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Advanced Ultrasound Imaging 2023 Synthetic Aperture Velocity Imaging

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$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

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Department of Health Technology

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Outline

- Limitations of current ultrasound system
- Potentials and problems of synthetic aperture flow imaging
- Solving the problems with vector flow and motion
- Application in practice – pre-clinical test
- Can we make quantitative 2-D images for all image types?
 - Non-linear/linear
 - Vector Flow fast-slow
 - Super resolution imaging
- Quantification and slow flow possibilities
- What about 3-D Tensor Velocity Imaging?

0.0 cm

Pulsating rotational flow in the Aorta

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Frame Rate problem: Limited Dynamic Range in VFI and CFM

$V_{max} = 152.8 \text{ cm/s}$

$V_{max} = 55.1 \text{ cm/s}$

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Limitations of current ultrasound systems

- Only one transmit focus
- Frame rate is limited especially for blood flow and 3D imaging

$$f_r = \frac{c}{2DN_d N_l} = \frac{1540}{2 \cdot 0.15 \cdot 100 \cdot 8} = 6 \text{ Hz}$$

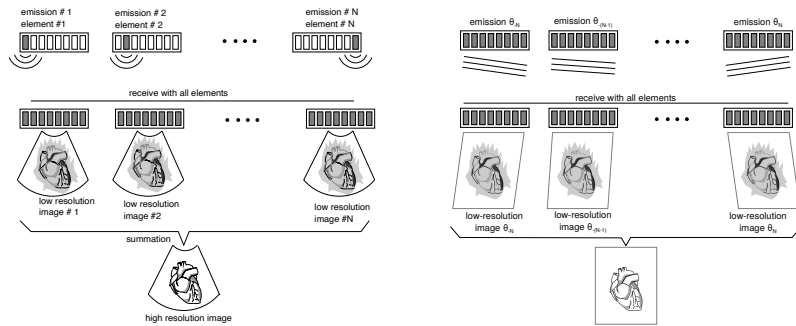
- Velocity estimation is poor due to few data samples
- Impossible to see perfusion
- Images are diffraction limited
- 3-D data rates are a major problem

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Synthetic Aperture and UltraFast Imaging



- Whole imaging region insonified
- Low resolution images (LRI) focused for every emission
- All LRIs combined to High Resolution Image (HRI)
- Dynamic focusing in both transmit and receive everywhere

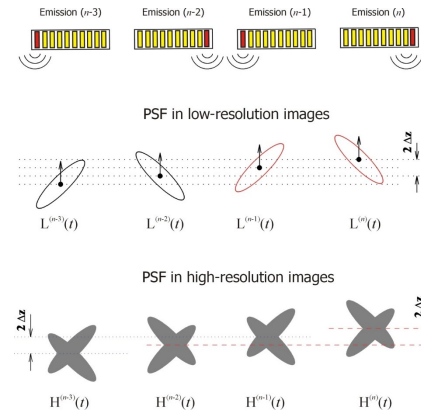
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Synthetic Aperture Flow Imaging



- $HRI(1) = LRI(1)+LRI(2)$ equal to $HRI(3) = LRI(3)+LRI(4)$ apart from displacement
- Correlation can yield displacement and, thus, velocity
- Continuous data everywhere
- Ideal for low velocity flow
- Contrast depends on length N of sequence
- Maximum detectable velocity given by:

$$v_{\max} \approx \frac{\lambda / 4}{NT_{prf}} = \frac{cf_{prf}}{4Nf_0}$$

Nikolov & Jensen: IEEE UFFC, 2003, 50(7), pp. 848-856

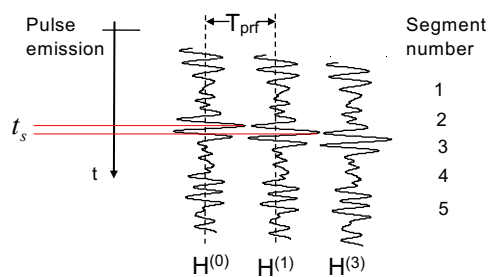
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Cross-correlation Velocity Estimator



1. Cross-correlate segments from two consecutive high-resolution images
2. Find offset t_s of maximum in cross-correlation function.

$$t_s = \frac{2|\vec{v}| \cos \Theta}{c} T_{prf}$$

The estimated axial velocity V_n is:

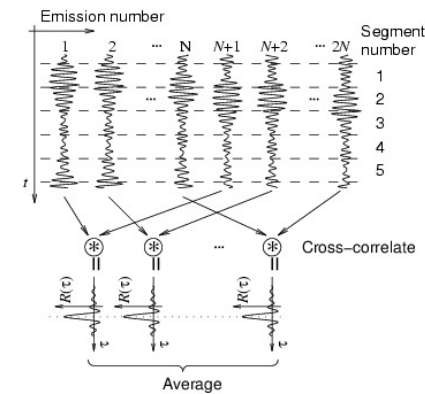
$$\hat{v}_n = \frac{ct_s}{2T_{prf}}$$

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Recursive Cross-correlation

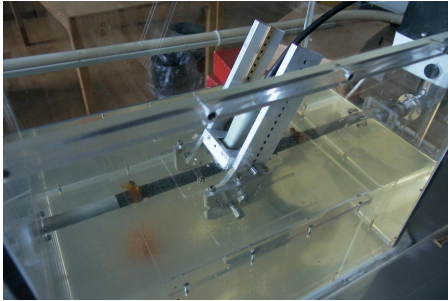


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Flow Measured in Flow Rig

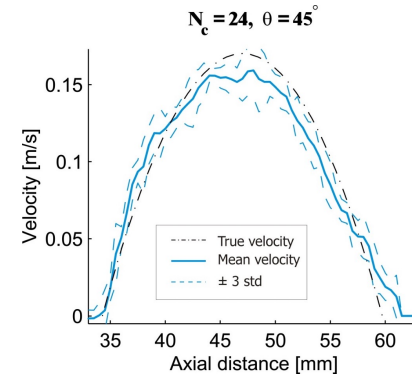


- Re-circulating flow rig
- 64 elements, 7 MHz linear array transducer
- 45 degrees flow angle
- 4 emission centers using 11 elements and 20 μ s chirp
- 6 x 4 emissions used in estimates



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First SA Velocity Image from Flow Rig



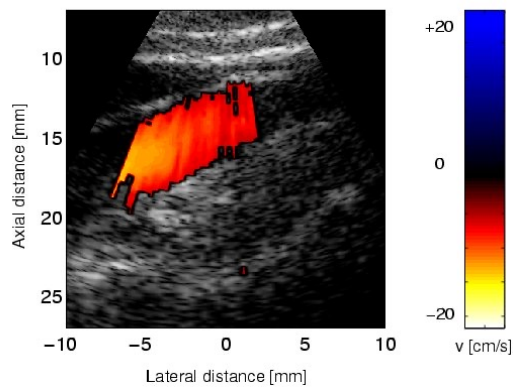
- Parabolic velocity profile
- Standard deviation relative to maximum: 3%
- 4 LRI for one HRI
- 6 HRIs/estimate
- 6,000 images/s at $f_{prf} = 25$ kHz

Nikolov & Jensen: IEEE UFFC, 2003, 50(7), pp. 848-856 and IUS 2001

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In-vivo SA Flow Image

In-vivo measurement – carotis



24 emissions used
500 used in traditional systems
-> **20 times faster**

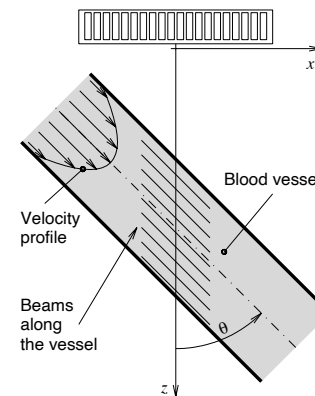
More than
200 images/sec to 15 cm depth

900 images/sec at 4 cm



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Directional beamforming



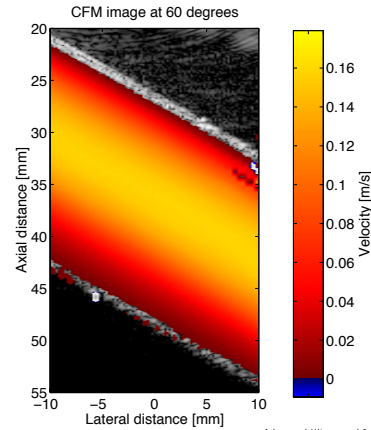
- Beamform along flow direction
- Cross-correlation to find velocity magnitude
- Minimizes de-correlation from velocity gradient
- Yields very precise estimates
- Possible to estimate high velocities

