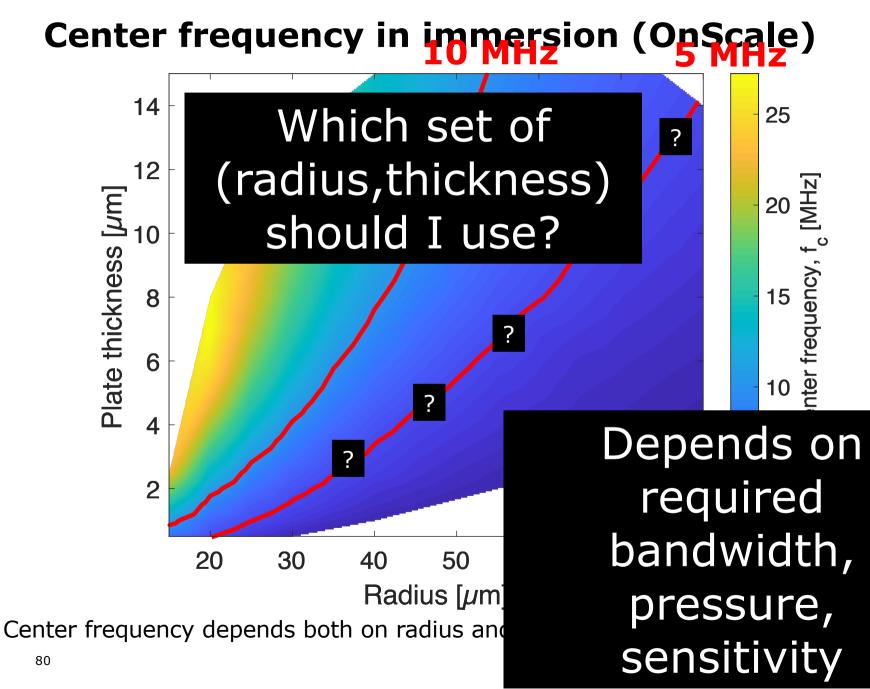
Circular plate pull-in voltage:

$$V_{\rm pi} = \sqrt{\frac{2.373g^3h^3Y}{a^4(1-\nu^2)\epsilon}}$$



- g = gap
- h =plate thickness
- a = radius
- Y = Young's modulus, ~148 GPa
- $\nu$  = Poisson's ratio, ~ 0.17
- $\rho$  = Plate density, ~ 2.33 g/cm<sup>3</sup>
- $\varepsilon$  = Vacuum permittivity
- $\Gamma = 0.6689$

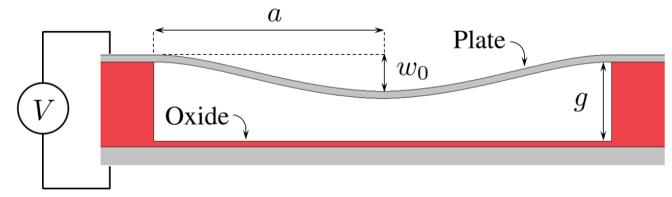




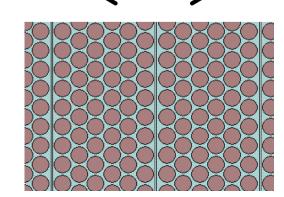
# **Basic CMUT design methodology**



- 1) Calculate pitch ( $\lambda$  or  $\lambda/2$  or ...) from wavelength in the media
- 2) Calculate element width (kerf almost zero or even negative)
- 3) Choose 2D cell layout (cell pitch, circles, squares, hexagonal ...)
- 4) Fit circles into the element and determine radius, a
- 5) Find the plate thickness, *h*, to match immersion frequency
- 6) Select pull-in voltage  $\approx 1.25 \times V_{DC}$
- 7) Adjust gap, g, to reach pull-in voltage
- 8) Check performance (bandwidth, pressure, PE sensitivity)
- 9) Check for substrate ringing and array effects ("Bragg" frequency)
- 10) If (performance < specs) goto 3
- 11) Check design with a full Finite Element model



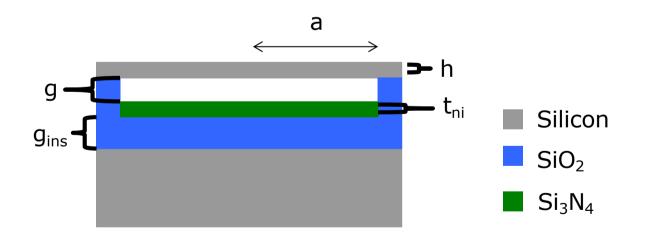




# **CMUT Design Example - Dimensions**



- Available plate thickness,  $h = 2.2 + 0.5 \mu m$  Circular plate size,  $a = 24.3 \mu m$
- Center frequency = 5 MHz
- Desired pull-in voltage = 240 V Insulating oxide thickness,  $g_{ins} = 380$  nm Nitride layer,  $t_{ni} = 50$  nm



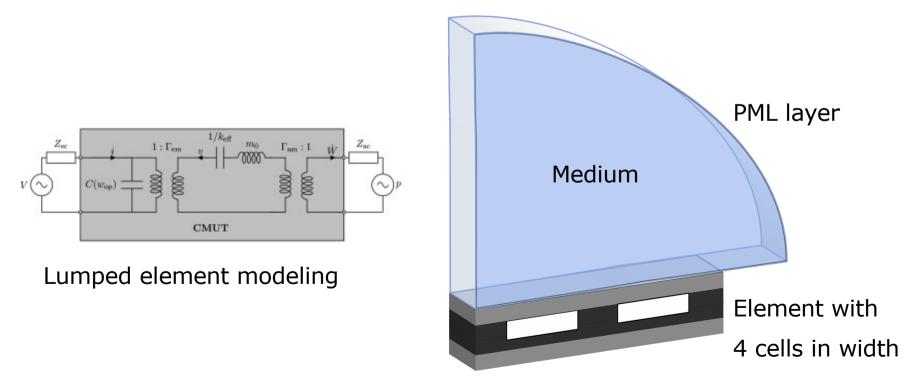
# Complication:

