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# Advanced Ultrasound Imaging 2023 Ultrasound Vector Velocity Imaging

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$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

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## Modern color flow mapping

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## Ultrasound Vector Velocity Imaging

### Part I: Vector velocity imaging using transverse oscillation

$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

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## Conventional velocity estimation system

- Low frame rate (approx. 20 Hz)
- Angle dependent velocity estimation

- Velocity changes direction in the image
- Determination is dependent on angle between beam and flow:

$$V_z = |v| \cos(\text{angle})$$

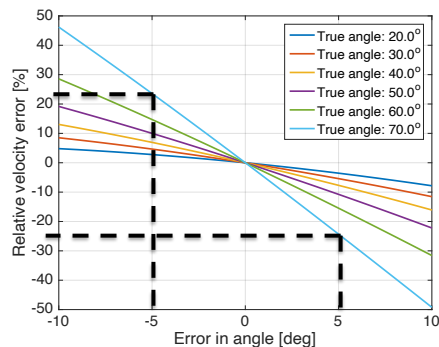
- At 45 degrees: 71% of velocity
- At 60 degrees: 50% of velocity
- At 80 degrees: 17% (!) of velocity
- At 90 degrees: 0%

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## Sensitivity to Angle



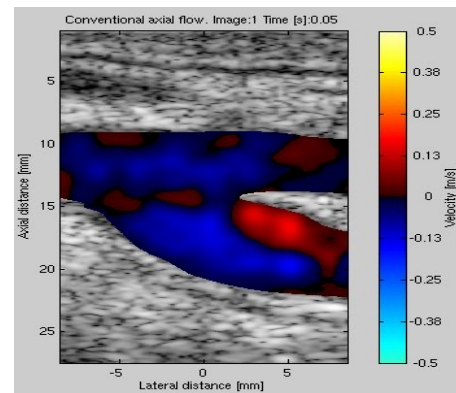
At 70° a 5° angle error gives a velocity error of more than +/-20%

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## Complicated flow in bifurcation



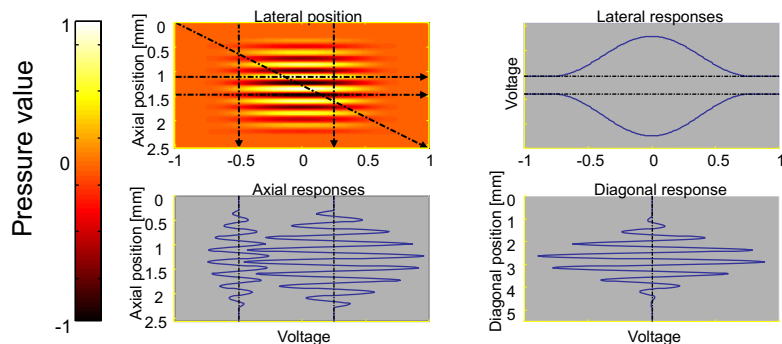
- What is the magnitude of the flow?
- What directions does it have?
- Is it normal?
- Not possible to use one correction factor
- Angle between beam and flow changes as a function of place and time
- Full velocity vector is needed

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## Normal velocity measurement: Sound field oscillates in ultrasound direction

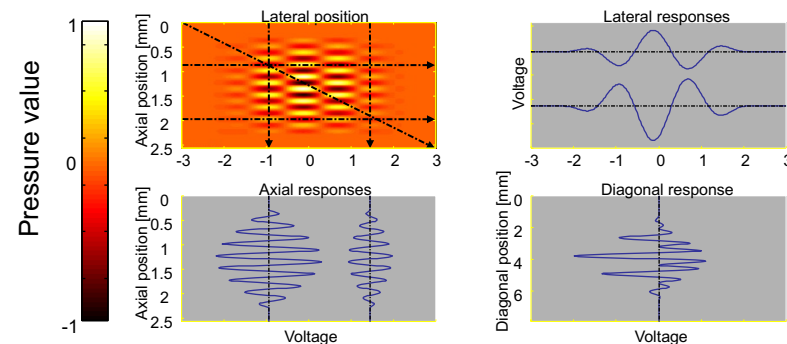


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## New vector velocity: Sound field also oscillates across beam



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## Simple generation

Oscillation across

Ultrasound propagation direction

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## Generation for a transducer

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## Fourier relation

Fourier relation between transducer apodization function  $r(\xi)$  and the transverse field  $R(x)$  at the focus:

$$R(x) = k_1 \int_{-\infty}^{+\infty} r(\xi) \exp\left(-j \frac{2\pi}{\lambda_z z} x \xi\right) d\xi = k_1 F\{r(\xi)\}$$

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## Creating a bounded lateral oscillation

Desired field:  $R(x) = \text{rect}(L) \cos\left(2\pi \frac{x}{\lambda_x}\right)$

Apodization function:

$$r(\xi) = F^{-1}\{R(x)\} = F^{-1}\{\text{rect}(L)\} * F^{-1}\{\cos\left(2\pi \frac{x}{\lambda_x}\right)\}$$

$$= \frac{L}{2Z\lambda_z} \left\{ \text{sinc}\left(\pi \left(\frac{\xi}{z\lambda_z} + \frac{1}{\lambda_x}\right)L\right) + \text{sinc}\left(\pi \left(\frac{\xi}{z\lambda_z} - \frac{1}{\lambda_x}\right)L\right) \right\}$$

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### Lateral oscillation period

- Peak position

$$\frac{\xi_p}{z \lambda_z} = \pm \frac{1}{\lambda_x}$$

- Lateral oscillation period:

$$\lambda_x = \frac{2z\lambda_z}{D}$$

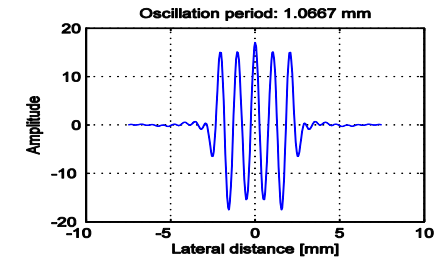
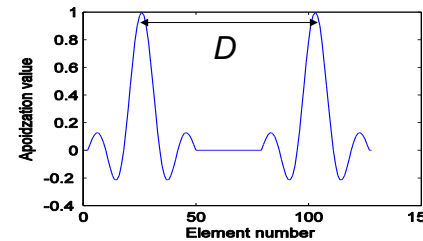
- Distance between peaks

$$2\xi_p = \frac{z\lambda_z}{\lambda_x}$$

-D: distance between peaks

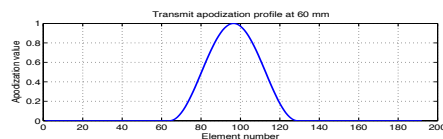
$\lambda_x = \frac{2z\lambda_z}{D}$

z – depth  
D – distance between peaks  
 $\lambda_z$  – axial wavelength  
 $\lambda_x$  – Lateral oscillation period