Jensen and Nikolov, IEEE UFFC, 2004, 51(9), pp. 1107-1118

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Directional SA Flow Imaging

- Full image acquired in 128 emissions
- 60 independent images to a depth of 10 cm can be shown per second
- Relative standard deviation of 0.36 %
- Correct velocity magnitude can be followed everywhere simultaneously at all times



Jensen and Nikolov, IEEE UFFC, 2004, 51(9), pp. 1107-1118

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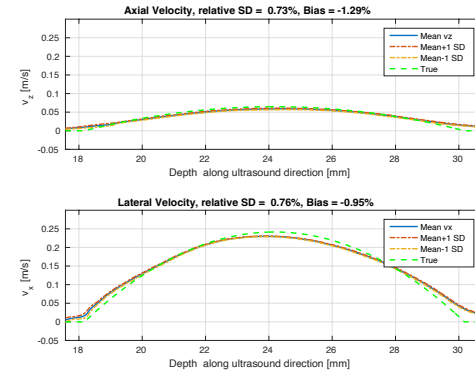
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Velocity profiles in flow rig at 75 degrees

Directional Transverse Oscillation, cross-correlation estimator



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Jensen: IEEE UFFC, 2019, 66(6), pp. 1024-1031 & 1032-1038

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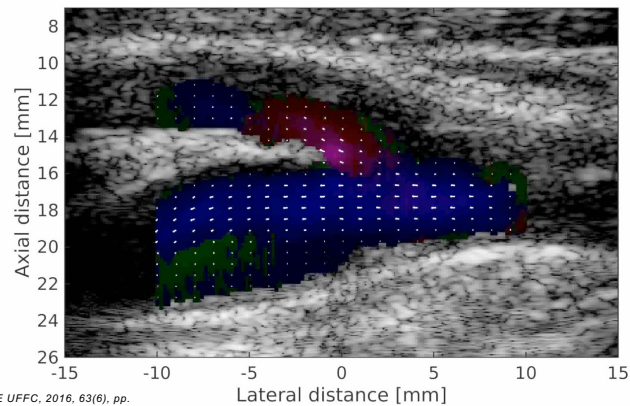
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- Measured data
- Fully quantified vector flow:
 - 0.76% SD
 - -1.29% bias
- Hundred to thousands of frames can be presented per second

SA Vector Flow Imaging in Carotid bifurcation

Frame Rate: 2000 Hz

Time = 2.5852 sec



Villagomez-Hoyos et al., IEEE UFFC, 2016, 63(6), pp. 842-853

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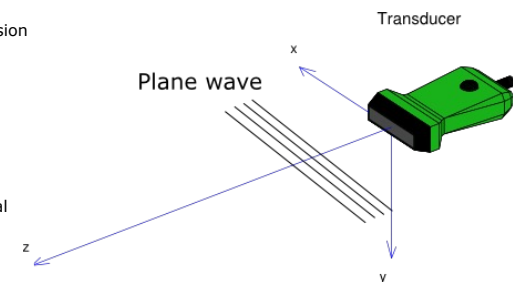
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Fast plane wave imaging

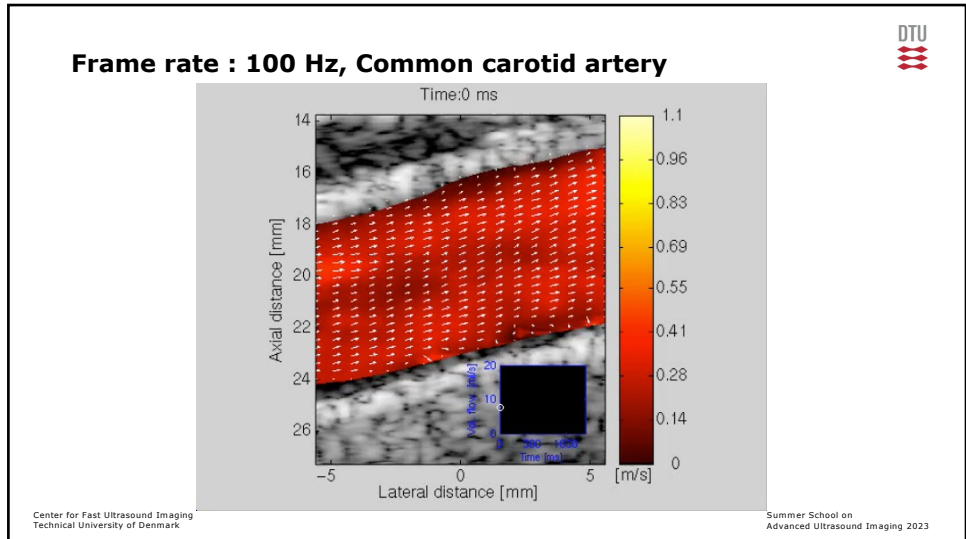
- Single plane wave emitted
- Full image reconstructed from single emission
- Very fast imaging can be attained with thousand of image per second
- Flow imaging with excellent temporal resolution
- Vector flow imaging possible
- Implemented on the RASMUS experimental scanner
- Frame rate of more than 100 Hz
- Speckle tracking used for velocity estimation