# Cells interact!

(Array effects)

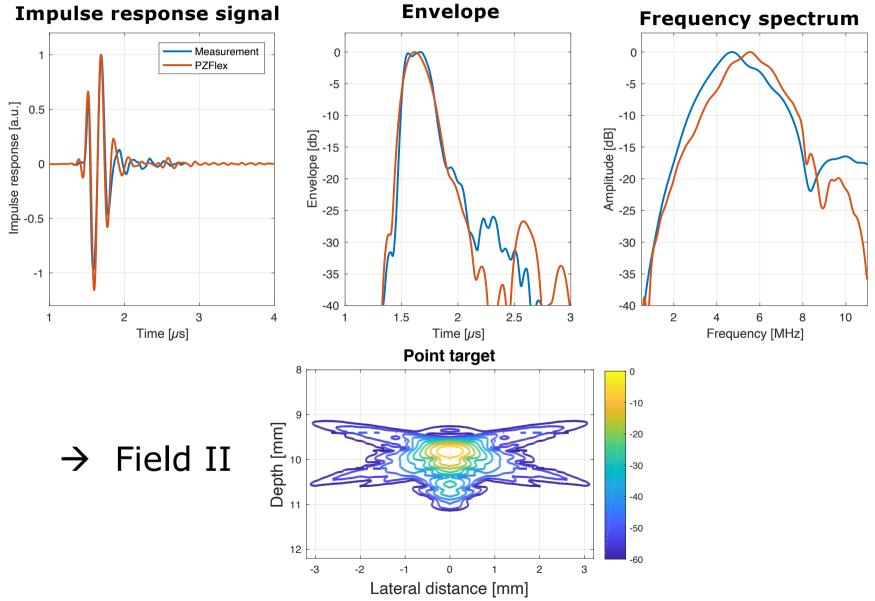


FEM simulations – PZFLEX/OnScale/COMSOL models
 Physics: Electrostatic, mechanical and acoustical
 Solvers: Frequency domain and transient
 Aim: Frequency spectrum and transient response



# Simulation & experiment fit well

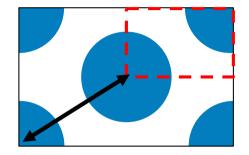




# **Optimization of a CMUT device**



- Model
  - Infinite array
  - Circular cells placed in a hexagonal grid
  - Simulating one unit cell



Cell pitch

- Results
  - Impulse response
    - Transmit
    - Receive
  - Sensitivity
  - Plate velocity at center
  - Pressure
  - Acoustic impedance

# Three cell and array effects

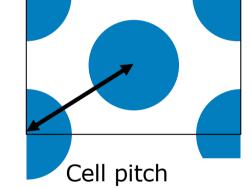
-0.5

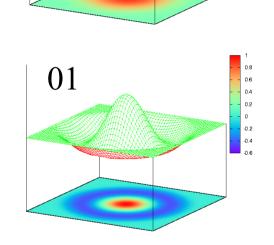
00

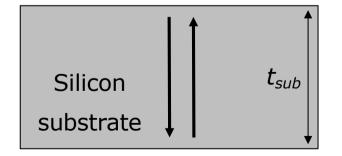


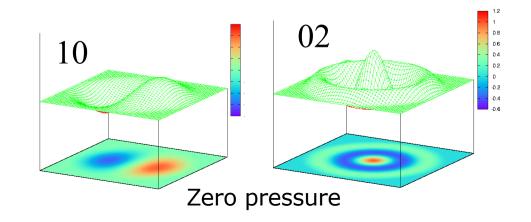
2) Mutual couplings: "Bragg frequency",  $f_b$ = (Speed of sound) / (cell pitch)

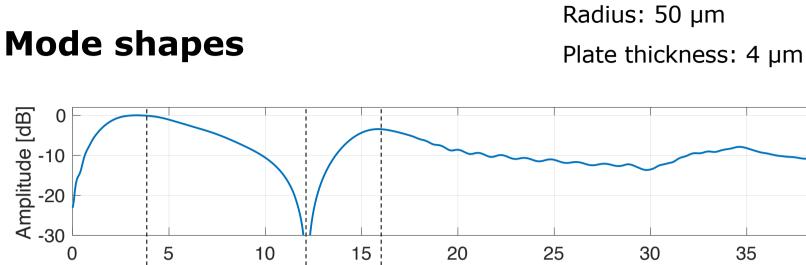
- 3) Substrate ringing
- $f_s$ = (Si Speed of sound) / (2  $t_{sub}$ )