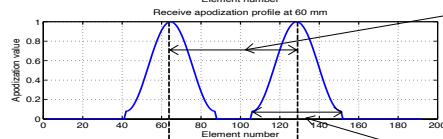
### Design of Lateral oscillation

$$\lambda_x = \frac{2\lambda z}{D} = \frac{2\lambda z}{N_d P_i}$$



Assume  $\lambda_x = 4 P_i$   
Distance between peaks:

$$N_d = \frac{2\lambda z}{4P_i^2}$$



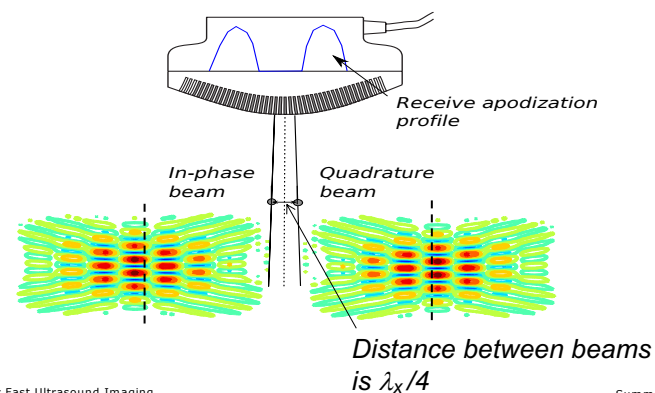
Width of peaks:

$$N_w = \frac{\lambda z}{2F_{\#TO} P_i}$$

$\lambda$  – wavelength  
D – distance between peaks  
 $F_{\#TO}$  – F-number for TO

z – depth  
 $P_i$  – element pitch

### In-phase and quadrature fields



## Velocity estimation



- Frequency for axial velocity
- Frequency for lateral velocity

$$f_z = \frac{2v_z}{c} f_0 = \frac{2v_z}{\lambda_z}$$

$$f_x = \frac{v_x}{\lambda_x}$$

Frequency should be found from complex received signal

## Pre-processing in New Estimator



Spatial quadrature signal:

$$r_{sq}(i) = \cos(2\pi f_p i T_{prf}) \exp(j2\pi f_x i T_{prf})$$

Temporal Hilbert transform:

$$r_{sqh}(i) = \sin(2\pi f_p i T_{prf}) \exp(j2\pi f_x i T_{prf})$$

Pre-processed signals:

$$r_1(i) = r_{sq}(i) + jr_{sqh}(i)$$

$$r_2(i) = r_{sq}(i) - jr_{sqh}(i)$$

## Processed signals:



$$r_1(i) = \exp(j2\pi i T_{prf} (f_x + f_z))$$

$$r_2(i) = \exp(j2\pi i T_{prf} (f_x - f_z))$$

Phase differences:

$$d\theta_1 = 2\pi T_{prf} (f_x + f_z)$$

$$d\theta_2 = 2\pi T_{prf} (f_x - f_z)$$

Velocity estimates:

$$d\theta_1 + d\theta_2 = 2\pi 2T_{prf} f_x, \quad v_x = \frac{(d\theta_1 + d\theta_2)\lambda_x}{4\pi T_{prf}}$$

## Final steps in derivation



Phase estimation:  $r(i) = x(i) + y(i)$

$$R(m) = \frac{1}{N-m} \sum_{i=0}^{N-m} r^*(i)r(i+m)$$

$$d\theta = \arctan\left(\frac{\Im\{R(1)\}}{\Re\{R(1)\}}\right)$$

Arctan calculation:

$$\tan(A+B) = \frac{\tan(A) + \tan(B)}{1 - \tan(A)\tan(B)}$$

## Estimation of Velocity

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Transducer

**Lateral velocity estimator:**

$$v_x = \frac{d_x}{2\pi 2T_{pf}} \arctan \left( \frac{\sum_{i=1}^{N-1} \Im\{R_1(i)\}\Re\{R_2(i)\} + \Im\{R_2(i)\}\Re\{R_1(i)\}}{\sum_{i=1}^{N-1} \Re\{R_1(i)\}\Re\{R_2(i)\} - \Im\{R_1(i)\}\Im\{R_2(i)\}} \right)$$

**Axial velocity estimator:**

$$v_z = \frac{c}{2\pi f_0 4T_{pf}} \arctan \left( \frac{\sum_{i=1}^{N-1} \Im\{R_1(i)\}\Re\{R_2(i)\} - \Im\{R_2(i)\}\Re\{R_1(i)\}}{\sum_{i=1}^{N-1} \Re\{R_1(i)\}\Re\{R_2(i)\} + \Im\{R_1(i)\}\Im\{R_2(i)\}} \right)$$

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## RASMUS

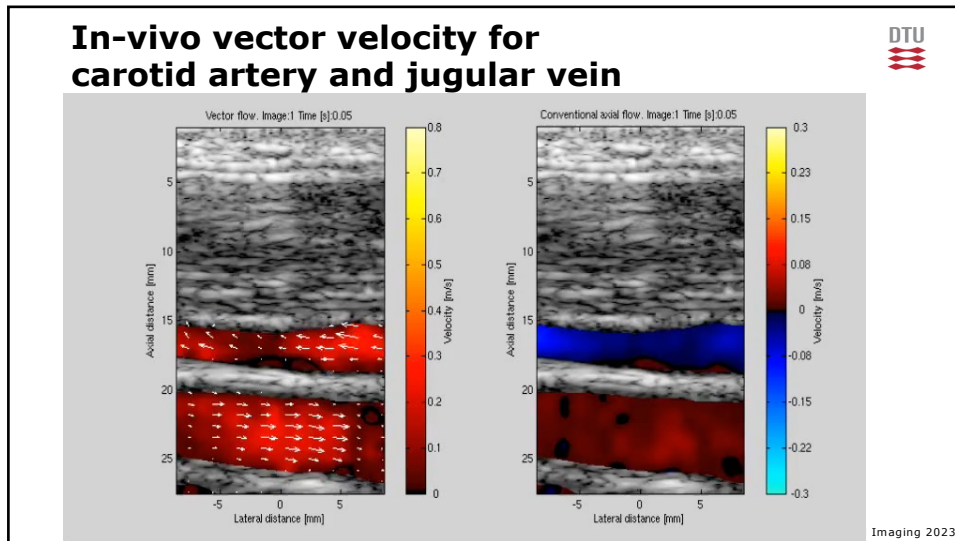
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- Remotely Accessible Software programmable Multi-channel Ultrasound System
- Can be used for synthetic aperture, real-time, *in-vivo* data acquisition
- Made solely for research purposes

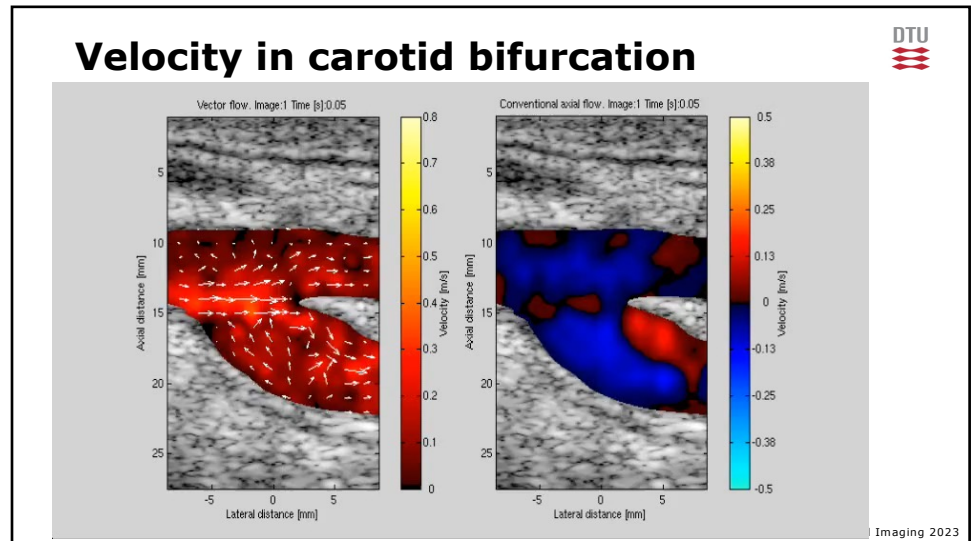
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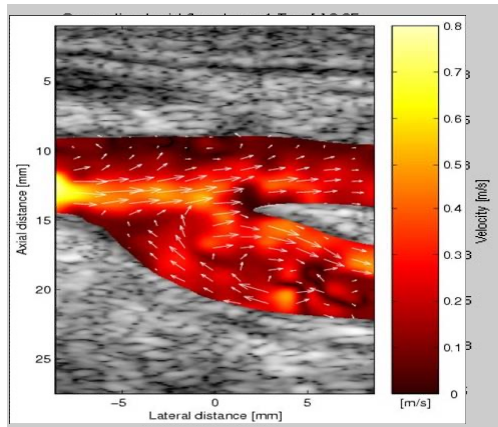
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## Complicated flow in bifurcation