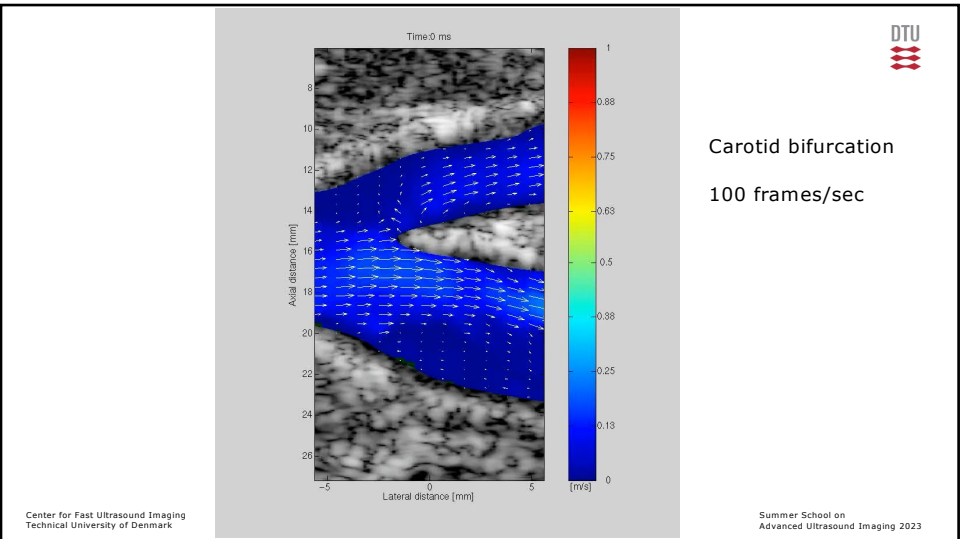
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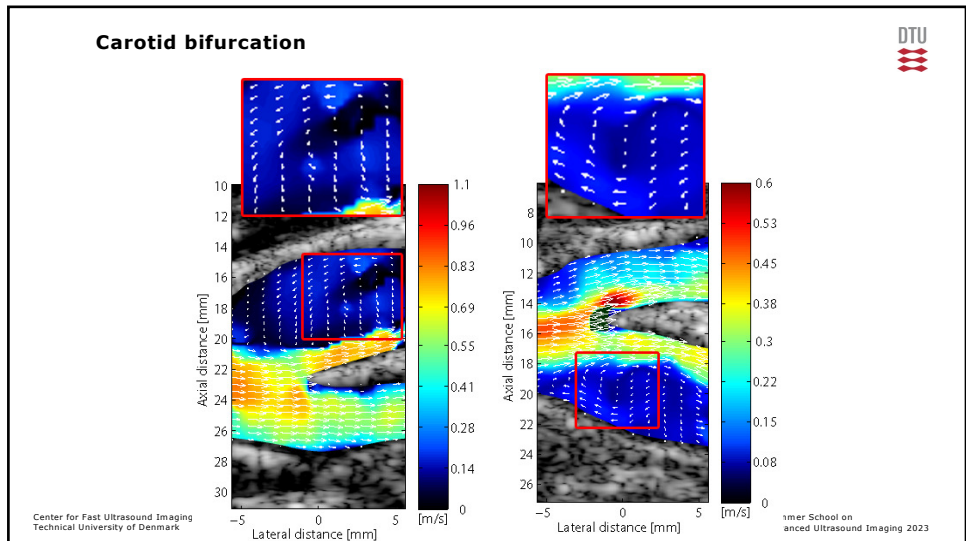
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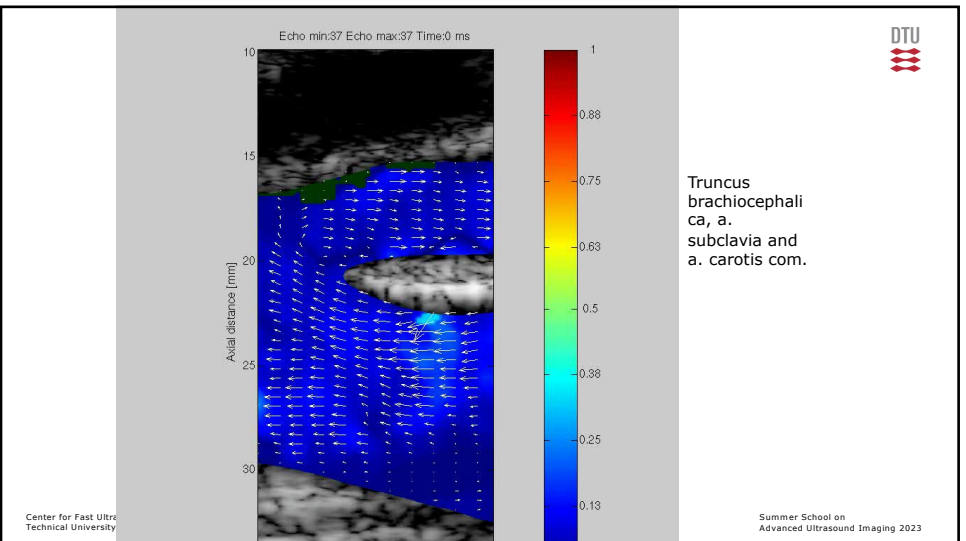
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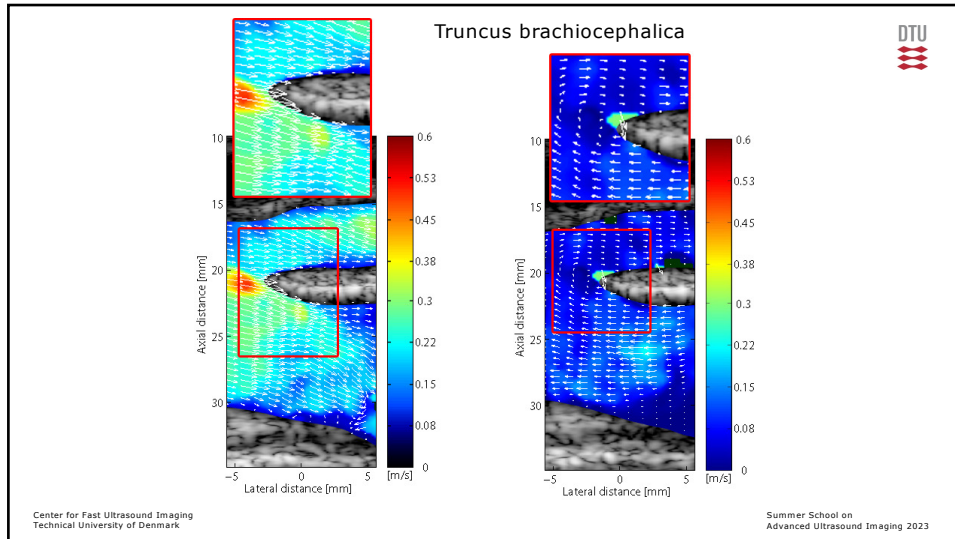
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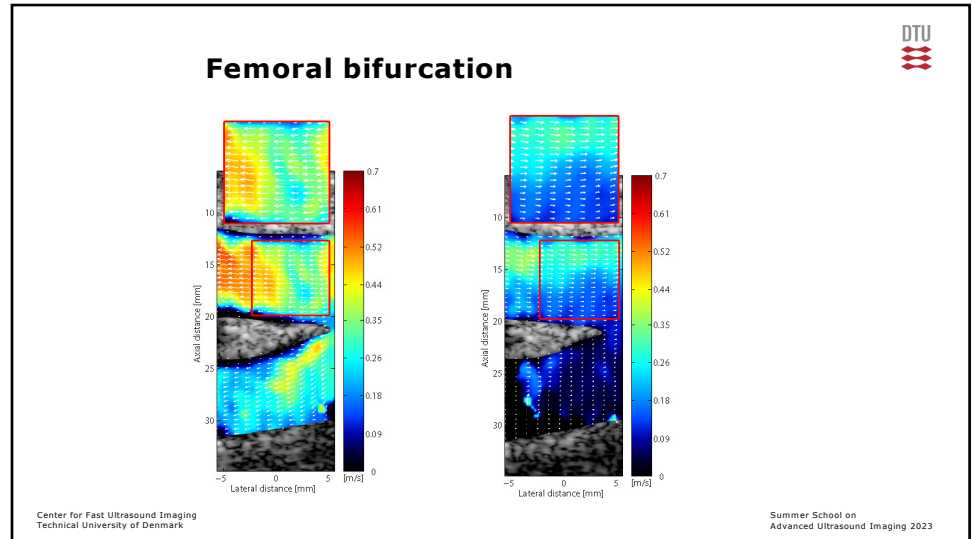
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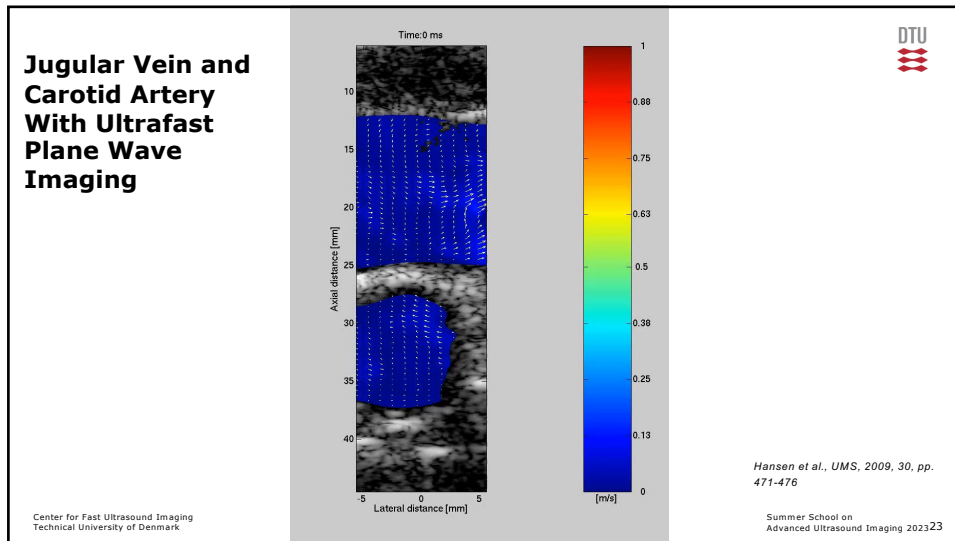
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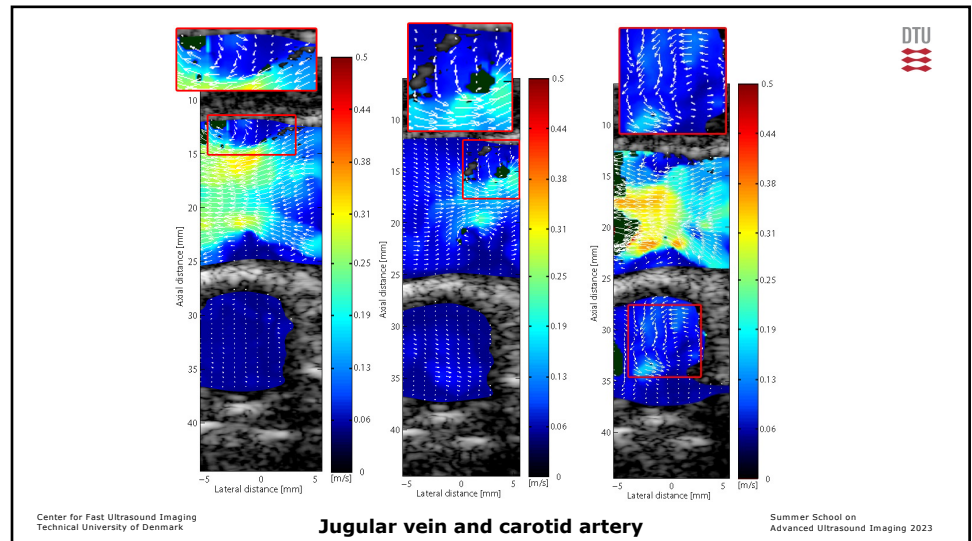
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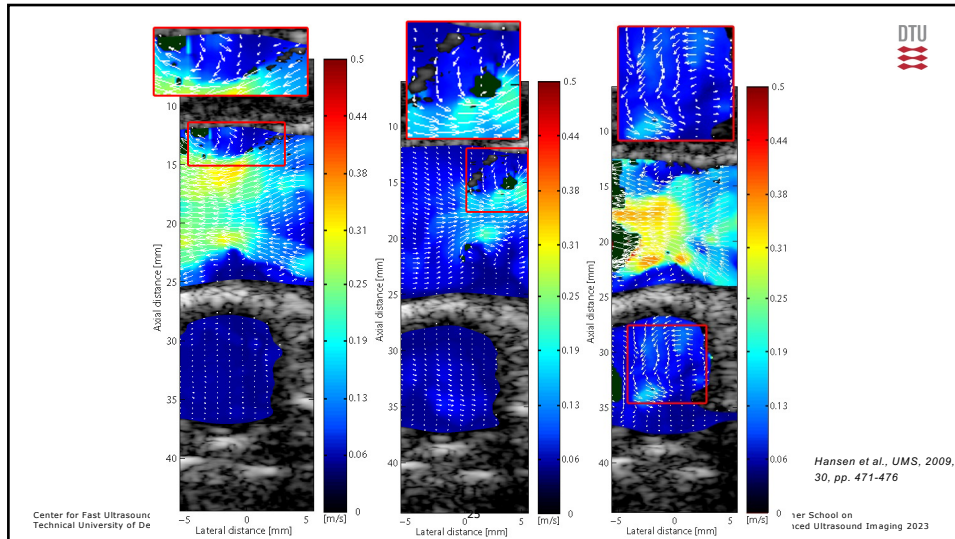
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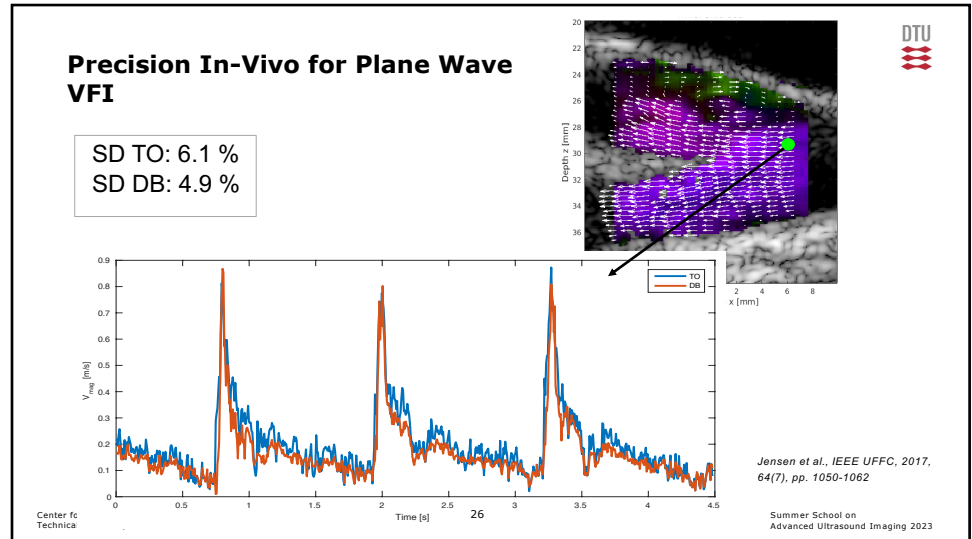
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Demands on Ideal Synthetic Aperture Sequence