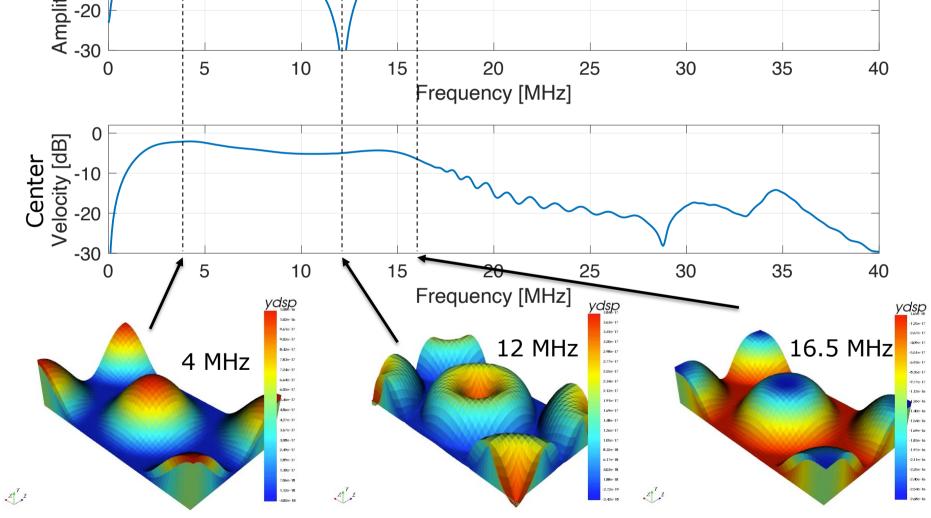






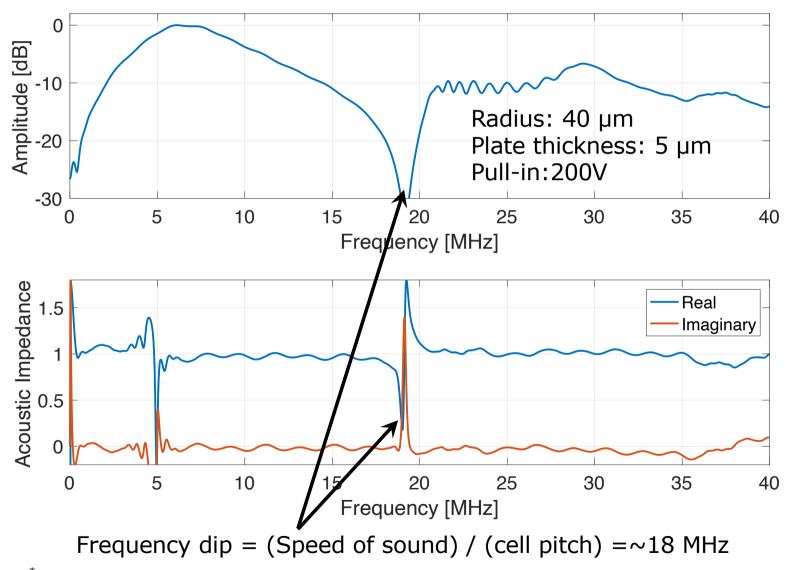


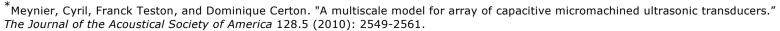






# **Output of One Transmit Simulation**





# **Parametric Sweep**

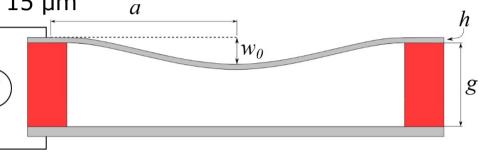
#### **Parameters**

- Plate thickness between 0.5µm and 15 µm
- Radius between 10  $\mu m$  and 80  $\mu m$
- Fixed pull-in voltage at 200 V
- Fixed distance between cells, 5 μm
- Constant electrode area, 1 cm<sup>2</sup>
- Both transmit and receive

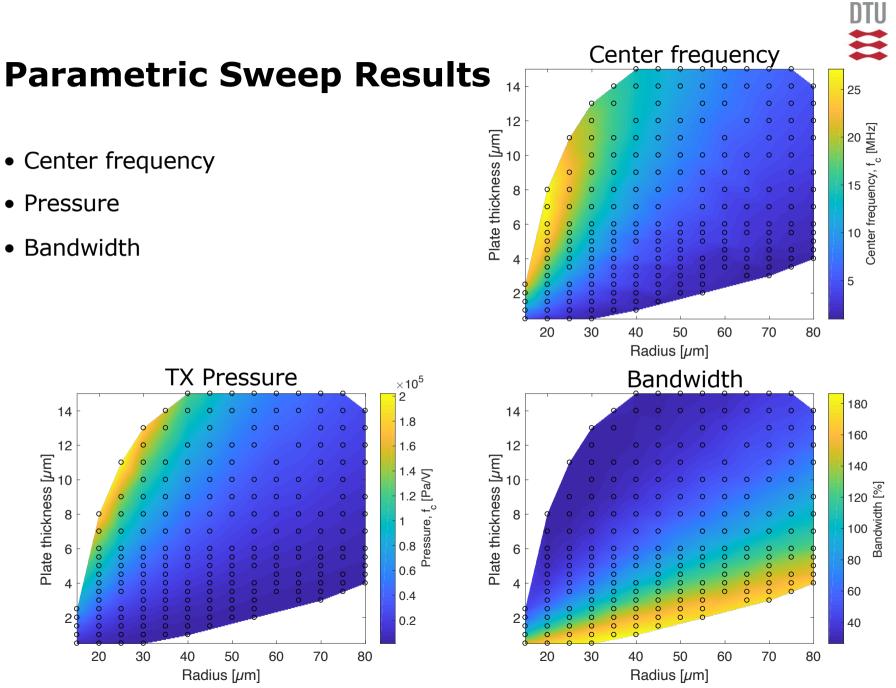
Total of 567 simulations

#### Simulation time

- Personal computer (8 cores, 64GB ram) : >1 week
- In the cloud: <2 hours (2 cores per simulation, parallel, ~600 core hours)