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## New Transverse Estimator



$$v_x = \frac{\lambda_x}{2\pi 4T_{prf}} \arctan\left(\frac{\Im\{R_1(1)\}\Re\{R_2(1)\} + \Im\{R_2(1)\}\Re\{R_1(1)\}}{\Re\{R_1(1)\}\Re\{R_2(1)\} - \Im\{R_1(1)\}\Im\{R_2(1)\}}\right)$$

$$v_z = \frac{\lambda}{2\pi 4T_{prf}} \arctan\left(\frac{\Im\{R_1(1)\}\Re\{R_2(1)\} - \Im\{R_2(1)\}\Re\{R_1(1)\}}{\Re\{R_1(1)\}\Re\{R_2(1)\} + \Im\{R_1(1)\}\Im\{R_2(1)\}}\right)$$

$$R_1(l) = \frac{1}{(N-1)N_d N_s} \sum_{i=1}^{N-1} \sum_{n=1}^{N_d} \sum_{k=-N_s/2}^{N_s/2} r_1^*(k+N_z, n, i) r_1(k+N_z, n, i+l)$$

$$R_2(l) = \frac{1}{(N-1)N_d N_s} \sum_{i=1}^{N-1} \sum_{n=1}^{N_d} \sum_{k=-N_s/2}^{N_s/2} r_2^*(k+N_z, n, i) r_2(k+N_z, n, i+l)$$

$R_1$  - Complex autocorrelation of signal one averaged over directional signal and depth

$R_2$  - Complex autocorrelation of signal two

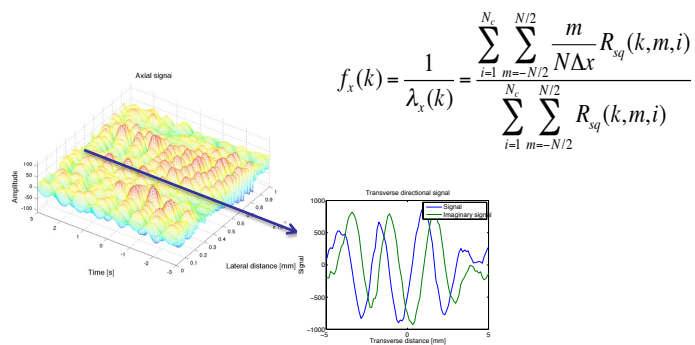
$N_z$  - RF sample depth for velocity estimate

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## Calculation of Mean Lateral Oscillation Wavelength



$$f_x(k) = \frac{1}{\lambda_x(k)} = \frac{\sum_{i=1}^{N_s} \sum_{m=-N/2}^{N/2} \frac{m}{N\Delta x} R_{sq}(k, m, i)}{\sum_{i=1}^{N_s} \sum_{m=-N/2}^{N/2} R_{sq}(k, m, i)}$$

$R_{sq}(k, m, i)$  - Fourier transform of lateral signal at sample  $k$  and emission  $i$

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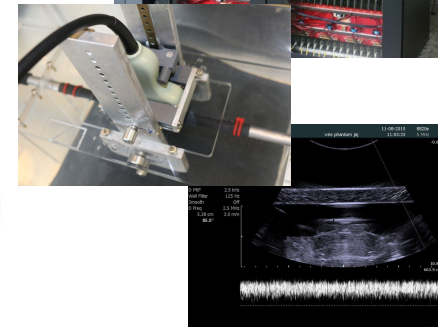
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## SARUS Experimental Ultrasound Scanner



- 192 channels sampled at 17.5 MHz/12 bits
- 129 B-mode emissions
- Interspaced with VFI emissions focused at 105 mm
- $f_{prf} = 5$  kHz
- BK Medical 8820e 3 MHz convex array probe used
- Data acquired for 30 frames
- Acquired on rig with parabolic flow

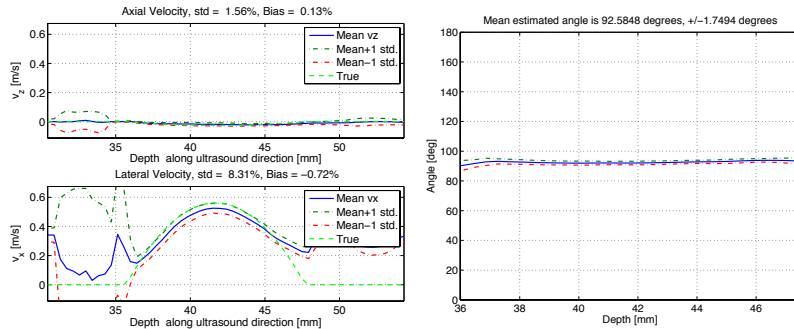


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## Velocity Profiles at 40 mm using 16 Emissions at 90° Beam-to-flow Angle



$V_x$  std: 8.31%, bias -0.72%, angle std: 1.75 degrees

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## Is it Accurate? Clinical study



- 11 healthy volunteers
  - seven males and four females,
  - 24 – 44 years old, mean age: 32 years)
- Each person was scanned by US and MRI



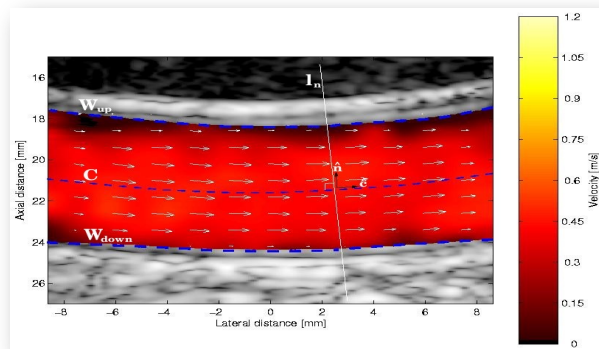
- Examination for every person were performed at two separate occasions with no more than a week in between.
- The volunteer rested supine 15 minutes prior to both examinations.
- All scans were carried out by an experienced radiologist.

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## Vector Velocity Image of Stroke Volume

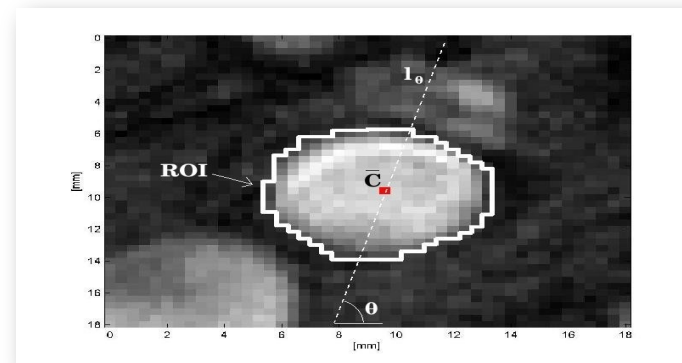


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## MR Measurement of Volume Flow



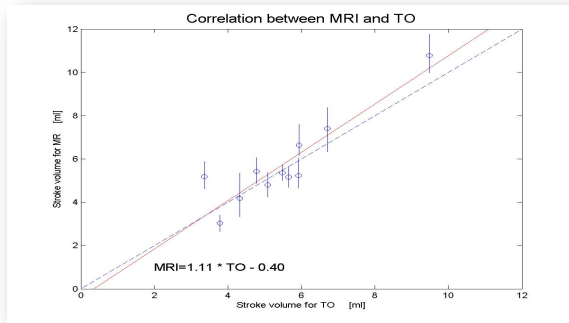
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## Clinical Validation of Vector Flow against MR



$R = 0.91, P < 0.01$   
95% CI for R: 0.69 to 0.98

Regression line:

$$\text{MRI} = 1.11 * \text{TO} - 0.4 \text{ ml}$$

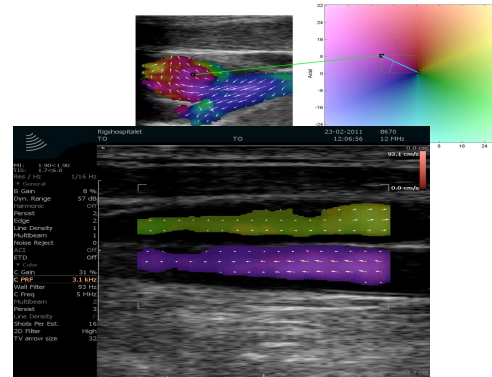
Vertical bars indicate range for rotational symmetry assumption.