- Can we design a single nearly optimal synthetic aperture (SA) acquisition sequences for all imaging modes?

- B-mode image
- Non-linear
- Tissue motion
- Power Doppler
- Color flow mapping
- Vector flow imaging
 - Fast flow
 - Slow flow
- Super resolution

- Would enable retrospective diagnostics involving all the above images

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Demands

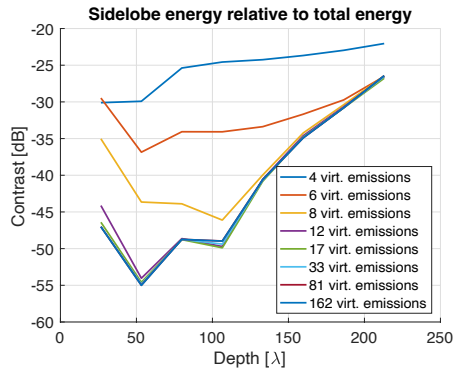
- B-mode
 - High resolution → Wide coverage of aperture
 - High contrast → Many receiving elements and many emissions
- Non-linear imaging
 - Isolation of non-linear component → Repeated emissions (PI or AM)
- Motion estimation
 - Correlation of frames → Repetition of high-resolution images
- Fast motion
 - Short distance between HRI → High f_{prf} and/or short sequences
- Slow flow
 - Long acquisition times → Continuous imaging

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B-mode Optimization



- Resolution:
 - Spread out virtual source as much as possible
 - Use all elements in receive
- Contrast
 - 12 virtual source give near optimal contrast
 - Hanning apodization in transmit and receive processing
- Signal-to-noise ratio:
 - Use 32 elements in transmit
- Non-linear imaging
 - Repeat virtual source with positive and negative emission (pulse inversion)

Motion Estimation Optimization



- High velocities:
 - Maximum detectable velocity

$$v_{max} \propto \lambda f_{prf}$$

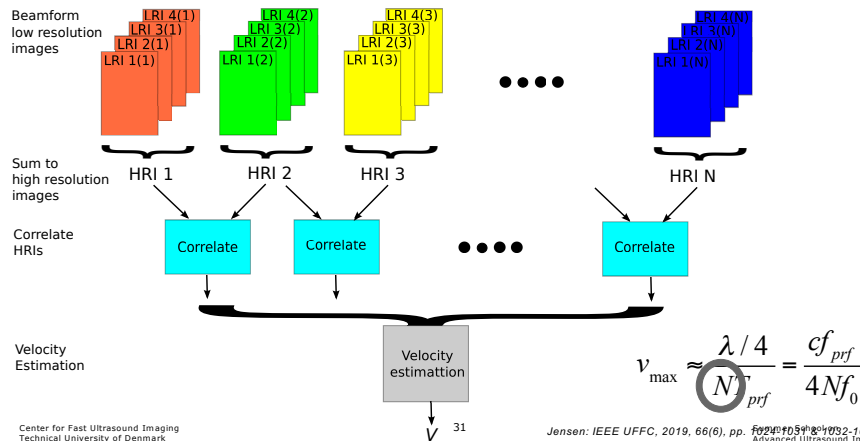
λ - Wavelength (c/f_0)
 f_{prf} - Pulse repetition frequency