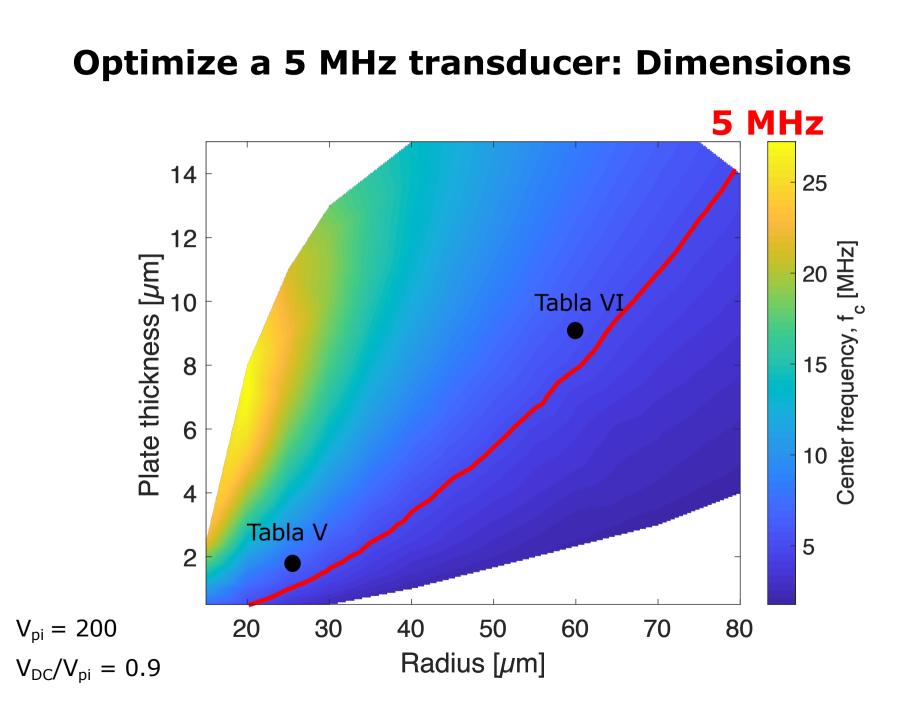


# Design of a 5 MHz transducer (like Tabla V & VI)



- Optimal parameters
- Trade-offs
- Evaluate
  - Sensitivity
  - Bandwidth
  - Frequency dip
- In
  - Transmit mode
  - Receive mode
  - Pulse-echo



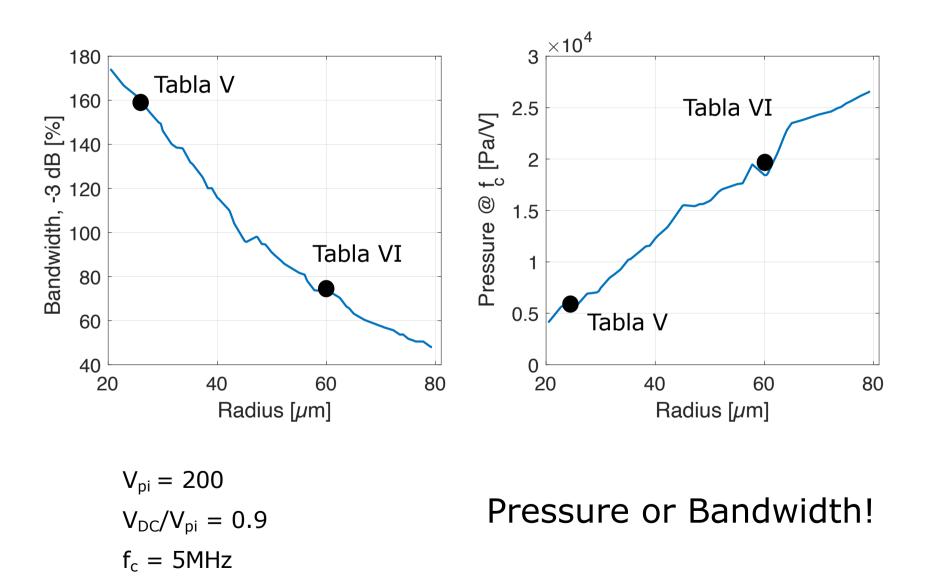


DTU

Ħ

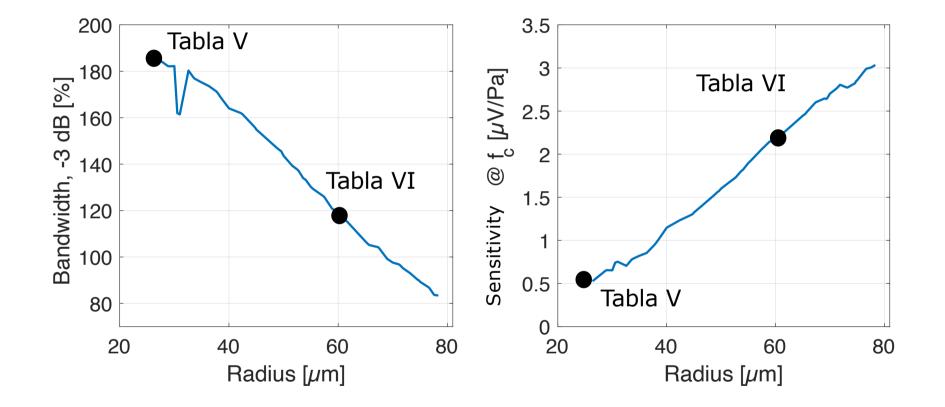


## **Transmit Mode**



## **Receive Mode**

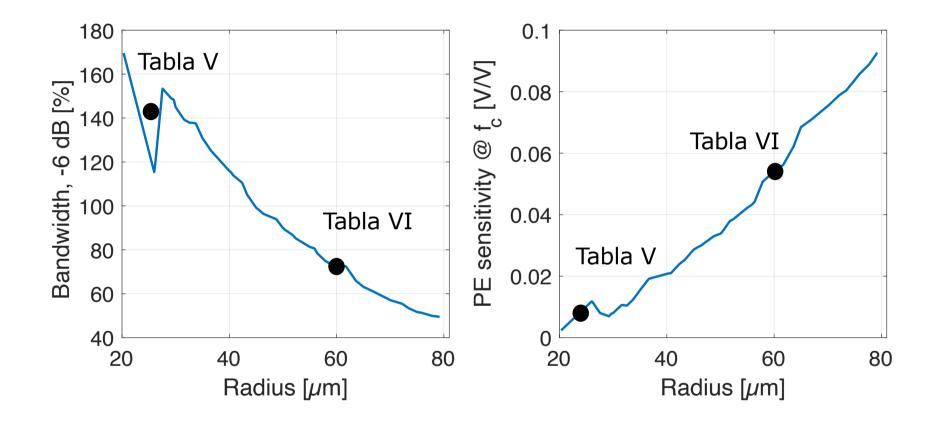




Sensitivity or Bandwidth!