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## Commercial implementation: BK Medical ProFocus scanner FDA approved January, 2012

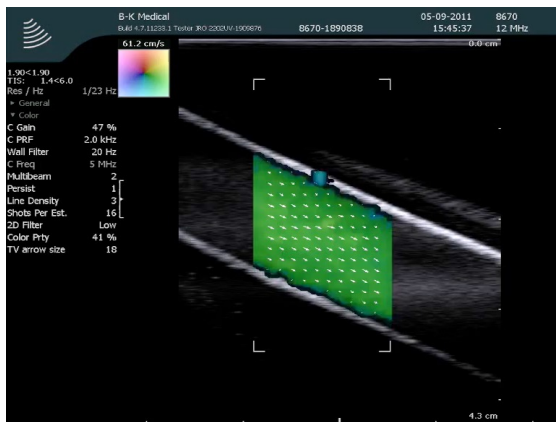


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## Display of velocity

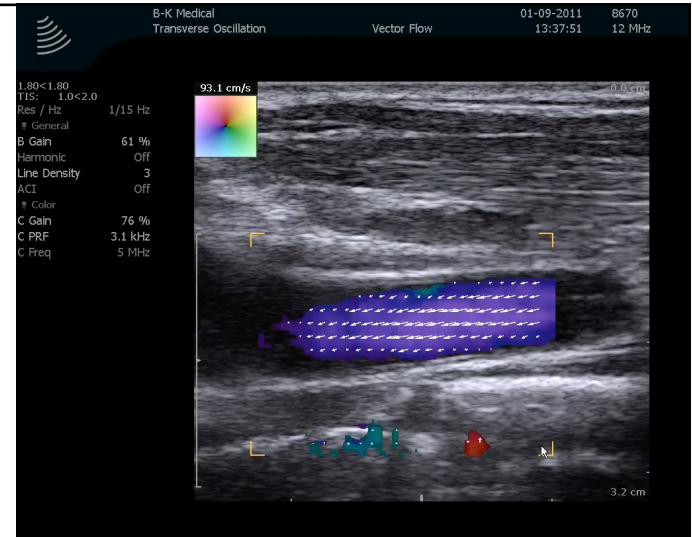


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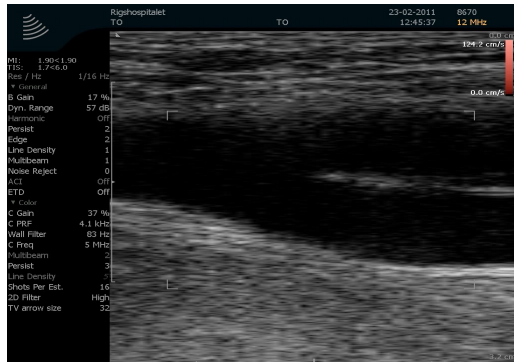
## Scanning of the carotid artery



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## Bifurcation in Femoral Artery



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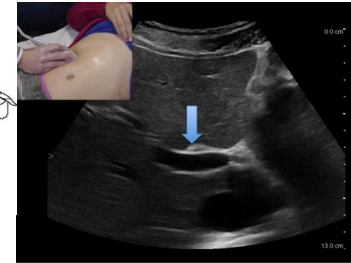
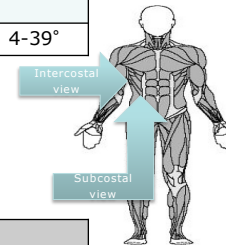
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## Influence of Beam-to-flow Angle



TO	SDU
10-61°	4-39°



TO	SDU
53-130°	57-99°

From Brandt et al., IEEE IUS, 2015

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## Estimated Peak Velocities



	Mean TO (SD)	Mean SDU (SD)	P-value
Intercostal view	0.203 ± (0.038) m/s	0.202 ± (0.029) m/s	0.94
Subcostal view	0.180 ± (0.034) m/s	0.320 ± (0.060) m/s	0.001
P-value	0.26	0.001	

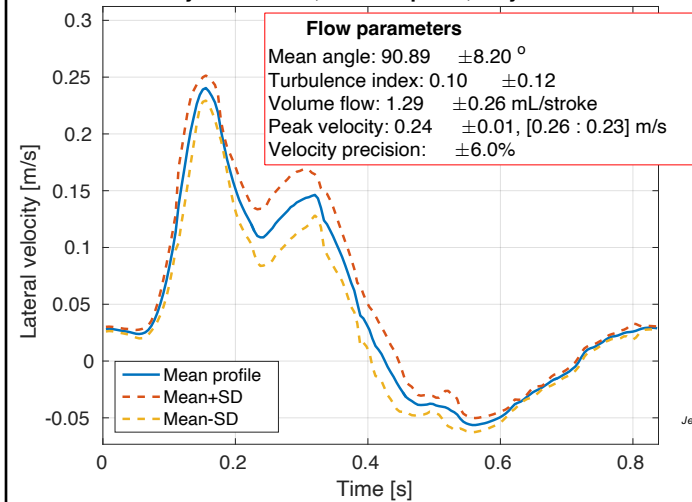
From Brandt et al., IEEE IUS, 2015

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## Velocity waveforms, femoral pulse, 9 cycles

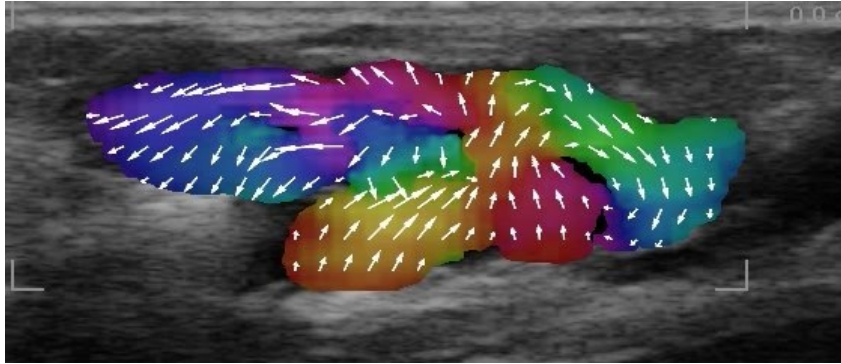


Jensen, IEEE UFFC, 2017, 64(8), pp. 1194-1204

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## Vein-artery connection for kidney hemodialysis patient

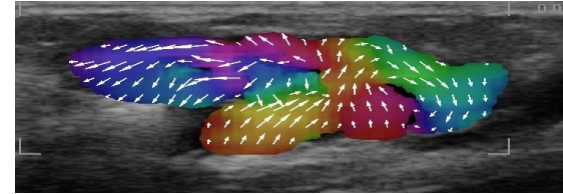


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## Anatomy of vein-artery graft