- Solution:
 - Shortest possible time distance between high resolution images
 - Interleaved sequence, repetition of emissions

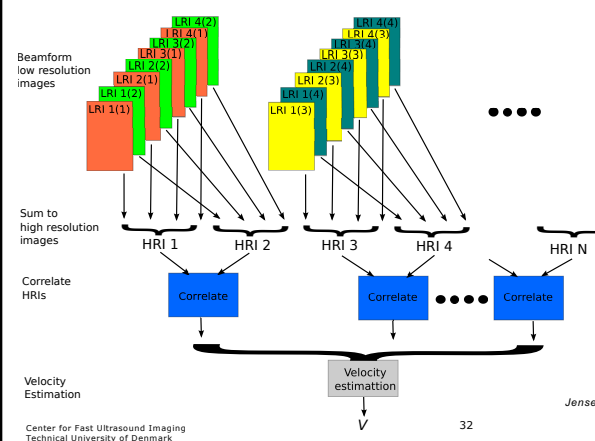
- Low velocities:
 - Minimum detectable velocity proportional to observation time $N/(f_{prf} N_{emis})$
 - Observation time limited by tissue motion in the image

- Solution
 - Motion estimation and correction
 - Continuous data sequence for unlimited observation time

Drawback of SA Velocity Imaging



SA VFI Interleaved Sequence



- 5 Virtual sources
- Interleaved with + - + for each virtual source - Pulse Inversion (5x3=15 LRI sequence)

- Data acquired using SARUS
- Phased array 3 MHz, 128 elements

$$v_{max} \approx \frac{\lambda / 4}{T_{prf}} = \frac{cf_{prf}}{4f_0}$$

Synthetic Aperture Sequence

- Synthetic aperture sequence with interleaved emissions
- Positive and negative emissions for PI imaging
- 12 virtual emissions using 32 elements and $F\# = -0.7$
- Virtual sources evenly spread over the aperture
- Continuous data acquisition for 2×12 emissions
- Applicable for any linear or phased array probe

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Estimates for Measured, Interleaved Data

*Mean velocity profile at 75 degrees,
 $f_{prf}=450$ Hz & directional beamforming*

- Directional beamforming and interleaved sequence
- SARUS measurements in flow rig
- $f_{prf} = 450$ Hz
- Effective $f_{prf} = 450/15=30$ Hz
- Bias: -1.35% , $SD=0.70\%$
- $V_{max}=10$ m/s for $f_{prf}=9$ kHz
- Even possible at $f_{prf}=225$ Hz @ 90°

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Corresponds to $V_{max} = 23.1$ m/s @ $f_{prf} = 10$ kHz

Jensen: IEEE UFFC, 2019, 66(6), pp. 1024-1031 & 1032-1038

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Verasonics Scanning Setup

- Verasonics Vantage 256 scanner
- Modified scan program with SARUS commands
- Real time GPU preview
- Continuous streaming to RAM at 3 Gbytes/s
- GPU beamforming and processing after acquisition
- SA PI sequence with 2×12 emissions
- HRI frame rate of 208 Hz

- Operated at 10 MHz
- In vivo scanning of exposed kidney of Sprague-Dawley rat

- Operated at 6 MHz
- Scanning of carotid bifurcation phantom with pulsating flow

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B-mode Image of Rat Kidney

Frame rate 208 Hz

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Linear B-mode SA images
Rat 77, frame rate 208 Hz

Jørgen Arendt Jensen

01-Sep-2022

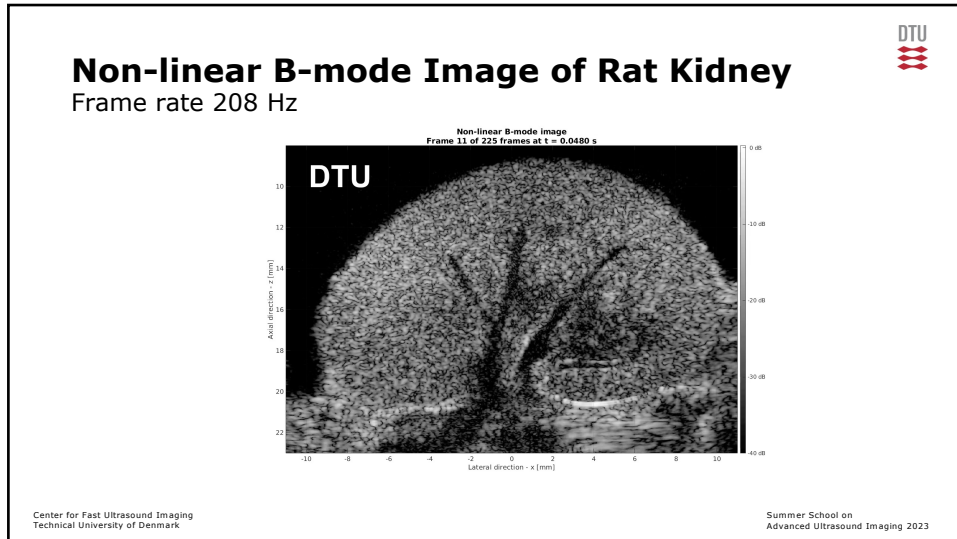
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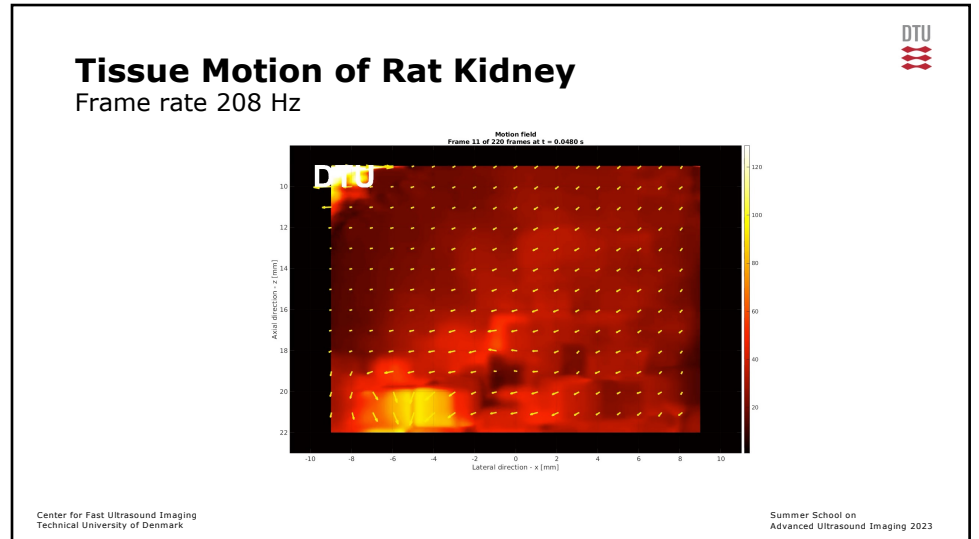
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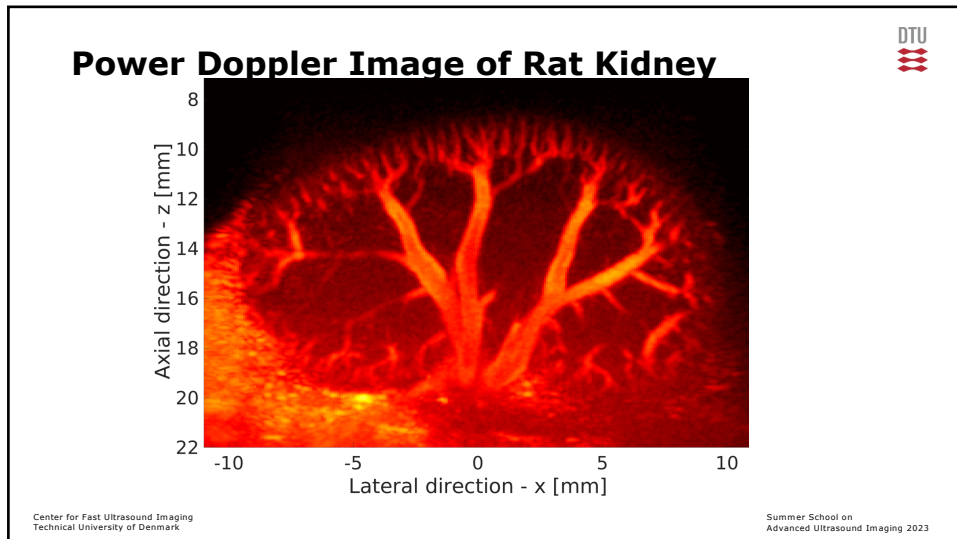
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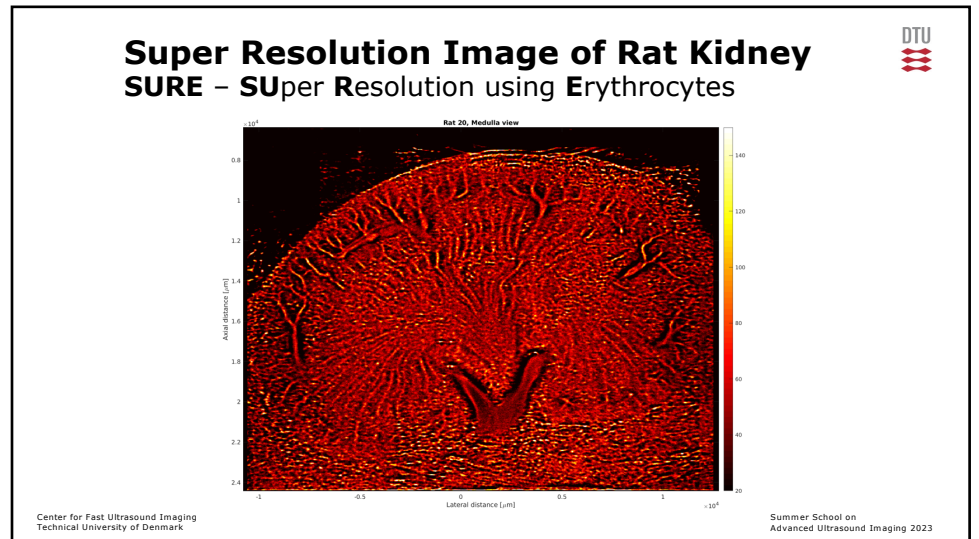
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Color Flow Map of Bifurcation Phantom