### **Pulse-echo**



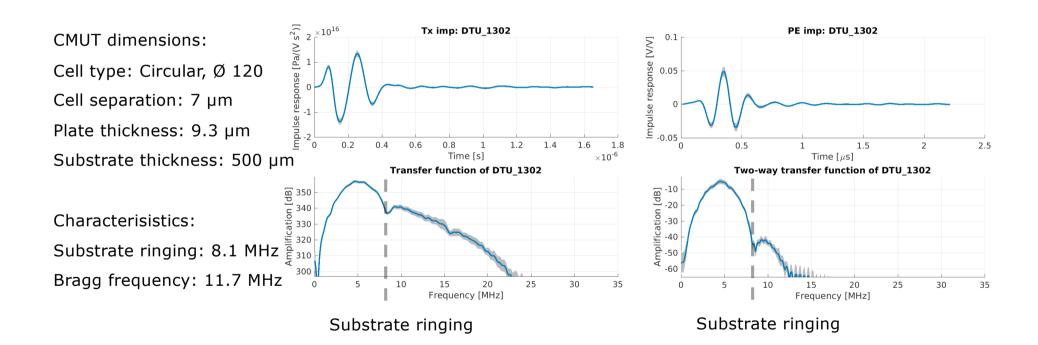


#### To summarize:

Pressure, sensitivity, and PE sensitivity can be improved at the expense of bandwidth

## Tabla VI





# **Sub - conclusion**



- High performance cloud computing and OnScale enables huge parametric FEA studies
- CMUT can be optimized with respect to output pressure and receive sensitivity, but at the expense of bandwidth.
- Mutual acoustic impedance effects are captured explaining dips in frequency spectra
  - can limit bandwidth and performance if not designed properly



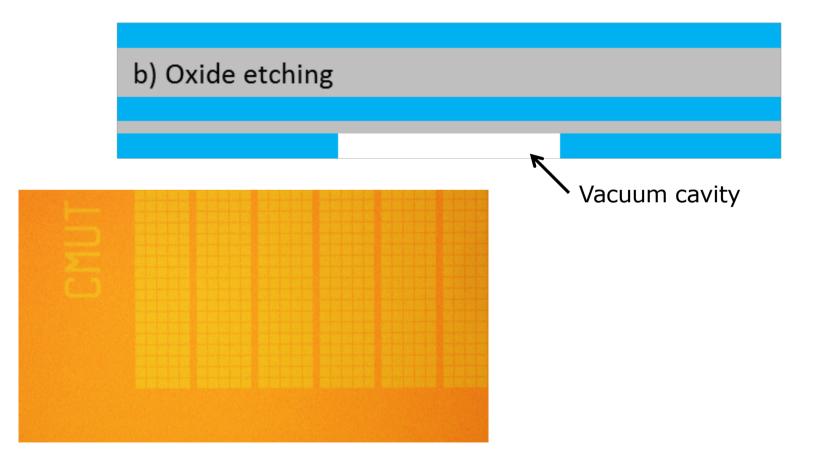
# **CMUT FABRICATION**











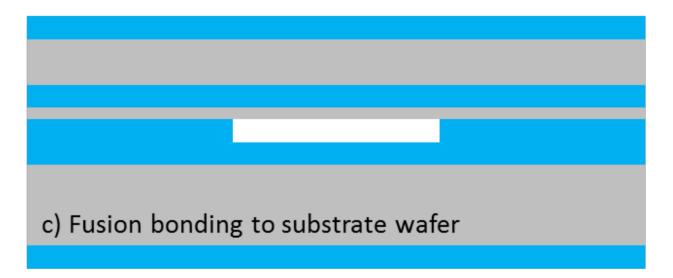




EVG 520HE at DTU: NIL & Fusion bonding

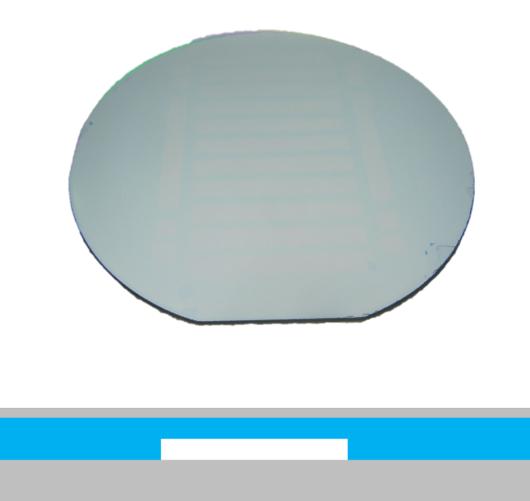
RCA cleaning before bonding

b) Oxide etching





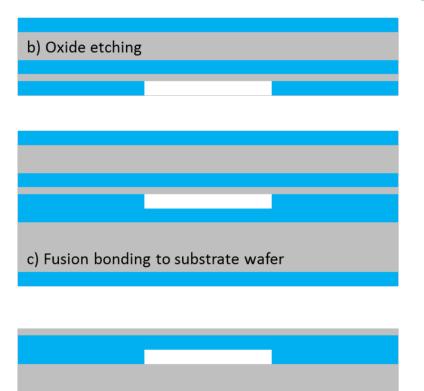
b) Oxide etching
c) Fusion bonding to substrate wafer