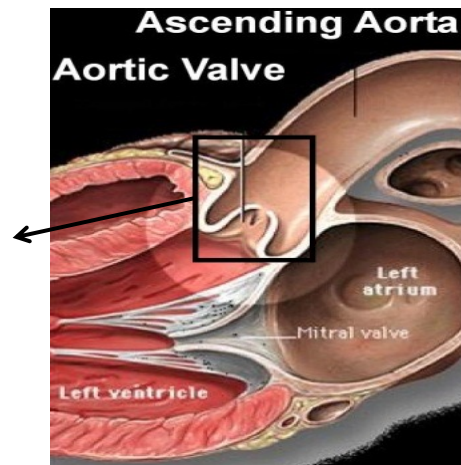
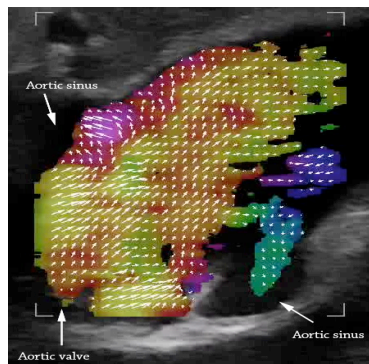


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## Anatomy of Intercardiac Scan of Right Atrium

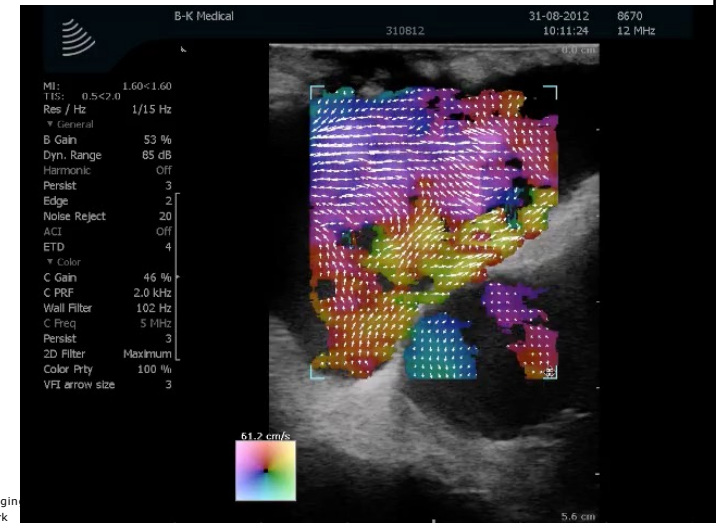


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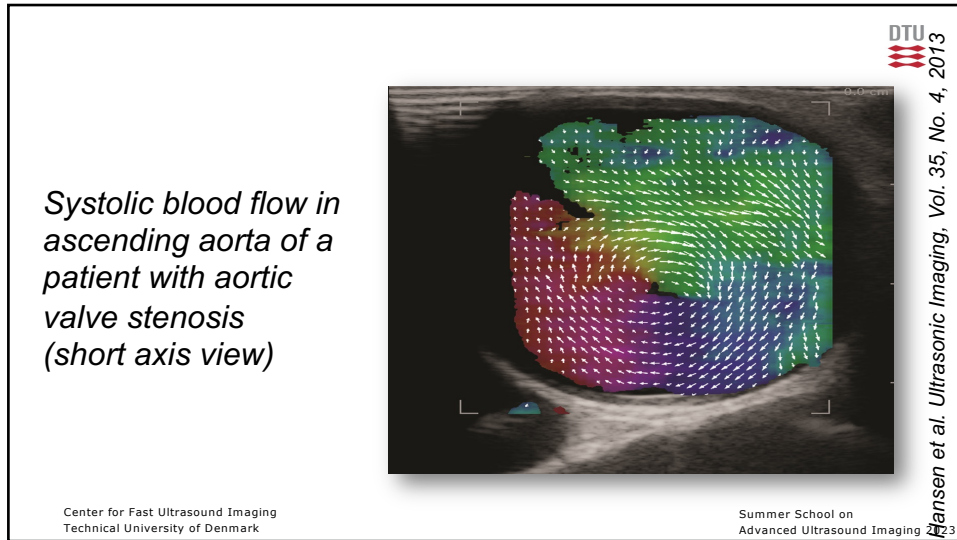
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## Intercardiac scan Right Atrium

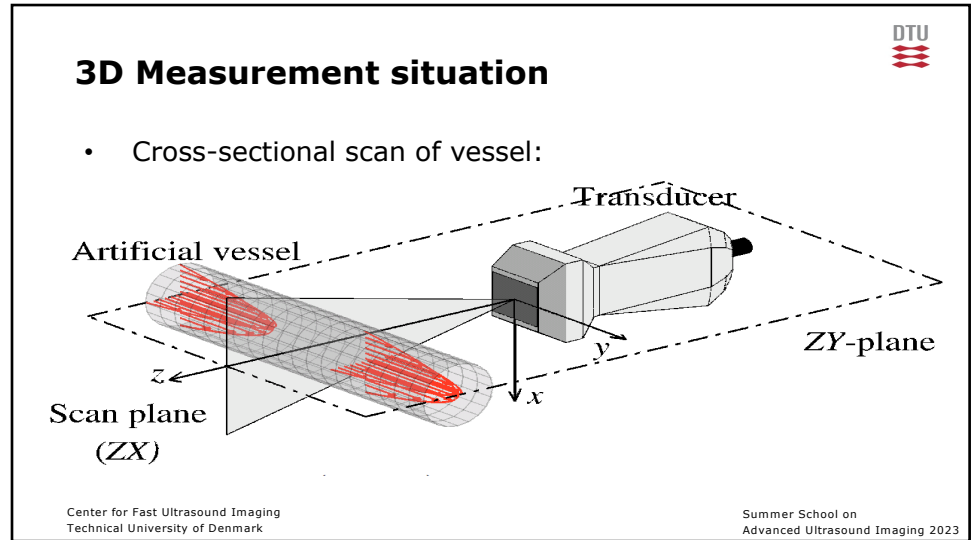


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**Requirements for 3D velocity estimation**

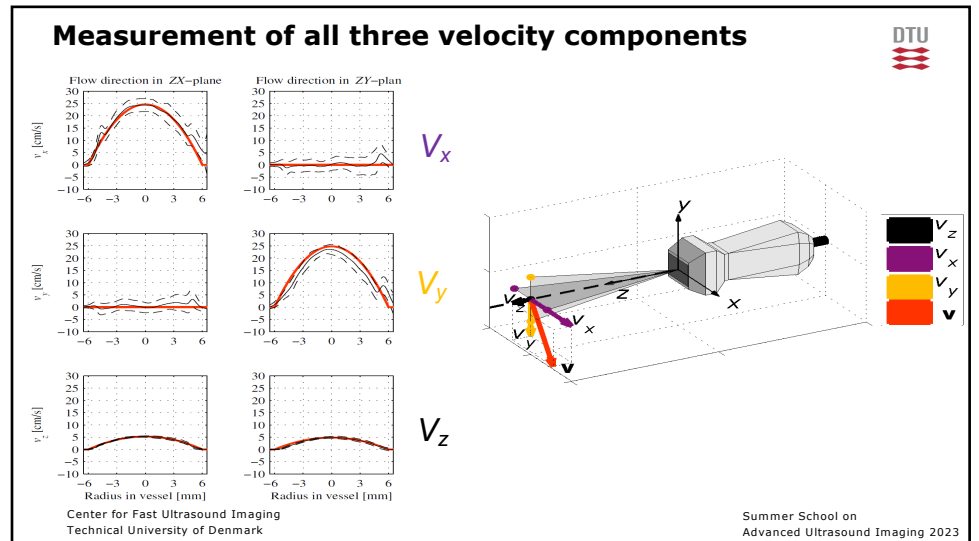
- 2D array transducer
  - 32 x 32 = 1024 elements
- Reception on all 1024 elements
- Beamforming of 5 beams in parallel from received data
- Three different apodization patterns should be employed