Frame rate 208 Hz



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Color Flow Map using Autocorrelation and SA Data
Carotid bifurcation phantom

Jørgen Arendt Jensen

06-Sep-2022

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Vector Flow Image, Bifurcation Phantom

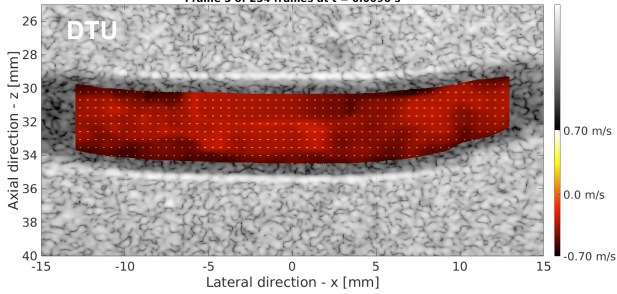
Frame rate 208 Hz



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Vector Flow Image, Bifurcation Phantom
Frame rate 208 Hz

Vector velocity image
Frame 3 of 234 frames at t = 0.0096 s



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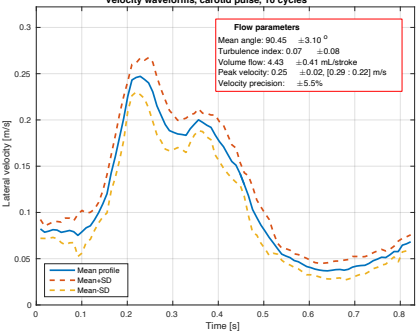
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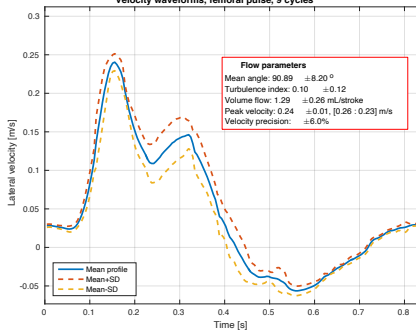
Quantification from multiple heart beats

Velocity waveforms, carotid pulse, 10 cycles



Flow parameters
 Mean angle: 90.45 ± 3.10 °
 Turbulence index: 0.07 ± 0.08
 Volume flow: 4.43 ± 0.41 mL/stroke
 Peak velocity: 0.25 ± 0.02 [0.29 - 0.22] m/s
 Velocity precision: ± 5.5%

Velocity waveforms, femoral pulse, 9 cycles



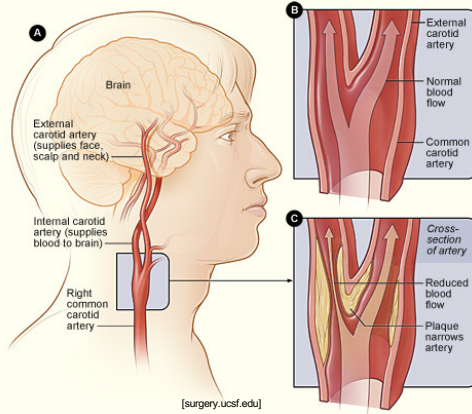
Flow parameters
 Mean angle: 90.89 ± 8.20 °
 Turbulence index: 0.10 ± 0.12
 Volume flow: 1.29 ± 0.26 mL/stroke
 Peak velocity: 0.24 ± 0.01 [0.26 - 0.23] m/s
 Velocity precision: ± 6.0%

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Pressure Gradient Measurements



[surgery.ucsf.edu]

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Estimating pressure gradients from Navier-Stokes equation

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Temporal acceleration

Pressure gradient

Neglect gravitation as patient lies down

$$\rho \left[\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} \right] = -\nabla p + \rho \mathbf{g} + \mu \nabla^2 \mathbf{v}$$

$m \cdot a = F$

Neglect viscosity due to large vessels

Spatial acceleration

VF I can estimate both spatial and temporal accelerations

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Pressure gradients in carotid bifurcation

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B-mode

[Ultrasound] $\Delta P = P_2 - P_1$

Standard deviation of a 2.2 Pa to 3.2 Pa

An order of magnitude more precise than pressure wires and catheters

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SA Low Velocity Flow

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Conventional Imaging

SA Plane Wave Imaging

Mace et al., *Nature Methods*, 2011(8) pp. 662-664

Mace et al., *IEEE UFFC*, 2013, 60(3), pp. 492-506

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Brain Disorders and Nervous Systems

Epileptic seizure in a rat brain

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CBV Changes (%)