d) Etching handle and BOX layer



#### e) Opening bottom contacts



d) Etching handle and BOX layer



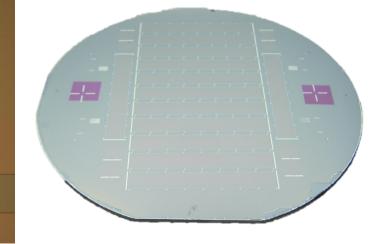
e) Opening bottom contacts

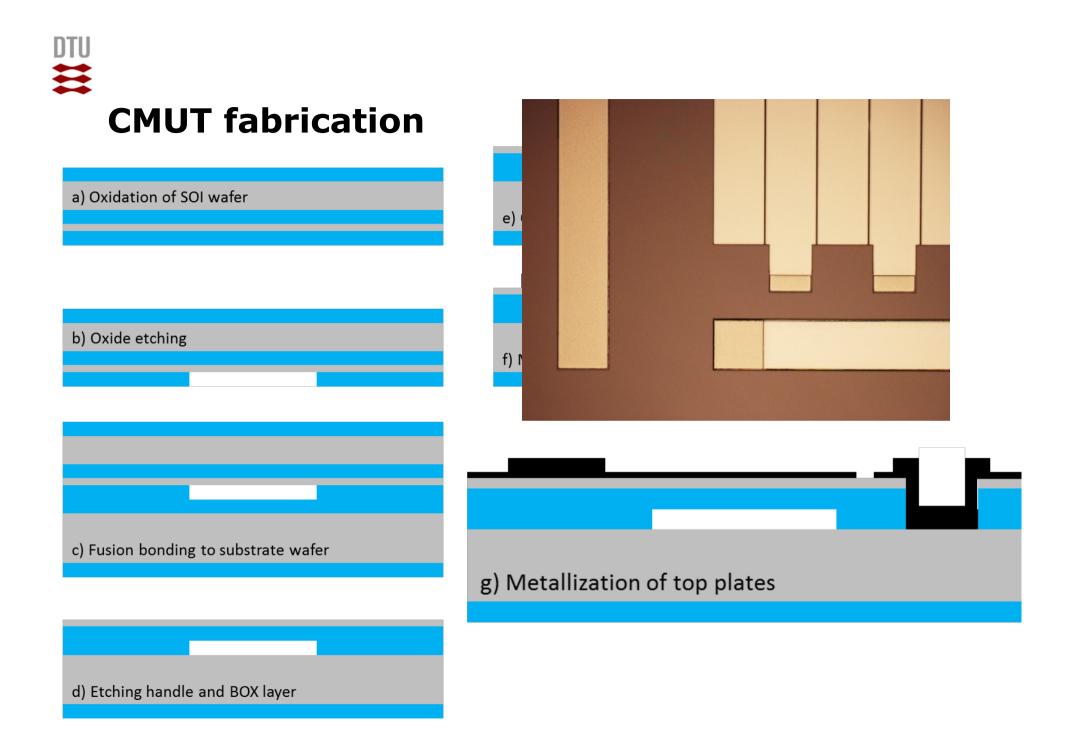
b) Oxide etching

f) Metallization for contact pads

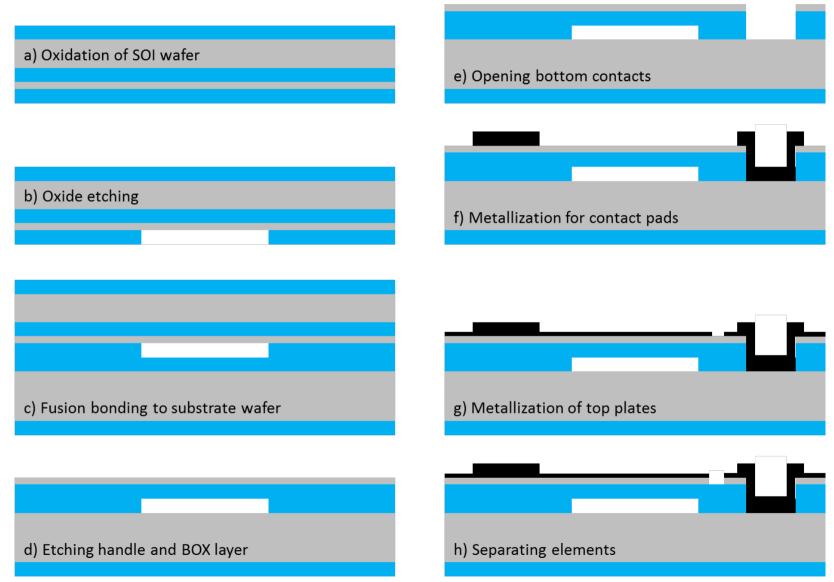
c) Fusion bonding to substrate wafer