Leads to acquisition of 32 x 32 2D array

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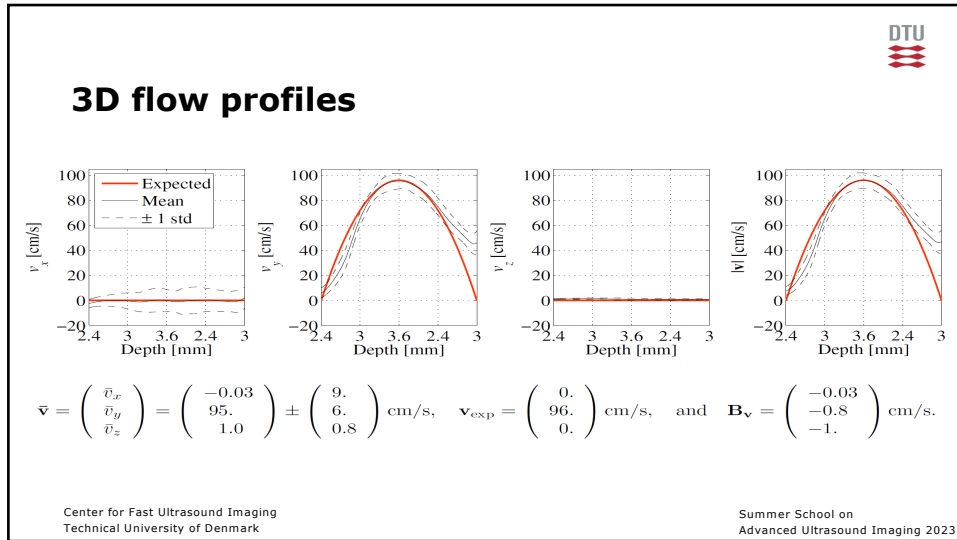
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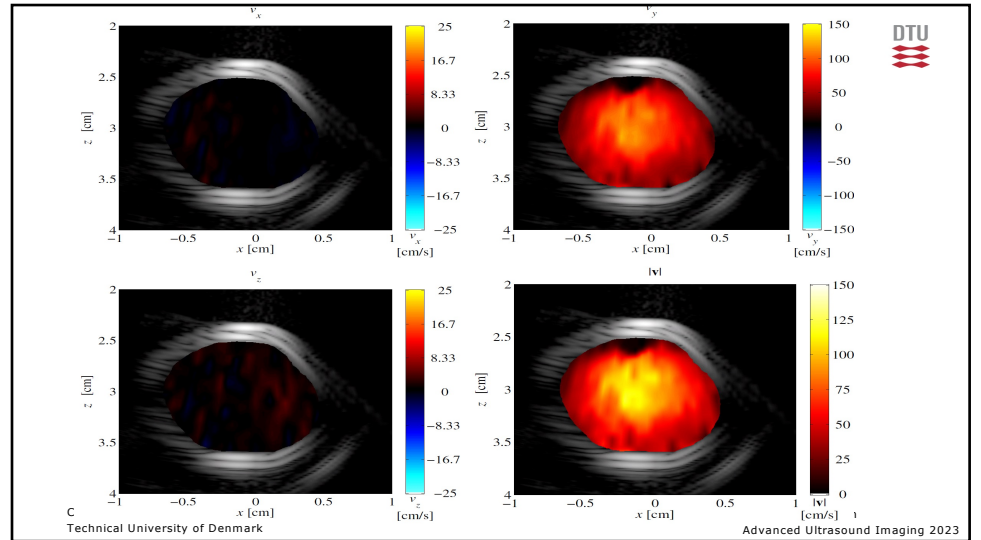


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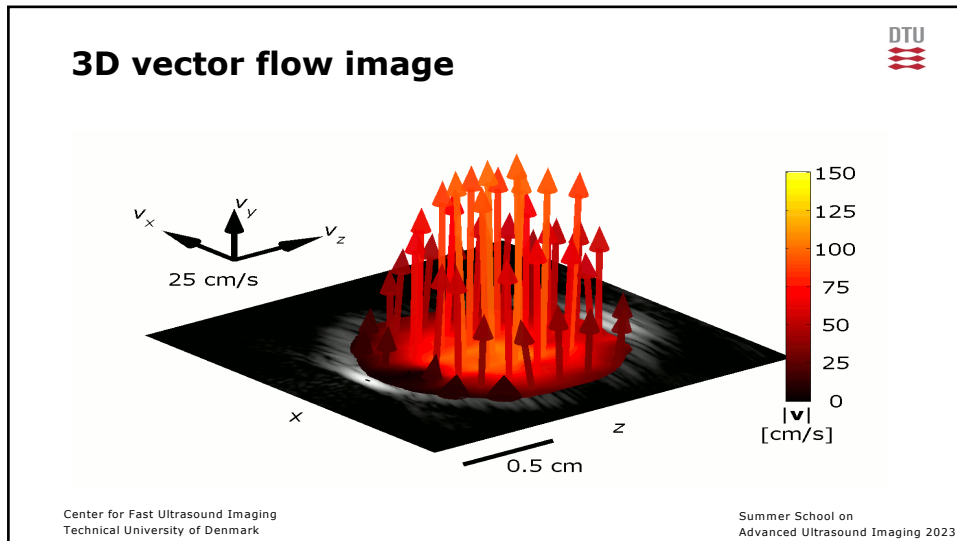




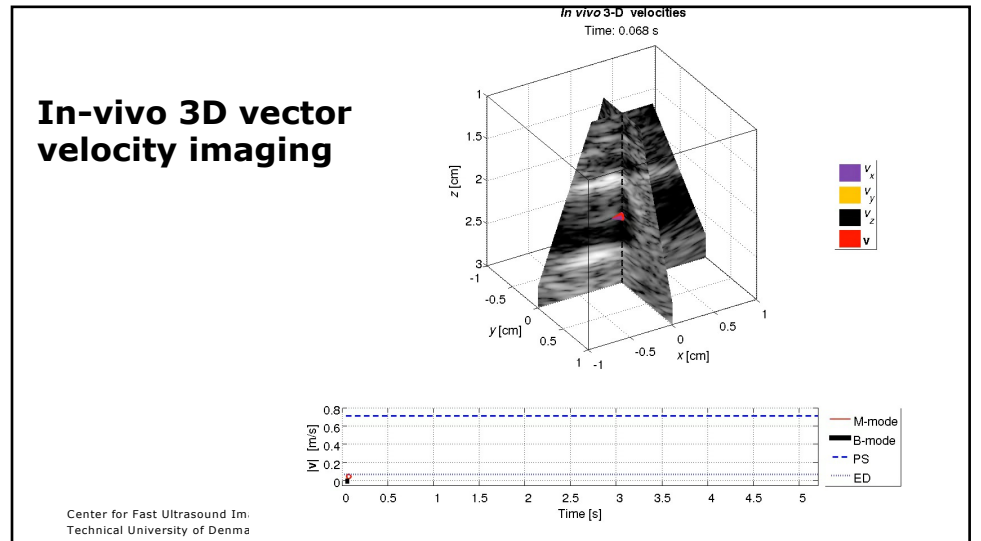
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# Ultrasound Vector Velocity Imaging

Part II:

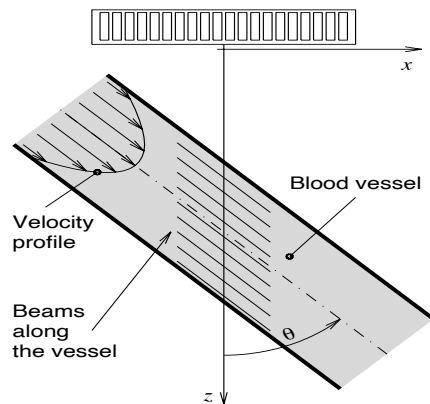
## Directional beamforming and other vector velocity methods