50

25

0

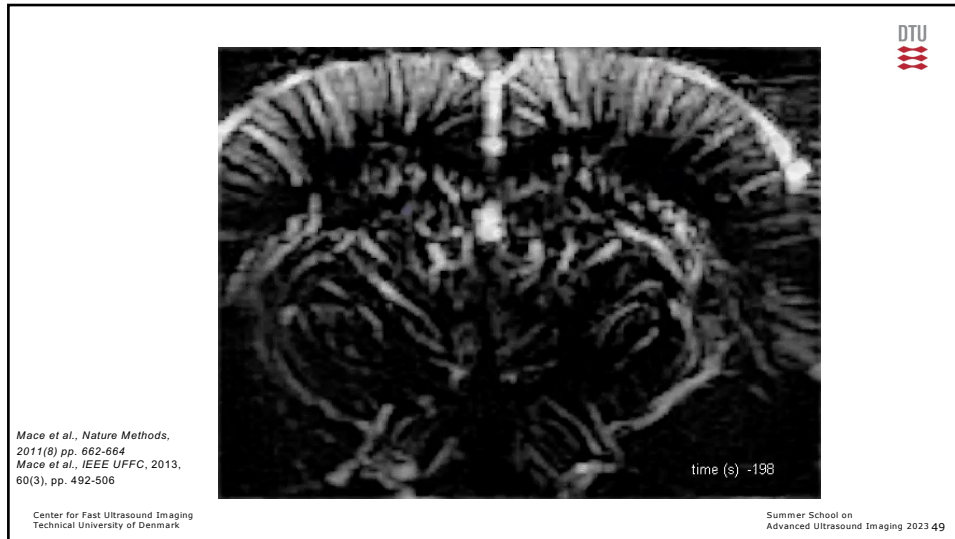
-25

Courtesy of: E. Macé, G. Montaldo, I. Cohen, M. Baulac, M. Fink, M. Tanter, *Nature Methods*, July 2011