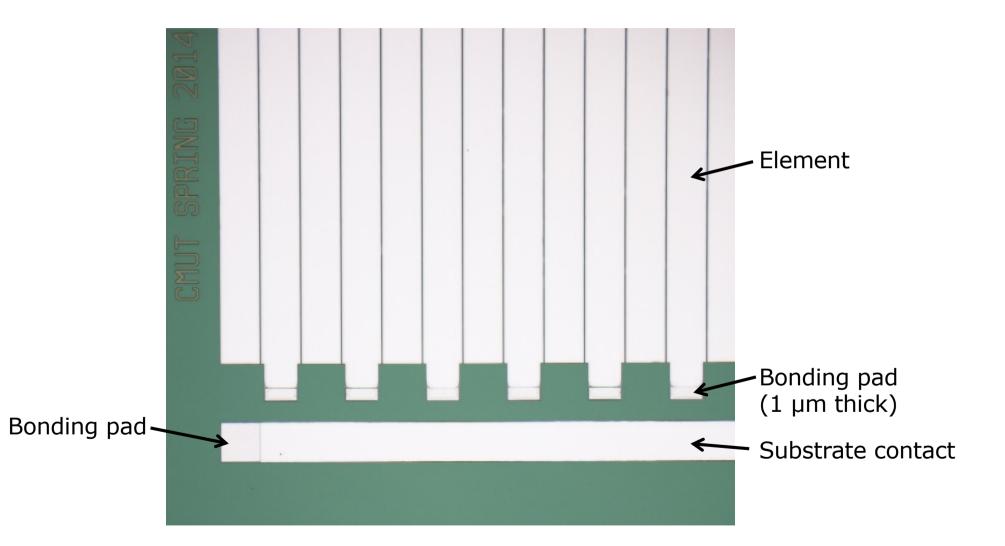






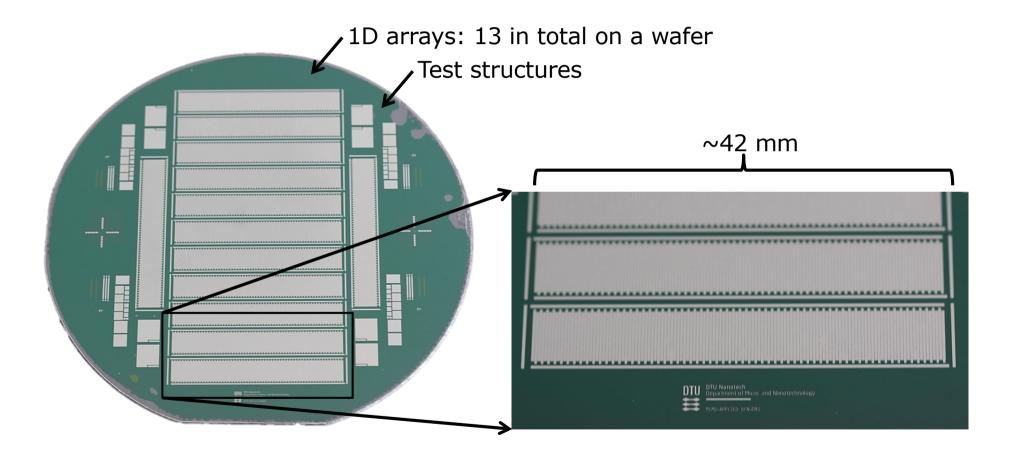


## **Finished array**





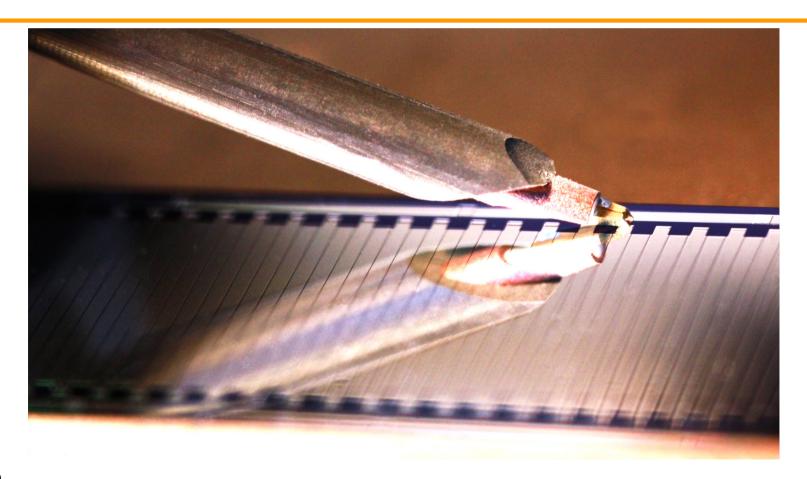
# More than 90% yield



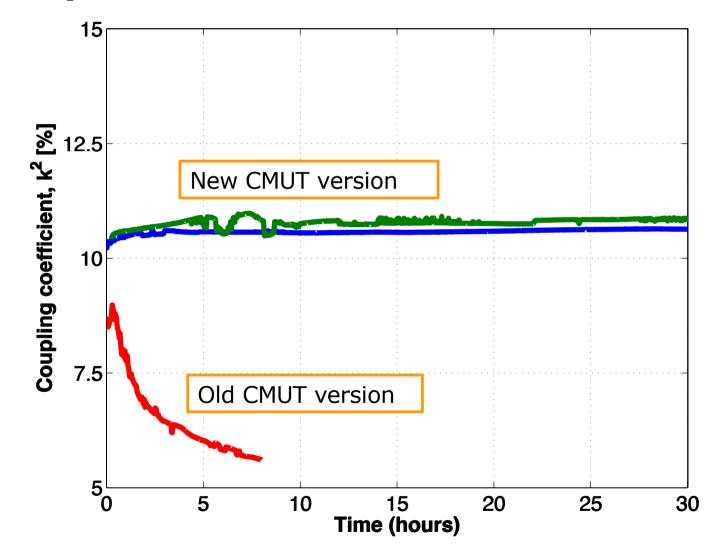


# Characterization

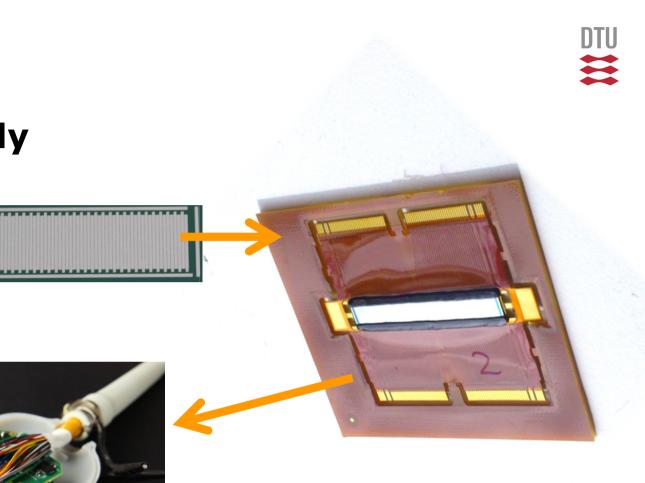
Impedance measurements in air to quantify the electromechanical coupling