$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

# Outline

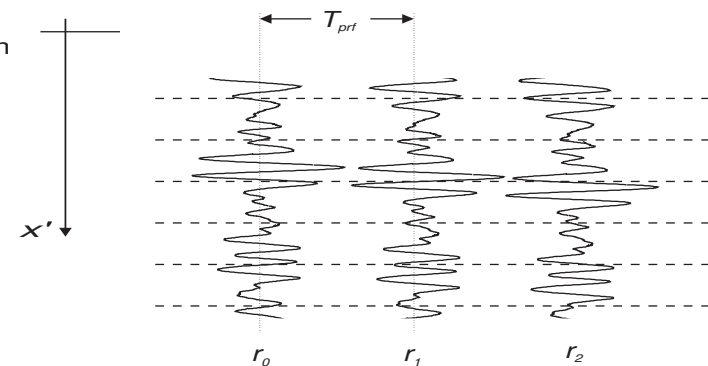
- Directional beamforming
  - Beamformation
  - Angle estimation
- Crossed beams velocity estimation
- Speckle tracking
- Finding the angle from the spectral display

# Directional beamforming



# Cross-correlation of directional lines

Pulse emission





## Cross-Correlation to Find Velocity

$$R_{12}(n) = \frac{1}{M} \sum_{j=0}^{M-1} r_1(j)r_2(j+n)$$

$$= \frac{1}{M} \sum_{j=0}^{M-1} r_1(j)r_1(j+n-n_s)$$

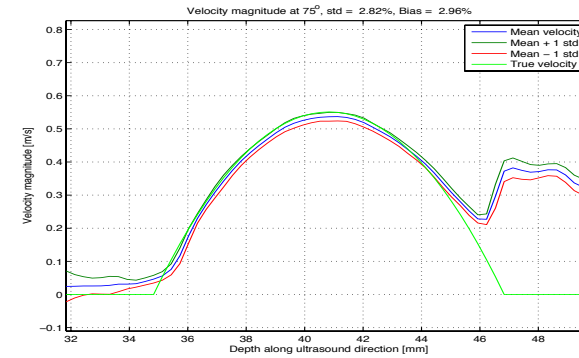
$$R_{12}(n) = R_{11}(n-n_s)$$

Velocity estimate is:

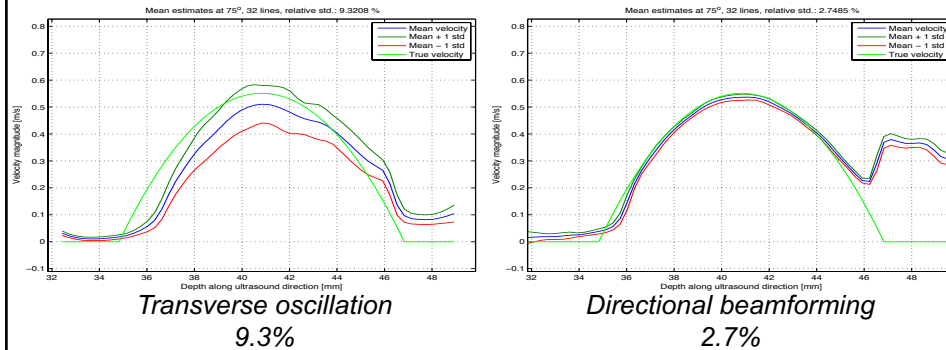
$$v_{mag} = \frac{n_s \Delta x'}{T_{prf}}$$

## Velocity profiles for directional beamforming

75° flow angle, 16 emissions/estimate, line length: 20 λ



## Performance using the same data



## Number of calculations

Transverse oscillation      Directional beamforming

$$N_{TO} = (4 \cdot 28 N_s) \frac{f_s}{N_s} F_f$$

$$N_d = (N_l^2 + N_l) \frac{f_s}{N_s} F_f$$

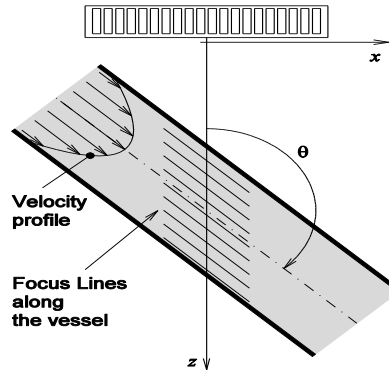
Ratio: 
$$R_c = \frac{N_d}{N_{TO}} = \frac{(N_l^2 + N_l)}{4 \cdot 28 N_s}$$

Typical values:  $N_l=100$ ,  $N_s=8$  gives  $R_c = 11.3$

Neglects finding the velocity direction

$N_l$  – Number samples in directional line       $N_s$  – Number of RF samples in estimate  
 $f_s$  – Sampling frequency       $F_f$  – Fraction of time for flow

## Determination at Different Angles



Directional lines are beamformed at different angles

Velocity profile  
Focus Lines along the vessel

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## Determination of Velocity Angle



$$R_{12n}(\theta) = \frac{\max\{R_{12}(k, \theta)\}}{R_{12}(0, \theta)}$$

$$\theta_m = \text{ArgMax}(R_{12n}(\theta))$$

Angle is found from maximum in normalized peak value of cross-correlation function.

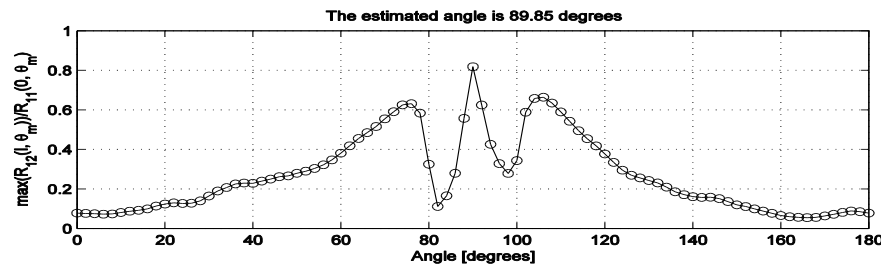
Value is interpolated using a second order polynomial to increase the accuracy.

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## Angle Determination at 90 deg

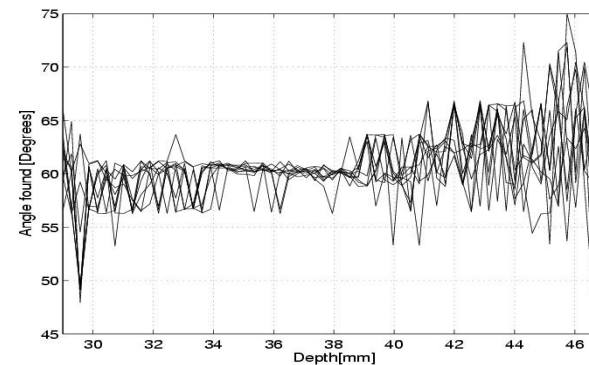


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## Estimated Velocity Angles at 60 deg



For all estimates:

Mean: 60.54 deg

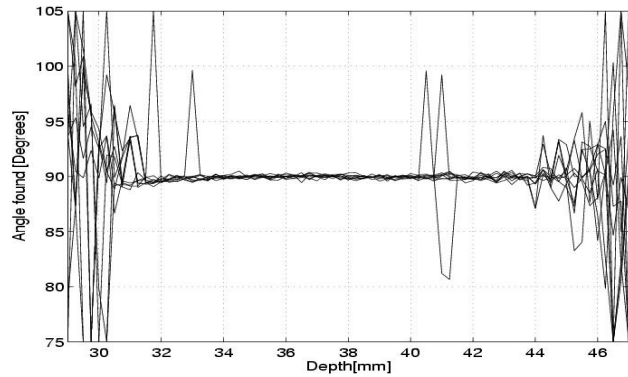
Std. 2.1 deg

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## Estimated Velocity Angles at 90 deg