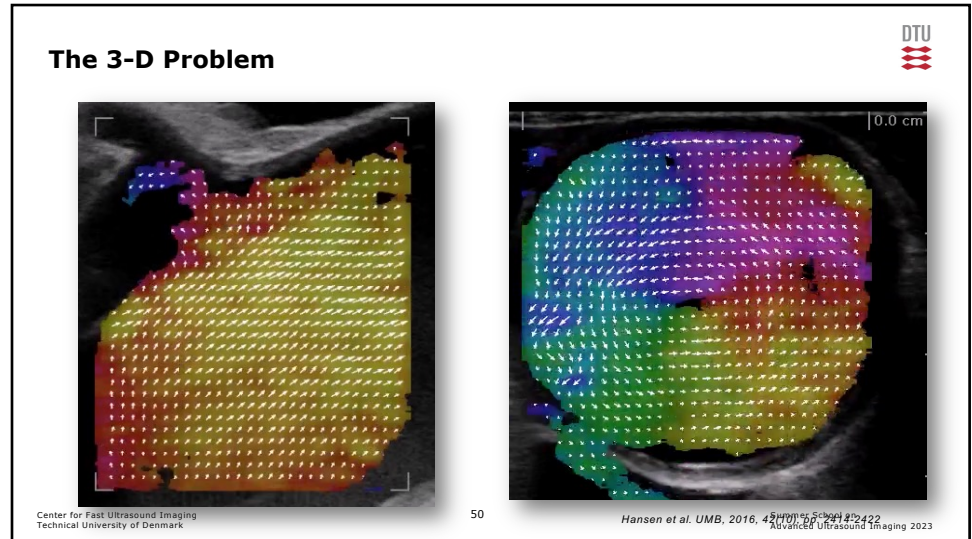
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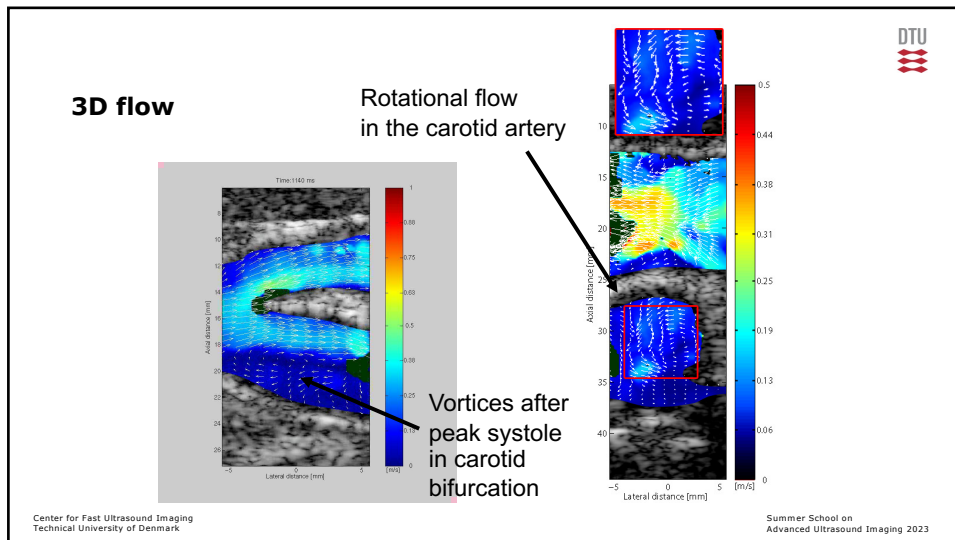
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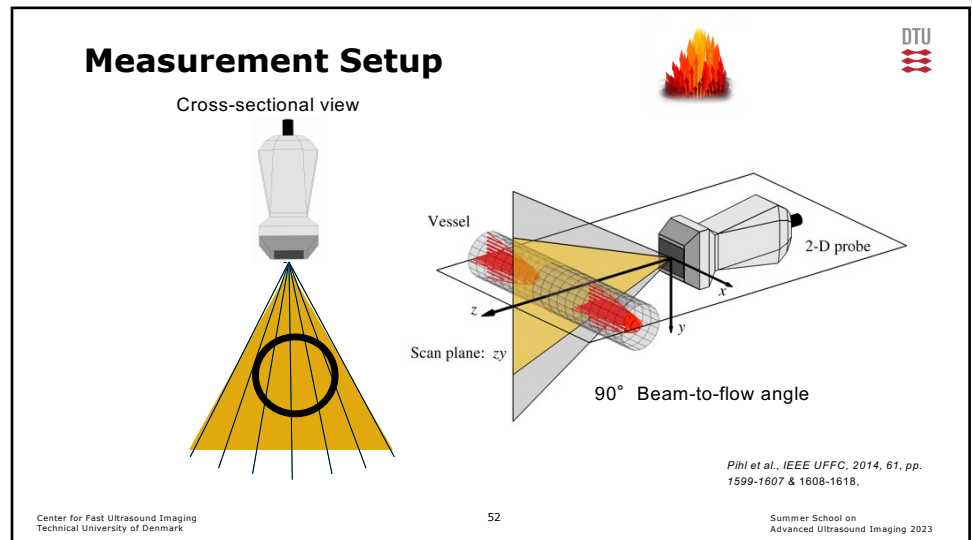
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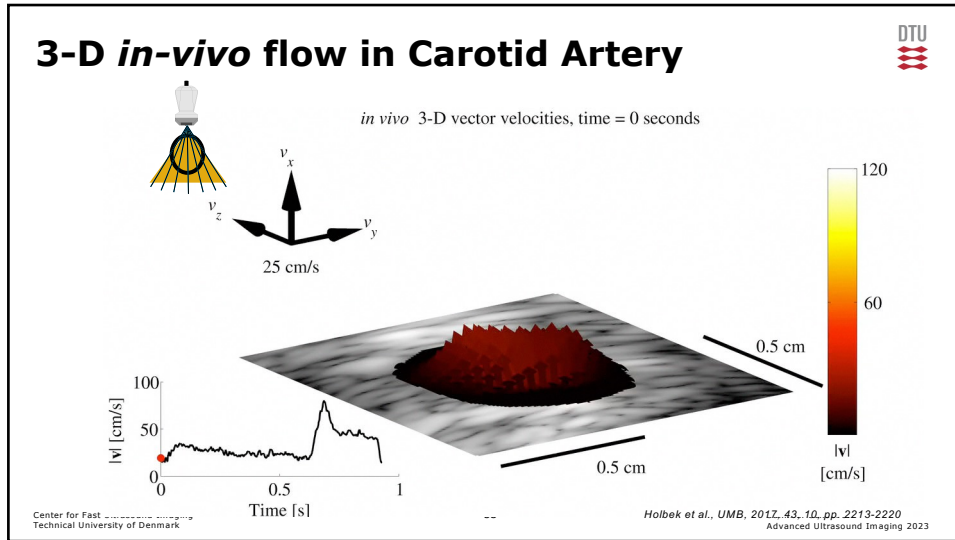
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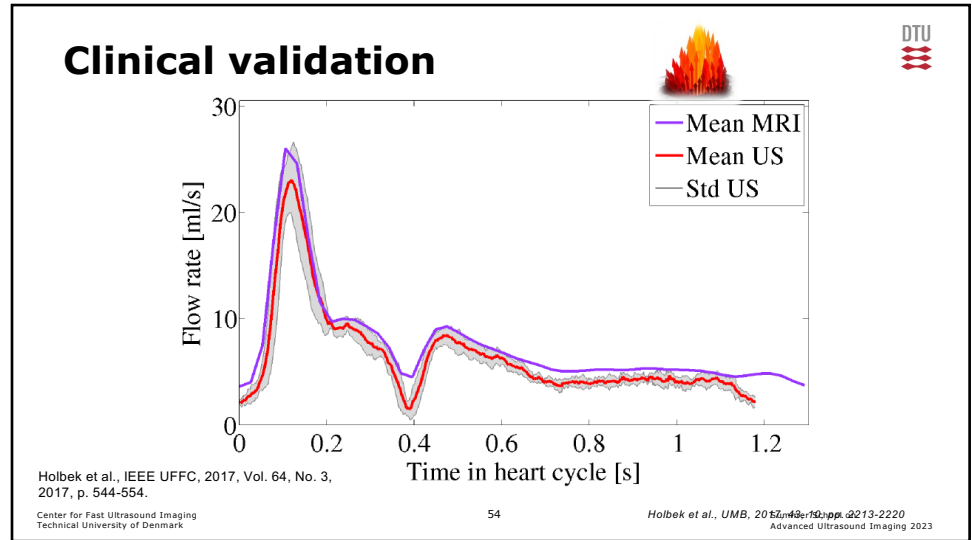
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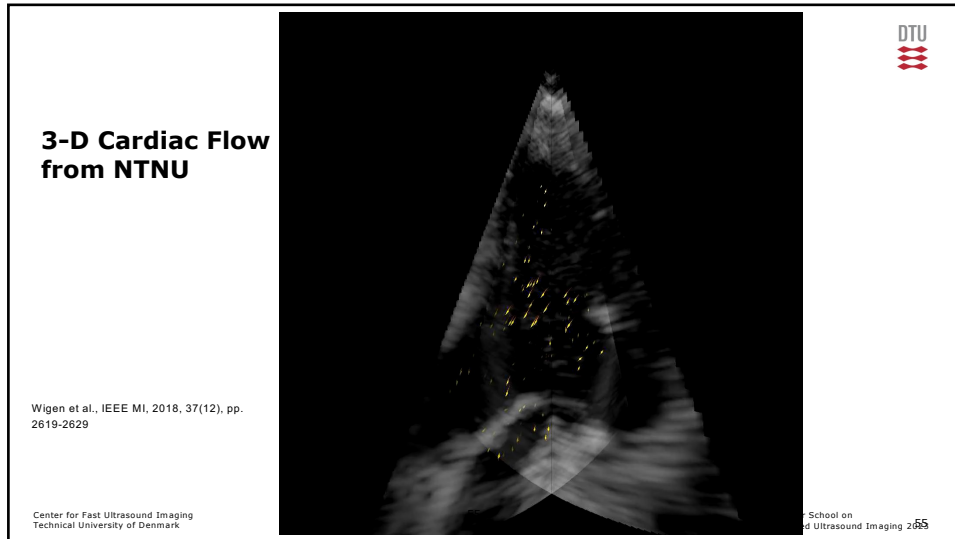
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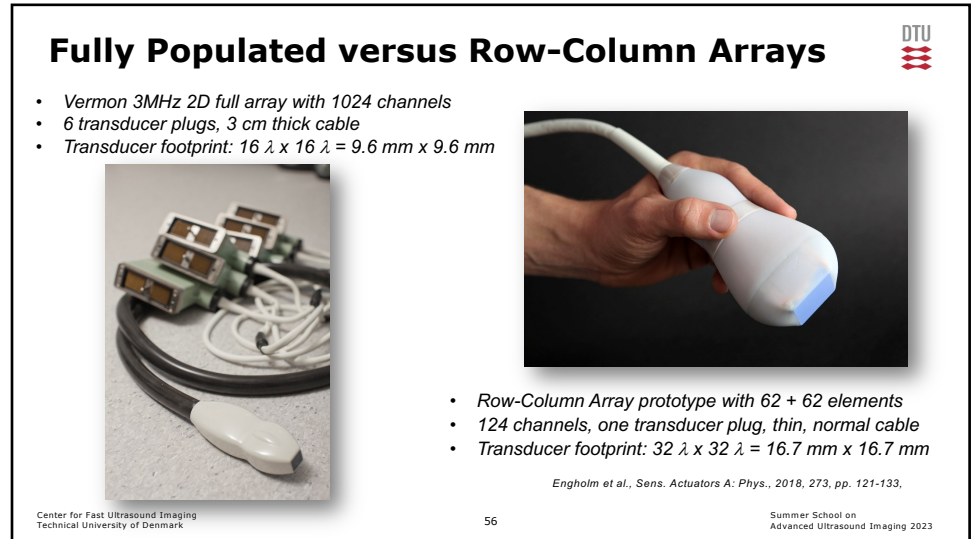
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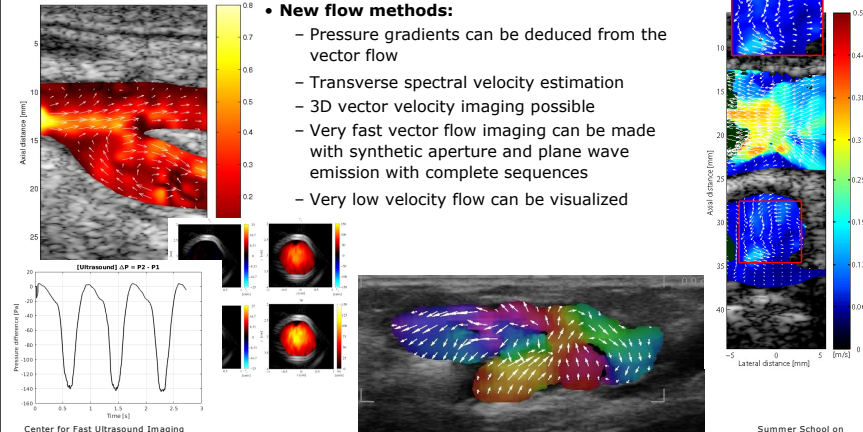
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Perspective on vector velocity imaging



• New flow methods:

- Pressure gradients can be deduced from the vector flow
- Transverse spectral velocity estimation
- 3D vector velocity imaging possible
- Very fast vector flow imaging can be made with synthetic aperture and plane wave emission with complete sequences
- Very low velocity flow can be visualized

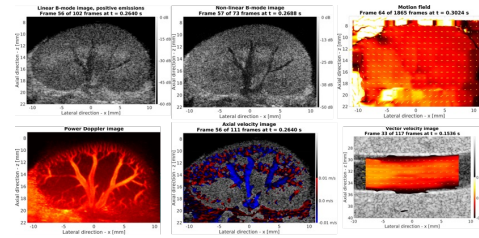


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Synthetic Aperture Imaging can give a Paradigm Shift in Ultrasound



- Universal SA sequence can be made
- Near optimal performance with 12 virtual sources
 - Non-linear images
 - Fast motion estimation
- Pulse inversion and interleaving yields
 - Precise velocity estimates
 - Low velocity
 - Pressure gradients and quantification
 - Super resolution
- Continuous data gives
 - Precise velocity estimates
 - Low velocity
 - Pressure gradients and quantification
 - Super resolution
- Images can be made retrospectively from the complete data set for precise diagnosis

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