# **Stability assesment**



120

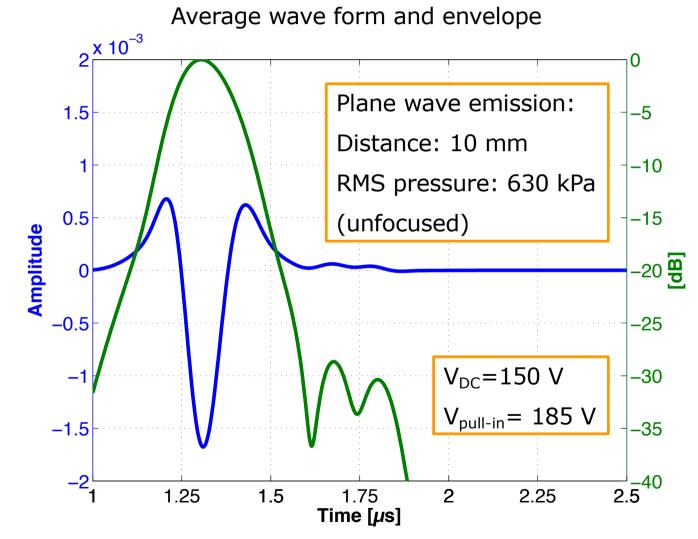


# **Probe assembly**



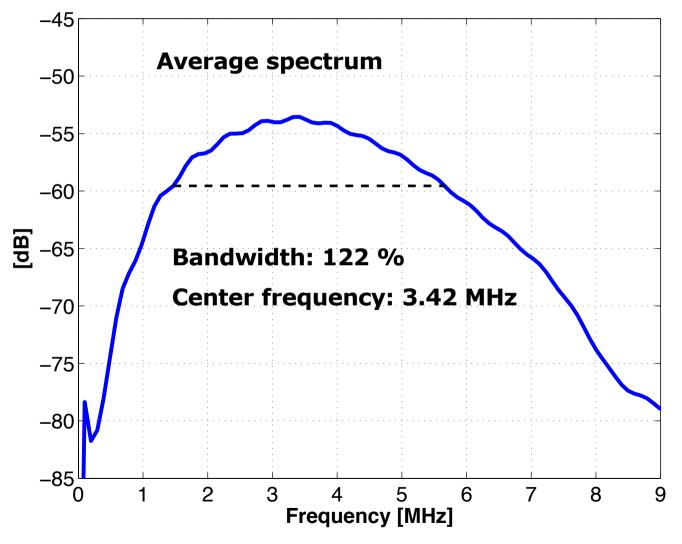


# Fully assembled probe – Pulse-echo





# Fully assembled probe - Pulse-echo sensitivity

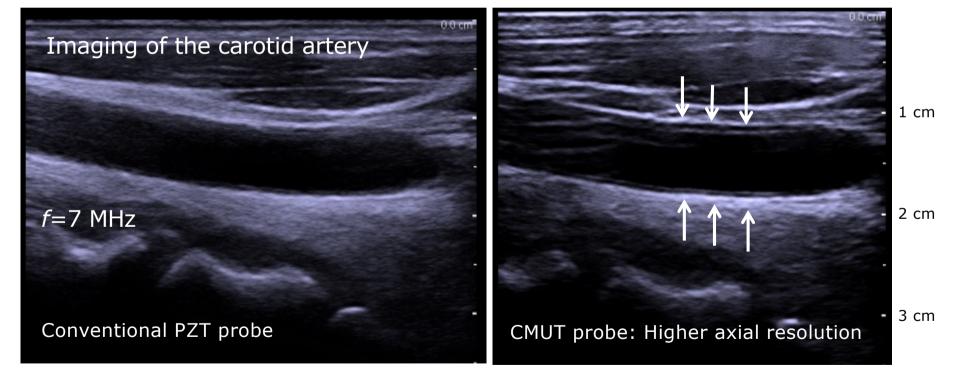


# **1-D TABLA probe**

- MEMS  $\rightarrow$  small mass •
- High bandwidth ٠
- High axial resolution ٠
- Improved image quality •







la Cour et al., IEEE Trans. Ultrason., Ferroelect., Freg. Control (62), 1563-1579, 2015; Lei et al. Proc. IEEE IUS 2015; Christiansen et al., ECS J. Solid State Sci. Technol. (3), 63-68, 2014; Christiansen et al., J. Acoust. Soc. Am. (135), 2523-2533; la Cour et al. Proc. IEEE IUS, 2584-2587, 2014; Lei et al. Proc. IEEE IUS, 2595-2598, 2014; Thomsen et al., Sensors and Actuators A (220), 347-364, 2014; Engholm et al. Proc. IEEE IUS, 2603 - 2606, 2014; la Cour et al. Proc. IEEE IUS, 2187-2190, 2013; Christiansen et al. Proc. IEEE IUS1737-1740, 2013; ; la Cour et al. Proc. IEEE IUS, 588-591, 2012

# Conclusion

- PZT technology dominates the transducer market
- CMUT is an emerging technology
  - Compatibility with silicon fabrication
  - Excellent dimensional control (≈1 µm)
  - No need for impedance matching layers
  - Large bandwidth (>100%)
  - Low price if many are made
  - Lead free
- All major players investigate CMUT technology

CMUT's could change the game – when full potential is realized



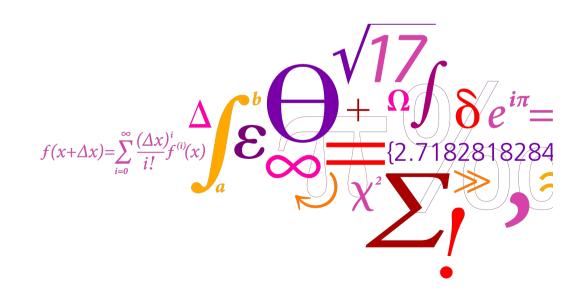
# Thank you for your attention!

Time for problem solving



# **Problems**

Design of PZT and CMUT transducers



# **Design of PZT thickness mode transducers**

We investigate the design of PZT transducers. The transducer has 128 elements, and it has a pitch of  $\lambda/2$ . The dicing saw has a blade width of 20  $\mu$ m.

Find the:

- thickness of the PZT
- pitch
- element width
- fill factor

for the following center frequencies:

- 3 MHz
- 8 MHz
- 15 MHz

# **Design of CMUTs**

We now investigate the design of CMUTs. The transducer has 128 elements, and it has a pitch of  $\lambda/2$ . The transducers operates at a DC voltage of 200 V.

We will do our calculations for the following center frequencies:

- 3 MHz
- 8 MHz
- 15 MHz

Follow the CMUT design guidelines (see next page) and calculate the parameters mentioned in the guidelines.

# **Basic CMUT design methodology**



- 1) Calculate pitch ( $\lambda$  or  $\lambda/2$  or ...) from wavelength in the media
- 2) Calculate element width (kerf almost zero or even negative)
- 3) Choose 2D cell layout (cell pitch, circles, squares, hexagonal ...)
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- 5) Find the plate thickness, *h*, to match immersion frequency
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