For all estimates:

Mean: 90.0003 deg

Std. 1.32 deg

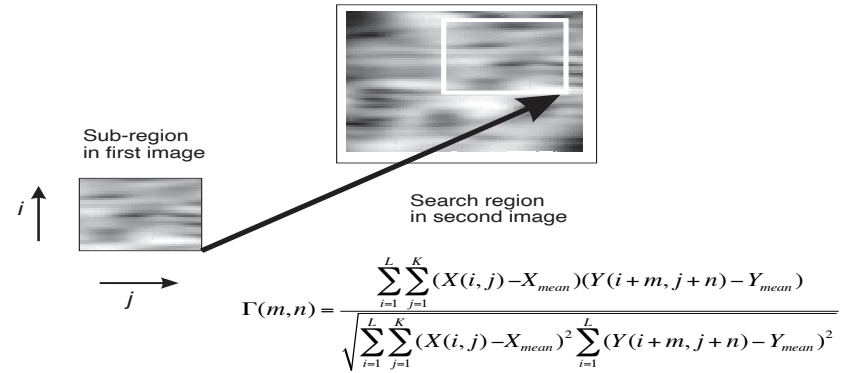
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## Speckle tracking

Search to find motion

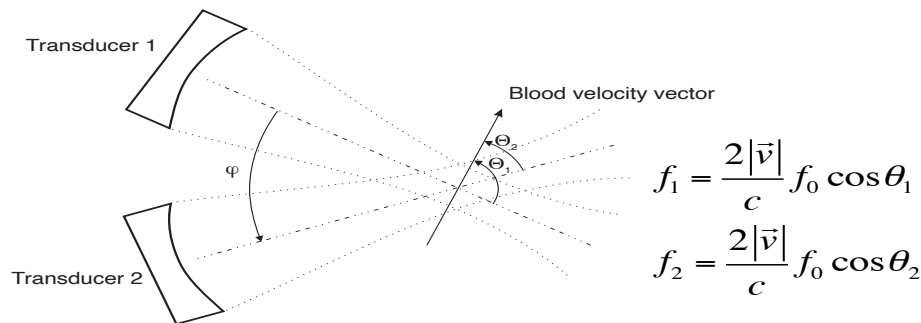


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## Crossed beams velocity estimation



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## Finding the velocity vector



- Calculation of the velocity components:

$$v_z = |\vec{v}| \cos \theta_1 = \frac{c}{2} \frac{f_1}{f_2}$$

$$v_x = |\vec{v}| \sin \theta_1 = \frac{c}{2} \frac{f_2 - f_1 \cos \varphi}{f_2 \sin \varphi}$$

$$\varphi = \theta_1 - \theta_2$$

$$\varphi = \arcsin \left( \frac{D_y / 2}{\sqrt{(D_y / 2)^2 + D_z^2}} \right)$$

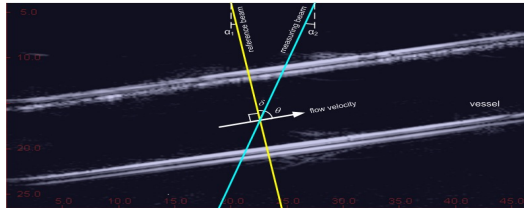
- Note how it is dependent on the angle difference

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## Dual beam method



**Assumption:**  
A reference beam can be transversely oriented to the flow direction

Angle estimation is based on inspection of the (transverse) Doppler spectrum

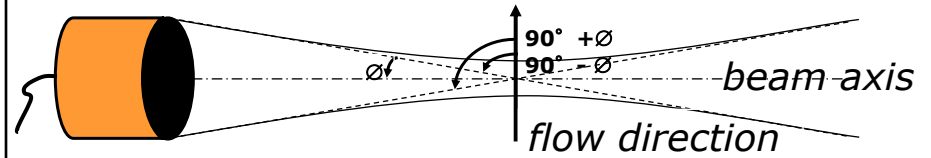
Slide courtesy of Piero Tortoli, University of Florence

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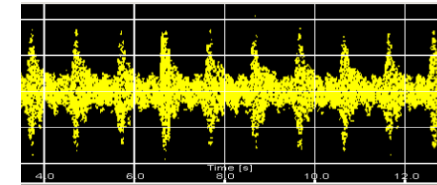
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## Transverse Doppler spectrum



The flow is interrogated by a range of angles around the nominal 90° Doppler angle



Corresponding spectrum is symmetrical around zero frequency

Slide courtesy of Piero Tortoli, University of Florence

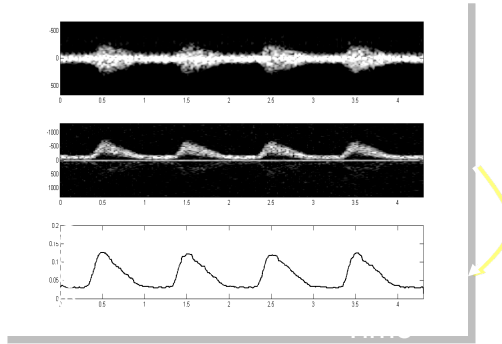
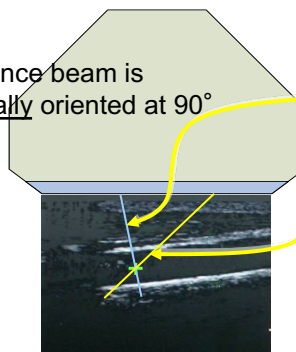
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## Automatic transverse angle tracking



The reference beam is automatically oriented at 90° to the flow



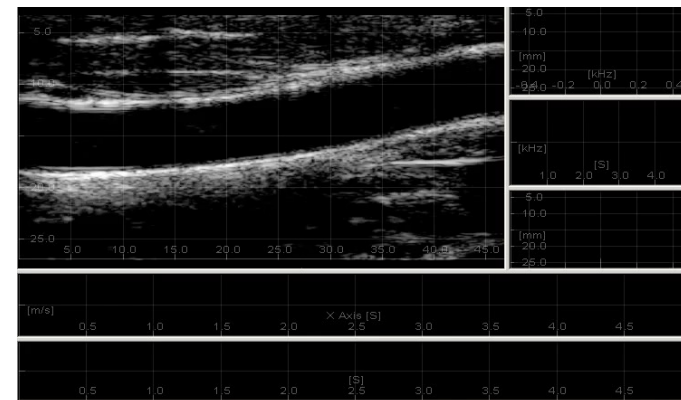
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## In vivo Test

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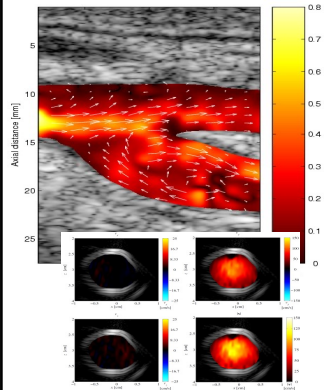
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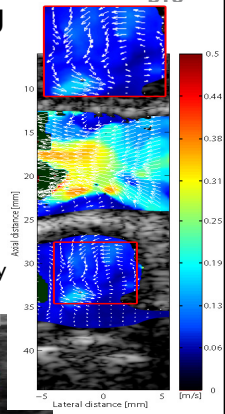
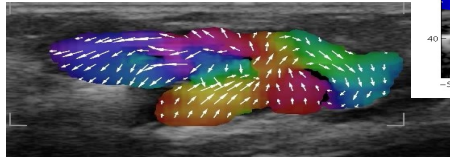
# Perspective on vector velocity imaging

DTU



- **Velocity imaging:**

- Velocity magnitude correctly identified
- No angle correction – correct magnitude and direction for all times and places
- Velocity is independent of transducer placement, which improves on workflow and accuracy
- Disturbed and turbulent flow can



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